

# 10<sup>th</sup> DIMACS Implementation Challenge – Graph Partitioning and Graph Clustering – **Results**

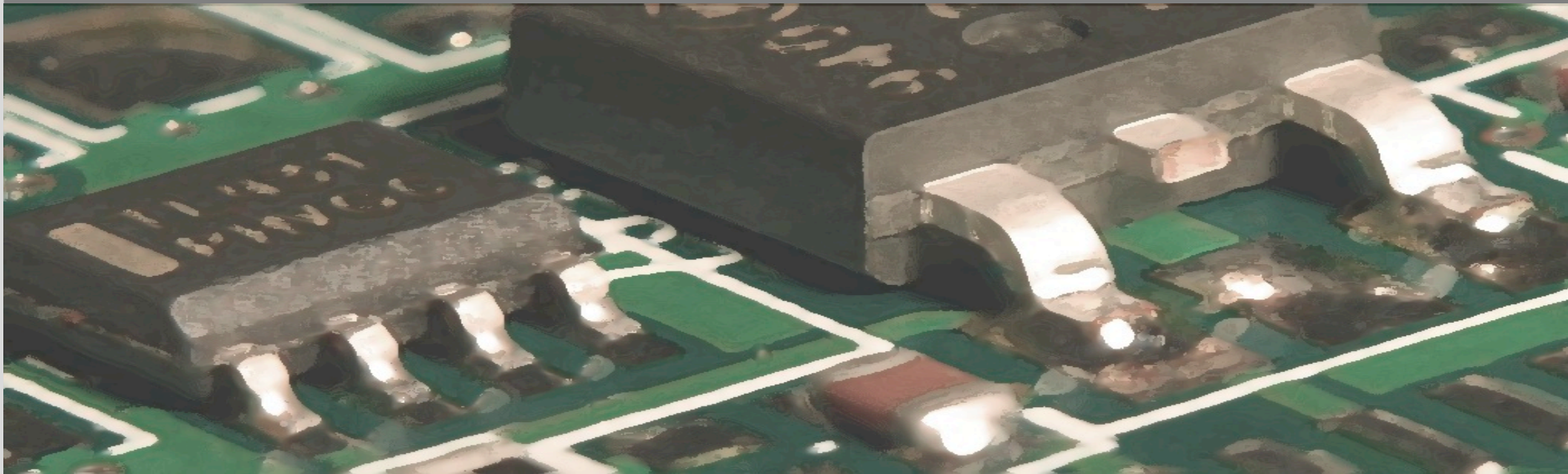
**David A. Bader**

School of Computational Science and Engineering, Georgia Institute of Technology, USA

**Henning Meyerhenke, Peter Sanders, Dorothea Wagner  
with Christian Schulz and Andrea Schumm**

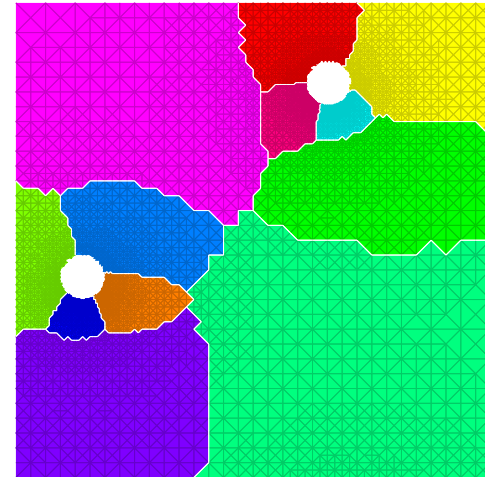
Institute of Theoretical Informatics, Karlsruhe Institute of Technology, Germany

Atlanta, Georgia · February 13/14, 2012

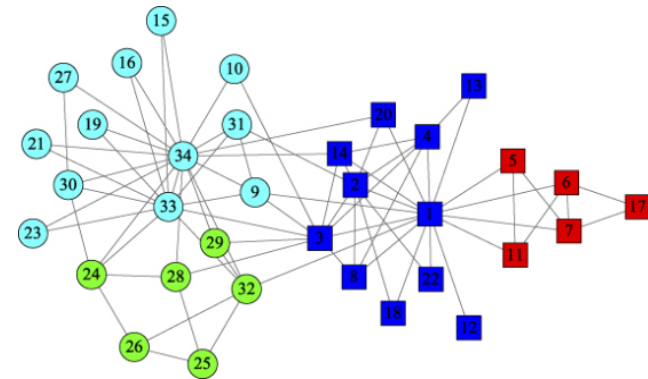


# Challenge Types

- Graph Partitioning
  - Quality Challenge
    - Edge Cut
    - Communication Volume
  - Pareto Challenge
    - Quality
    - Work

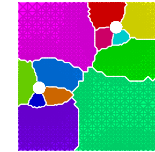


- Graph Clustering
  - Quality Challenge
    - Modularity
    - Mix
  - Pareto Challenge
    - Quality
    - Work

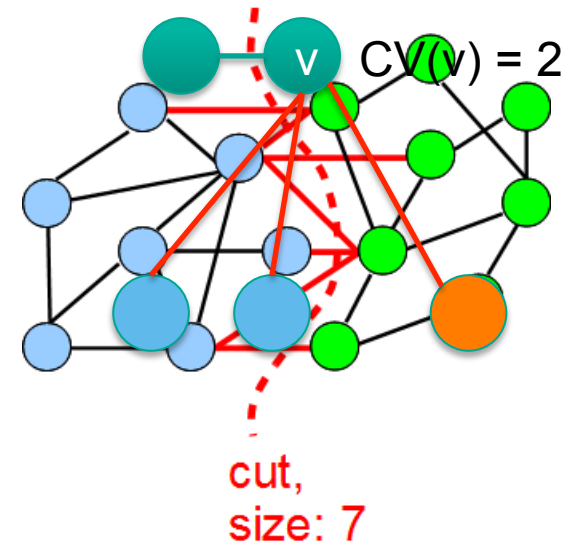


[Shen and Cheng, J. Stat. Mech. 2010]

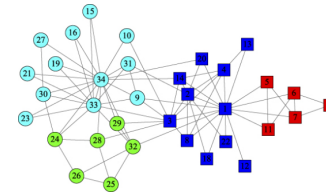
# Graph Partitioning – Objectives



- **Edge Cut:** Size of cut
- **Communication Volume:** Number of boundary vertices, counted as often as they are adjacent to different parts
- **Rationale:**
  - EC well established
  - CV more accurate in some apps
- k power of 2, between 2 and 1024
- 3% imbalance
- 90 instances (18 graphs with 5 values of k each) of different sizes



# Graph Clustering – Objectives



- **Modularity**
- **Mix:** Mixture of different objective functions
  - Performance
  - Average isolated inter-cluster conductance
  - Average isolated inter-cluster expansion
  - Minimum intra-cluster density
- **Rationale:**
  - Modularity popular, but has some flaws
  - Mix combines strengths (and weaknesses) of different measures
- 30 instances of different sizes

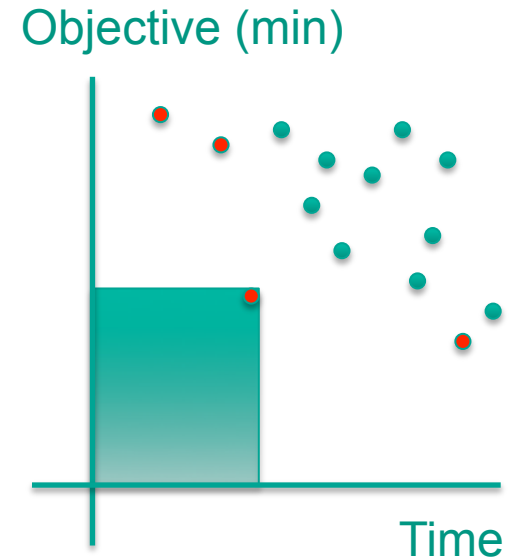
# Quality Scoring



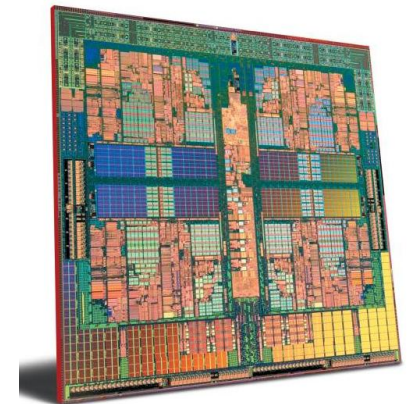
- Ranks given purely based on quality, F1 points for ranks: (10, 6, 4, 3, 2, 1)
- Each tuple (graph, k, objective) is an instance for which points are given
- **GP**: All points obtained are **accumulated** (EC + CV)
- **GC**: MO and MI are scored **separately**
  - Mix scoring rather complicated (look into the rules...)
- **The more points, the better!**

# Pareto Challenge Scoring

- **Rationale:** Quality is important, but also your investment (work) to get it
- **Two dimensions:** Work and quality
- **Work:** (Wall-clock) Running time scaled by capability of your system
- **Special considerations:**
  - Multicore CPUs
  - Clusters
  - Accelerators
- Performance on **graph algorithms** important
- **Normalization factor:**  $(\text{Number of cores})^{0.9} / \text{Benchmark timings}$  (9<sup>th</sup> DIMACS Impl. Challenge)



[techfresh.net]



[apcmag.com]

# CERTIFICATE OF EXCELLENCE

presented to

---

in recognition of your exceptional performance in the  
10th DIMACS Implementation Challenge - Graph Partitioning and Graph Clustering,  
held at Georgia Institute of Technology in Atlanta, Georgia,  
February 13<sup>th</sup> through February 14<sup>th</sup>, 2012.

---

David A. Bader  
Georgia Institute of Technology

---

Henning Meyerhenke  
Karlsruhe Institute of Technology

---

Peter Sanders  
Karlsruhe Institute of Technology

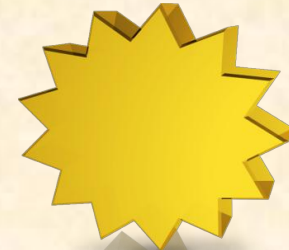
---

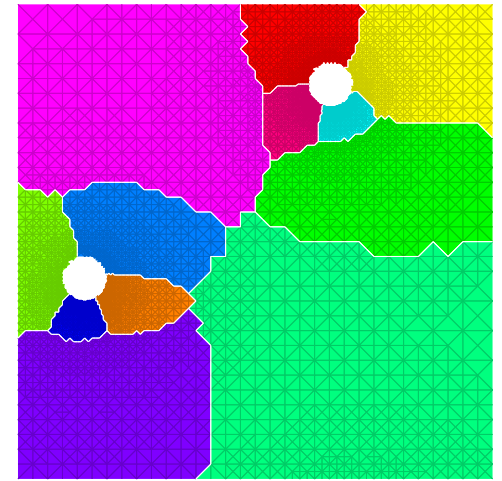
Dorothea Wagner  
Karlsruhe Institute of Technology

---

**DIMACS**

Center for Discrete Mathematics & Theoretical Computer Science  
Founded as a National Science Foundation Science and  
Technology Center



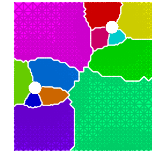


# GRAPH PARTITIONING RESULTS



# Results – Graph Partitioning

Quality Challenge (EC and CV combined)



## ■ Three solvers:

■ UMPa

(Catalyürek et al., OSU, ENS Lyon)

■ Mondriaan

(Fagginger Auer and Bisseling, Utrecht U)

■ Karlsruhe Partitioners (KaFFPa etc.) (Sanders and Schulz, KIT)

## ■ Formula 1 Points:

■ Karlsruhe Partitioners 1574

■ UMPa 1066

■ Mondriaan 616

## ■ Number of Best Ranked Solutions:

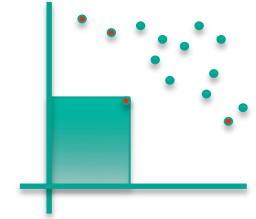
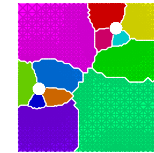
■ Karlsruhe Partitioners 139

■ UMPa 25

■ Mondriaan 6

# Results – Graph Partitioning

Pareto Challenge (EC and CV combined)



## ■ Six solvers:

- UMPa
- Mondriaan
- KaFFPaFast, KaFFPaEco, KaFFPaE, KaFFPaStrong

(Catalyürek et al., OSU, ENS Lyon)

(Fagginger Auer and Bisseling, Utrecht U)

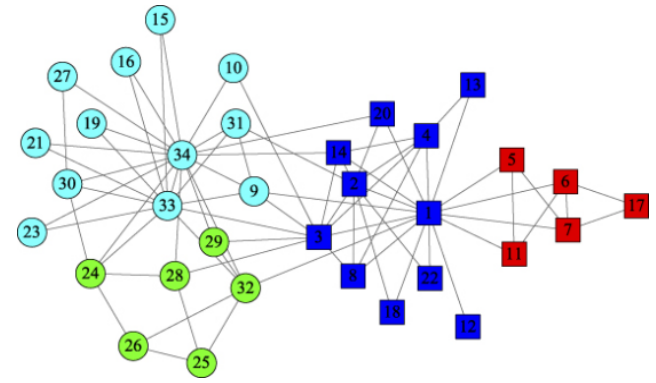
(Sanders and Schulz, KIT)

## ■ Formula 1 Points:

- KaFFPaFast 1680
- KaFFPaEco 1305
- KaFFPaE 1145
- KaFFPaStrong 1106
- UMPa Pareto 782
- Mondriaan 462

## ■ Number of Best Ranked Solutions:

- KaFFPaFast 168
- KaFFPaEco 122
- KaFFPaE 109
- KaFFPaStrong 100
- UMPa Pareto 53
- Mondriaan 27



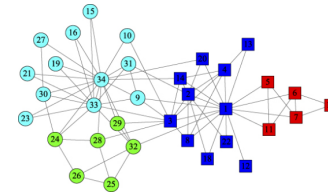
# MODULARITY RESULTS

# Results – Modularity

## Quality Challenge: Solvers

### ■ 15 solvers from 8 groups:

- CGGCI\_RG
- RG
- RG+
- ParMod
- CLU\_TBB
- CLU\_CUDA
- Scalable and Accurate...
- community-el
- community-el-xmt2
- k-Community
- k-Community++
- VNS\_quality
- Stable Communities
- Stable Communities HD
- Stable Communities BC



(Ovelgönne and Geyer-Schulz, KIT)

(Catalyürek et al., OSU, ENS Lyon)

(Fagginger Auer and Bisseling, Utrecht U)

(Djidjev and Onus, LANL, Cankaya U)

(Riedy et al., Georgia Tech, KIT)

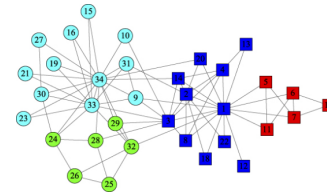
(Verma and Butenko, Texas A&M U)

(Aloise et al., UF Rio Grande et al.)

(Bhowmick and Srinivasan, UNO)

# Results – Modularity

## Quality Challenge



### ■ Formula 1 Points:

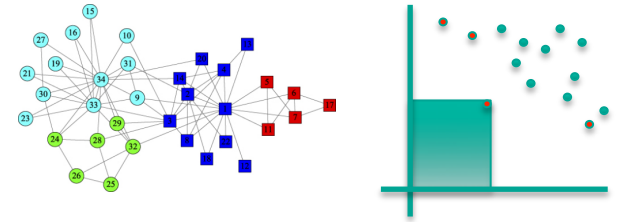
|                            |     |
|----------------------------|-----|
| ■ CGGCI_RG                 | 222 |
| ■ VNS_quality              | 196 |
| ■ ParMod                   | 115 |
| ■ RG+                      | 100 |
| ■ RG                       | 54  |
| ■ Scalable and Accurate... | 34  |
| ■ community-el             | 16  |
| ■ community-el-xmt2        | 16  |
| ■ CLU_TBB                  | 5   |
| ■ ...                      | <=1 |

### ■ # Rank 1:

|                     |    |
|---------------------|----|
| ■ CGGCI_RG          | 15 |
| ■ VNS_quality       | 11 |
| ■ ParMod            | 2  |
| ■ community-el      | 1  |
| ■ community-el-xmt2 | 1  |
| ■ ...               | 0  |

# Results – Modularity

## Pareto Challenge



- 10 (out of 15) solvers remain

### ■ Formula 1 Points:

|                            |     |
|----------------------------|-----|
| ■ RG                       | 264 |
| ■ CGGCI_RG                 | 256 |
| ■ RG+                      | 256 |
| ■ CLU_TBB                  | 202 |
| ■ Scalable and Accurate... | 117 |
| ■ VNS_pareto               | 116 |
| ■ community_el             | 59  |
| ■ CLU_CUDA                 | 27  |
| ■ community-el-xmt2        | 17  |
| ■ ...                      | <=5 |

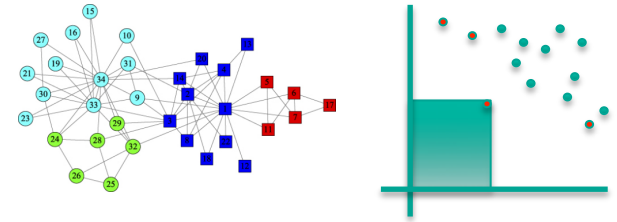
### ■ # Rank 1:

|                            |    |
|----------------------------|----|
| ■ RG                       | 26 |
| ■ CGGCI_RG                 | 25 |
| ■ RG+                      | 25 |
| ■ CLU_TBB                  | 19 |
| ■ VNS_pareto               | 9  |
| ■ Scalable and Accurate... | 8  |
| ■ CLU_CUDA                 | 2  |
| ■ community_el             | ?  |
| ■ ...                      | 0  |

# Results – Modularity

## Pareto Challenge

without normalizing system performance

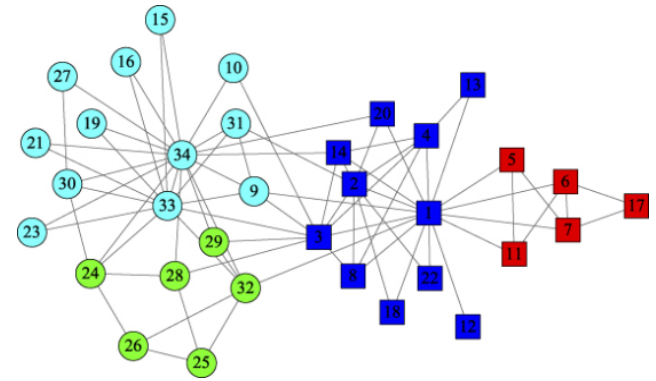


### ■ Formula 1 Points:

|                            |     |
|----------------------------|-----|
| ■ RG+                      | 255 |
| ■ CLU_TBB                  | 247 |
| ■ RG                       | 246 |
| ■ CGGCI_RG                 | 240 |
| ■ VNS_pareto               | 152 |
| ■ community-el             | 150 |
| ■ Scalable and Accurate... | 111 |
| ■ CLU_CUDA                 | 52  |
| ■ community-el-xmt2        | 18  |
| ■ ...                      | 0   |

### ■ Wall clock running time (minutes) for uk-2002 (n=18 520 486, m=261 787 258):

|                            |        |
|----------------------------|--------|
| ■ RG+                      | 228.5  |
| ■ CLU_TBB                  | 0.5    |
| ■ RG                       | 13.2   |
| ■ CGGCI_RG                 | 7981.0 |
| ■ VNS_pareto               |        |
| ■ community-el             | 3.0    |
| ■ Scalable and Accurate... |        |
| ■ CLU_CUDA                 |        |
| ■ community-el-xmt2        | 12.9   |

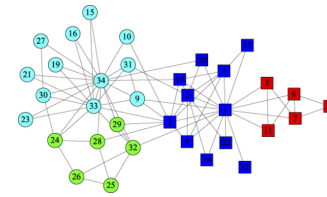


# MIX CHALLENGE RESULTS



# Results – Mix

## Quality Challenge



4 (out of 15) solvers remain:

community-el  
community-el-xmt2  
k-Community  
k-Community++

(Riedy et al., Georgia Tech, KIT)

(Verma and Butenko, Texas A&M U)

### ■ Formula 1 Points:

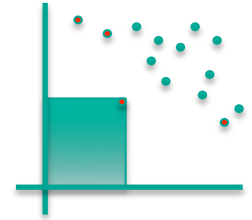
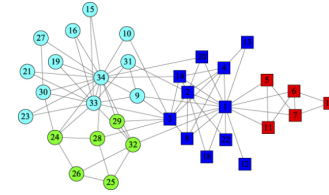
|                     |     |
|---------------------|-----|
| ■ community-el      | 155 |
| ■ community-el-xmt2 | 153 |
| ■ k-Community++     | 146 |
| ■ k-Community       | 78  |

### ■ # Rank 1:

|                     |    |
|---------------------|----|
| ■ community-el      | 10 |
| ■ community-el-xmt2 | 9  |
| ■ k-Community++     | 9  |
| ■ k-Community       | 4  |

# Results – Mix

## Pareto Challenge



■ 3 (out of 4) solvers remain

■ Formula 1 Points:

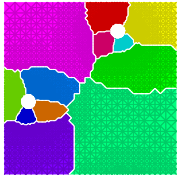
|                 |     |
|-----------------|-----|
| ■ community-el  | 182 |
| ■ k-Community++ | 152 |
| ■ k-Community   | 110 |

■ # Rank 1:

|                 |    |
|-----------------|----|
| ■ community-el  | 16 |
| ■ k-Community++ | 10 |
| ■ k-Community   | 8  |

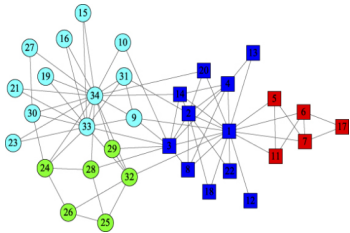
# Challenge Summary

- Many submissions for modularity 😊
- Few for the two other categories 😞



- **KaFFPa variants** dominate graph partitioning (both competitors focus on hypergraphs)

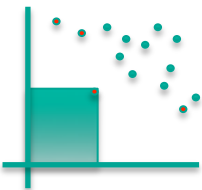
- **RG variants** best for modularity, even in Pareto challenge



- Mixed challenge sees two entrants, **community-el** slightly better than **k-Community++**

- Pareto Challenge did not yield significantly different results

- Likely due to Formula 1 scoring scheme



# WORKSHOP SUMMARY

# Workshop Summary

- Let's make this quick...
- Participation:
  - 19 contributed papers
  - GP: 3 groups
  - MO: 8 groups
  - MI: 2 groups
- Clustering has become the dominant topic
- Outreach:
  - Encyclopedia of SNA and Mining
  - ISMP 2012
- Please fill out your questionnaire
- Remove me from your SPAM list! ;-)



# What happens next

- **Soon:** Several of the best workshop papers will be invited to write extended versions for an AMS-DIMACS book on the DIMACS Challenge Workshop
- Selection based on:
  - Scientific merit and novelty
  - Challenge results
- Tentative deadlines:
  - Submissions due in **March**
  - Review decision mailed in **May**
  - Final version due in **June**
- Details will be sent to authors of invited papers



# Acknowledgments

## People involved

- Advisory board:
  - Bruce Hendrickson, Sandia National Laboratories
  - David S. Johnson, AT&T Labs – Research
  - Timothy G. Mattson, Intel Corp, Comput. Software Laboratory
  - Chris Walshaw, University of Greenwich
- DIMACS:
  - Fred Roberts, Rebecca Wright
  - Nicole Clark, Linda Casals, ...
- KIT:
  - Christian Schulz
  - Andrea Schumm
  - Robert Görke
- Georgia Tech:
  - Della Phinisee

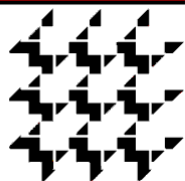
T  
H  
A  
N  
K  
S  
!

# Acknowledgments

## Sponsors

**DIMACS**

Center for Discrete Mathematics & Theoretical Computer Science  
Founded as a National Science Foundation Science and  
Technology Center



- Provided travel grants, waived registration fees and other goodies!

Finally, thank you  
for your participation!!!