Attention and Transformers

Arjun Majumdar Georgia Tech

Slide Credits: Andrej Karpathy, Justin Johnson, Dhruv Batra

Lecture Outline

- Machine Translation with RNNs
- RNNs with Attention
- From Attention to Transformers
- What can Transformers do?

Sequence Modeling with RNNs

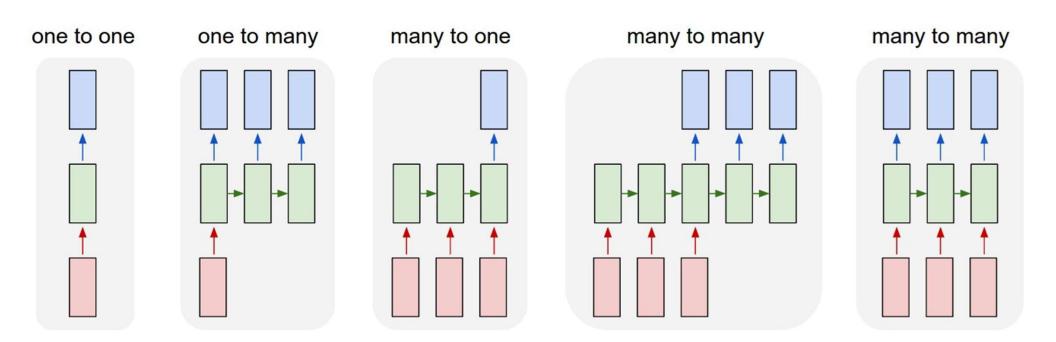


Image Credit: Andrej Karpathy

Machine Translation

we are eating bread



estamos comiendo pan

Machine Translation

estamos comiendo pan

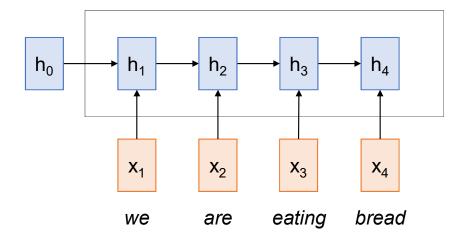
RNN Encoder



RNN Decoder

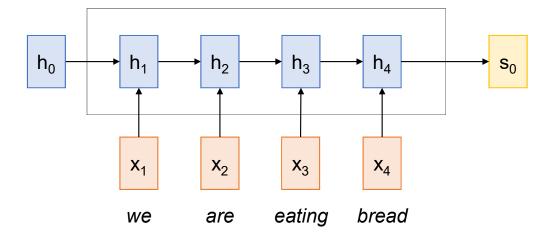
we are eating bread

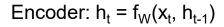
Encoder: $h_t = f_W(x_t, h_{t-1})$



Encoder: $h_t = f_W(x_t, h_{t-1})$

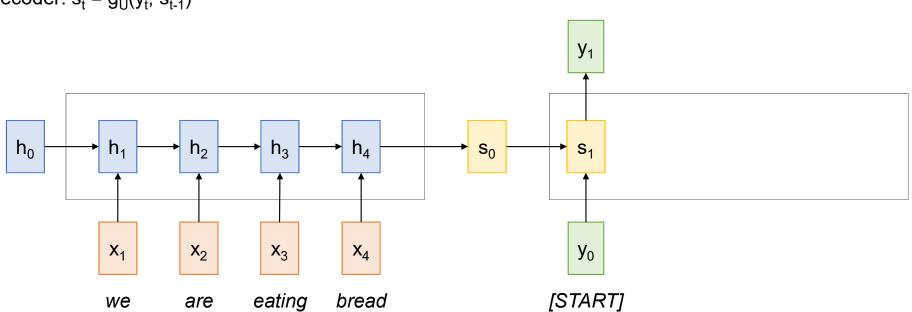
$$s_0 = h_4$$





Decoder: $s_t = g_U(y_t, s_{t-1})$

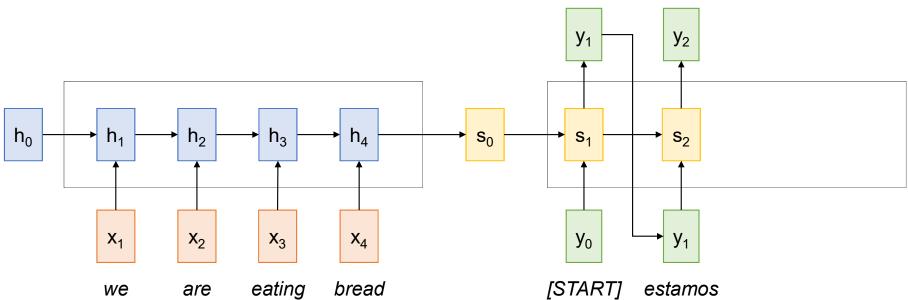


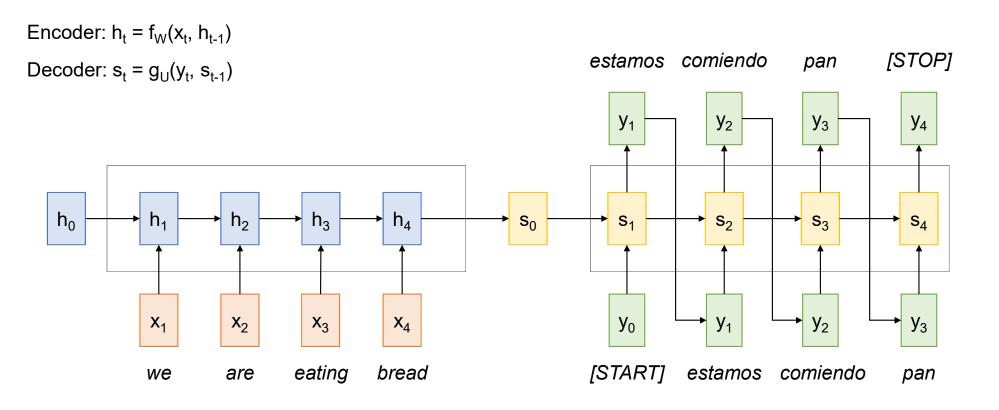


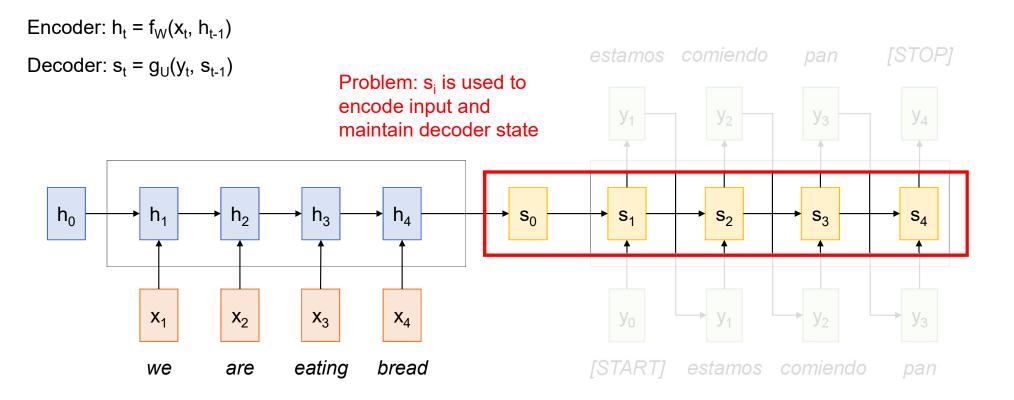
Encoder: $h_t = f_W(x_t, h_{t-1})$

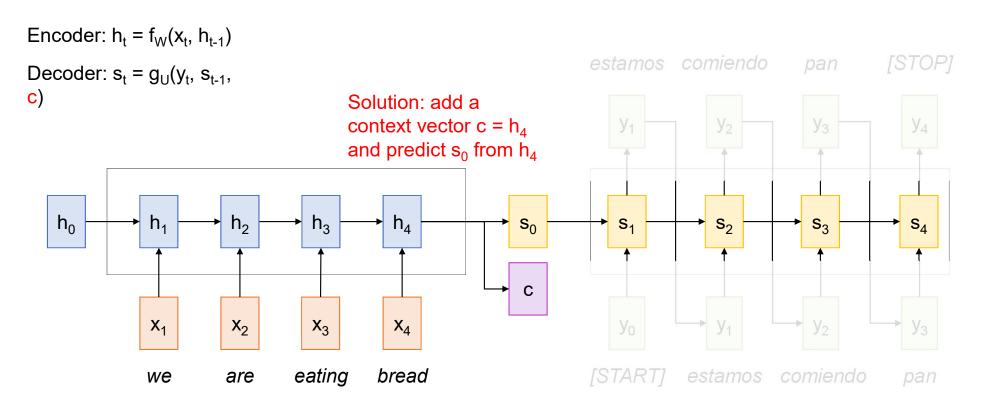
Decoder: $s_t = g_U(y_t, s_{t-1})$

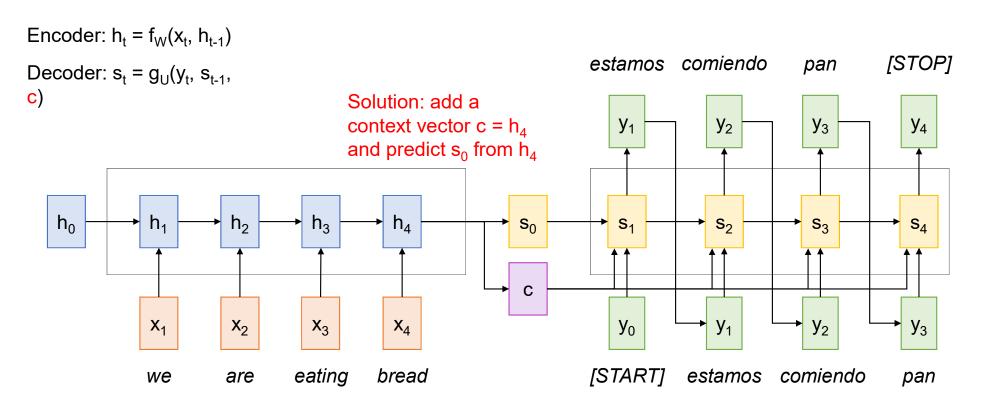
estamos comiendo

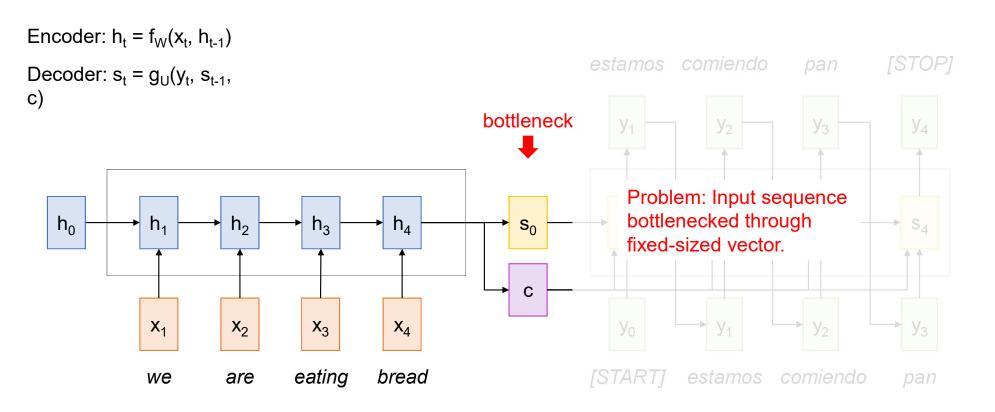


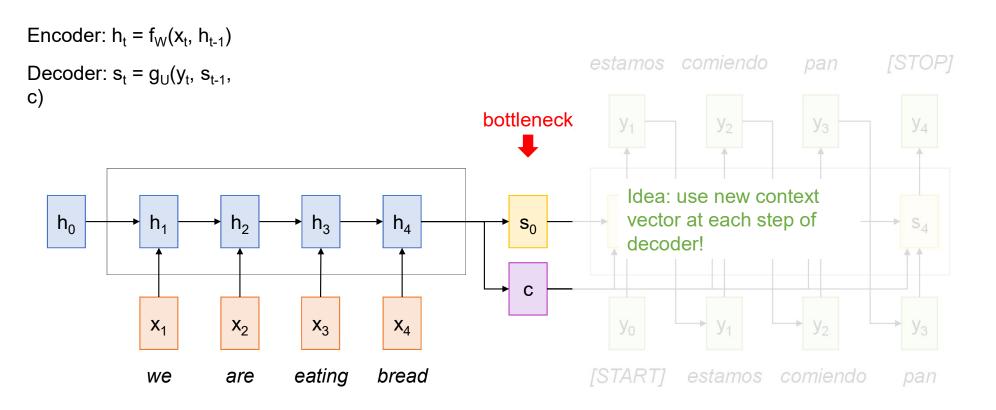




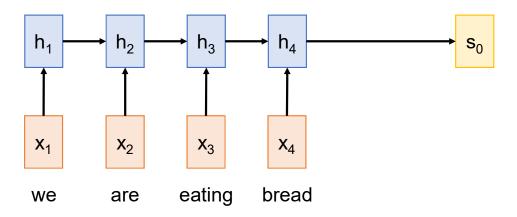








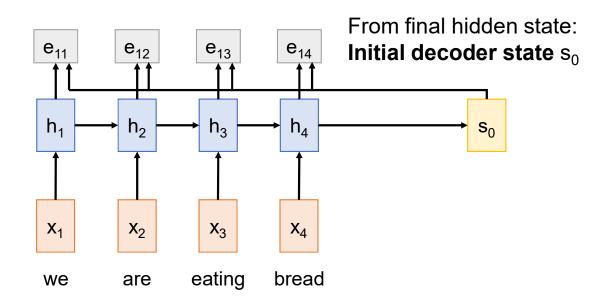
From final hidden state: **Initial decoder state** s₀



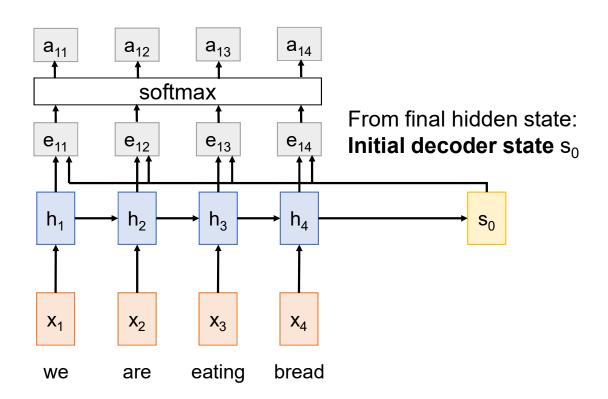
Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

Compute alignment scores

$$e_{t,i} = f_{att}(s_{t-1}, h_i)$$
 (f_{att} is an MLP)



Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015



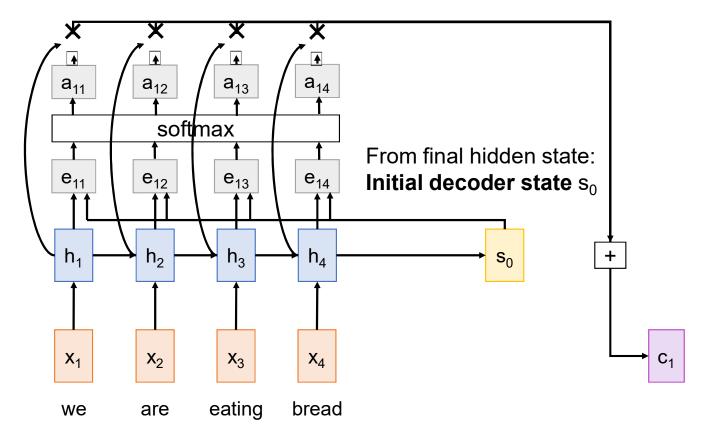
Compute alignment scores

$$e_{t,i} = f_{att}(s_{t-1}, h_i)$$
 (f_{att} is an MLP)

Normalize to get attention weights

$$0 < \alpha_{t,i} < 1$$
 $\sum_{i} \alpha_{t,i} = 1$

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015



Compute alignment scores

$$\mathbf{e}_{t,i} = \mathbf{f}_{\alpha tt}(\mathbf{s}_{t-1}, \mathbf{h}_i)$$
 (\mathbf{f}_{α}

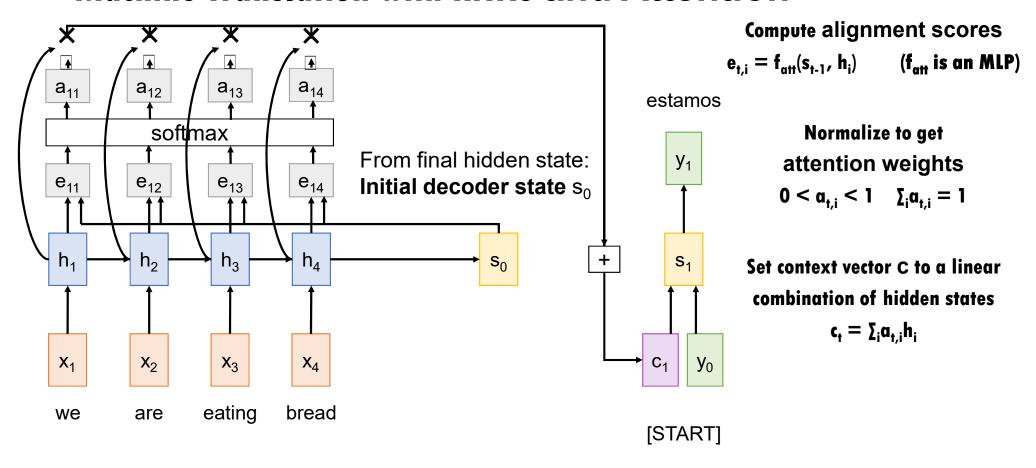
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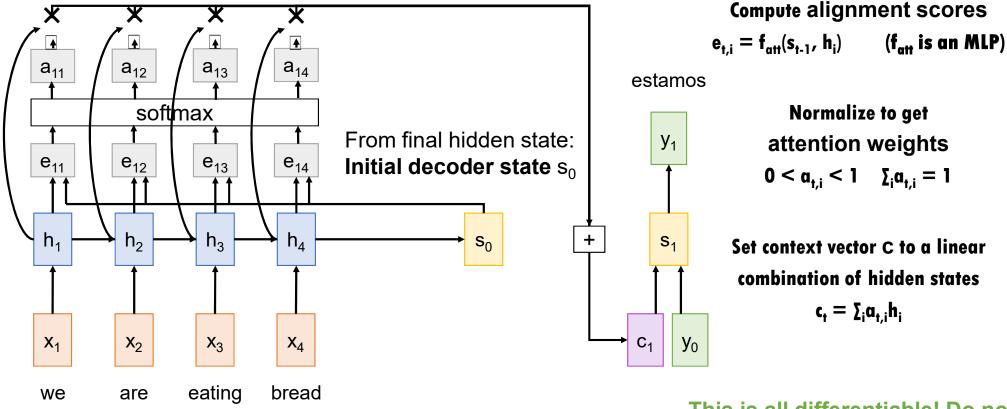
$$0 < \alpha_{t,i} < 1$$
 $\sum_{i} \alpha_{t,i} = 1$

Set context vector C to a linear combination of hidden states

$$c_t = \sum_i a_{t,i} h_i$$

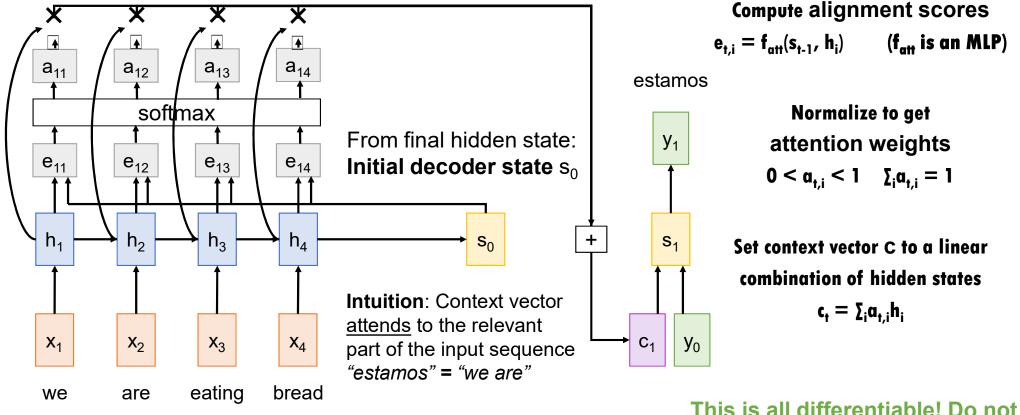


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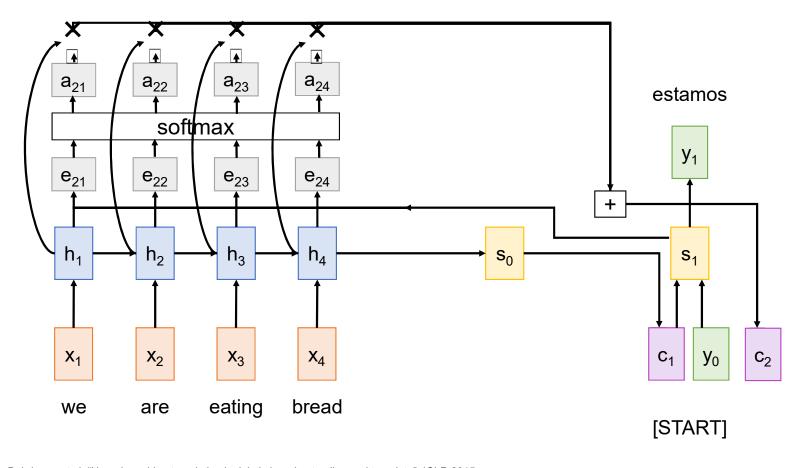
This is all differentiable! Do not supervise attention weights – backprop through everything



Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

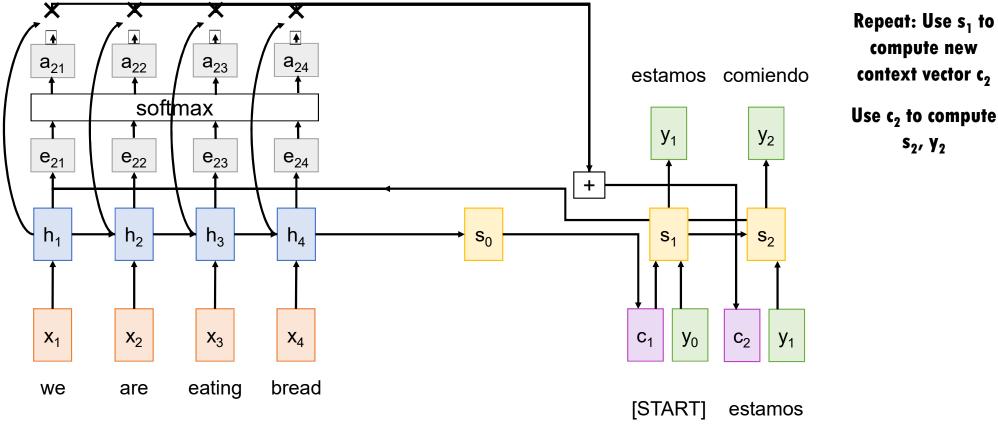
 $a_{11}=0.45$, $a_{12}=0.45$, $a_{13}=0.05$, $a_{14}=0.05$

supervise attention weights –
backprop through everything



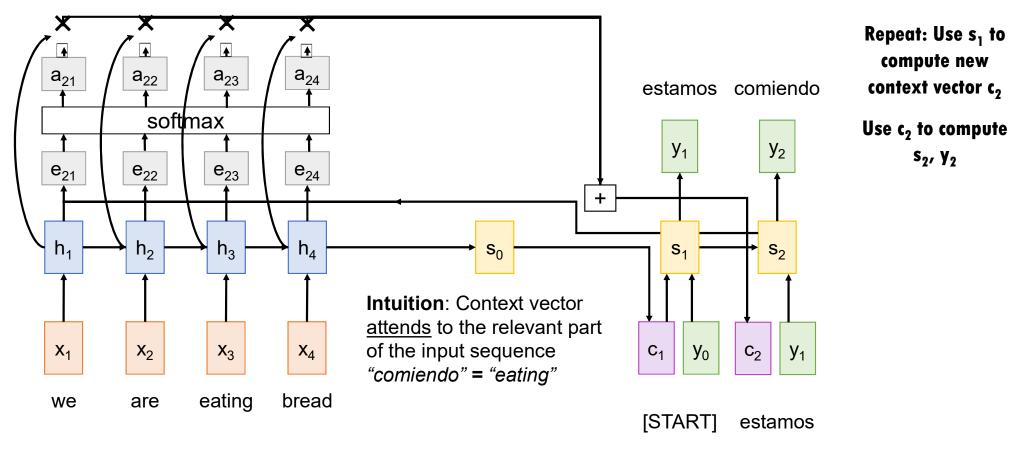
Repeat: Use s₁ to compute new context vector c₂

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015



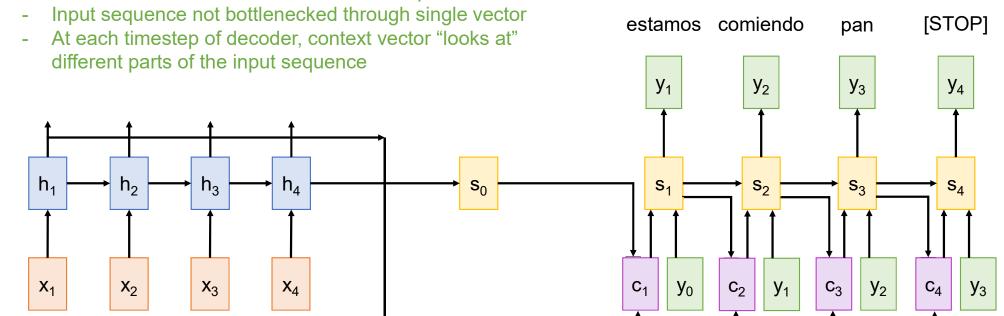
context vector c₂ Use c₂ to compute

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015



Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

Use a different context vector in each timestep of decoder



[START]

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

eating

we

are

bread

Slide credit: Justin Johnson

pan

estamos comiendo

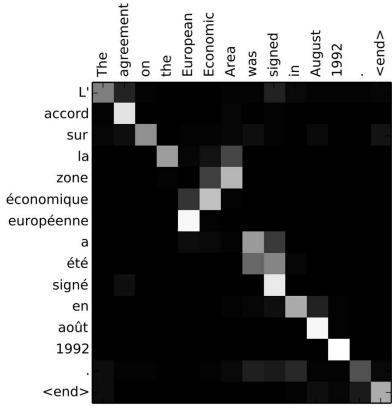
Example: English to French translation

Input: "The agreement on the European Economic Area was signed in August 1992."

Output: "L'accord sur la zone économique européenne a été signé en août 1992."

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

Visualize attention weights a_{t,i}



Example: English to French translation

Input: "The agreement on the European Economic Area was signed in August 1992."

Output: "L'accord sur la zone économique européenne a été signé en août 1992."

Diagonal attention means words correspond in order

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Visualize attention weights ati accord sur zone économique européenne été signé en août 1992 <end>

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

Example: English to French translation

Input: "The agreement on the European Economic Area was signed in August 1992."

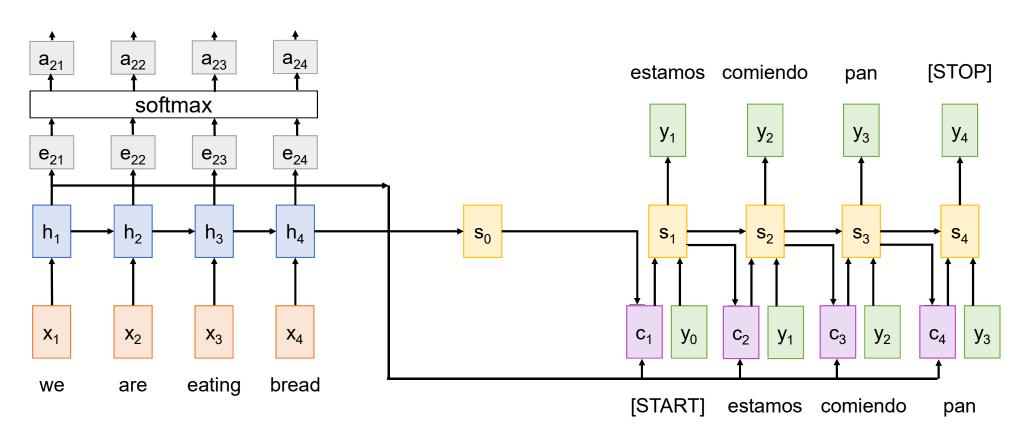
Output: "L'accord sur la zone économique européenne a été signé en août 1992."

Diagonal attention means words correspond in order Attention figures out different word orders

Diagonal attention means words correspond in order

Visualize attention weights ati accord sur la zone économique européenne été signé en août 1992 <end>

Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015



Bahdanau et al, "Neural machine translation by jointly learning to align and translate", ICLR 2015

Inputs:

State vector: **s**_i (Shape: D_Q)

Hidden vectors: \mathbf{h}_{i} (Shape: $N_{X} \times D_{H}$)

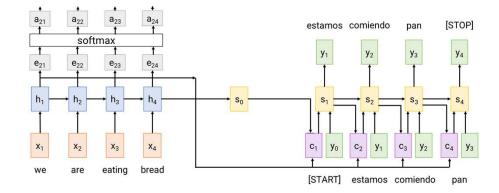
Similarity function: f_{att}

Computation:

Similarities: e (Shape: N_X) $e_i = f_{att}(s_{t-1}, h_i)$

Attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i h_i$ (Shape: D_X)



Inputs:

Query vector: q (Shape: D_Q)

Input vectors: X (Shape: $N_X \times D_X$)

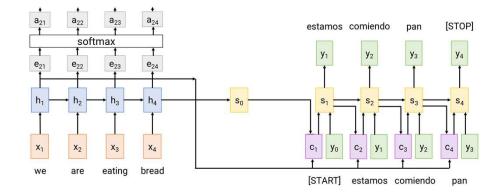
Similarity function: fatt

Computation:

Similarities: e (Shape: N_X) $e_i = f_{att}(\mathbf{q}, \mathbf{X}_i)$

Attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)



Inputs:

Query vector: **q** (Shape: D_O)

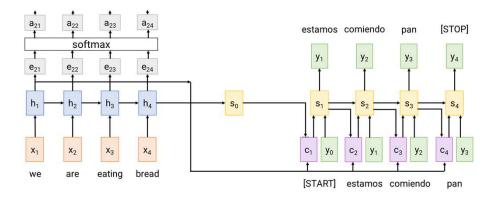
Input vectors: **X** (Shape: N_X x D_Q) **Similarity function**: dot product

Computation:

Similarities: e (Shape: N_X) $e_i = \mathbf{q} \cdot \mathbf{X}$

Attention weights: a = softmax(e) (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)



Changes:

- Use dot product for similarity

Inputs:

Query vector: **q** (Shape: D_O)

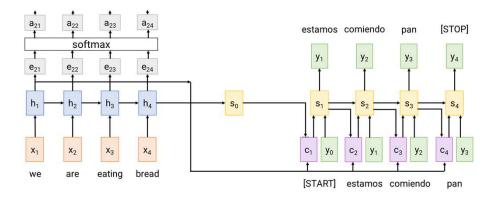
Input vectors: X (Shape: N_x x D_o)

Similarity function: scaled dot product

Computation:

Similarities: e (Shape: N_X) $e_i = \mathbf{q} \cdot \mathbf{X}_i / \operatorname{sqrt}(D_Q)$ Attention weights: $a = \operatorname{softmax}(e)$ (Shape: N_X)

Output vector: $y = \sum_i a_i X_i$ (Shape: D_X)

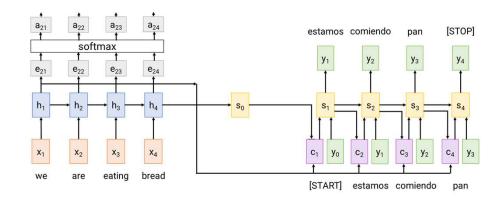


Changes:

Use scaled dot product for similarity

Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$)
Input vectors: X (Shape: $N_X \times D_Q$)



Computation:

Similarities: $E = \mathbf{QX^T}$ (Shape: $N_Q \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{X}_j / \operatorname{sqrt}(D_Q)$ **Attention weights**: $A = \operatorname{softmax}(E, \dim = 1)$ (Shape: $N_Q \times N_X$)

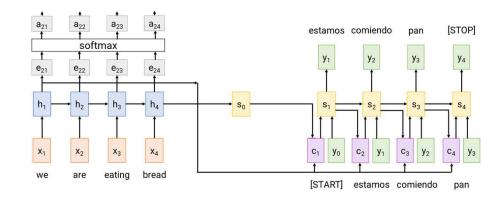
Output vectors: Y = AX (Shape: $N_Q \times D_X$) $Y_i = \sum_j A_{i,j} X_j$

Changes:

- Use dot product for similarity
- Multiple query vectors

Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$)



Computation:

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) Value vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^{T}$ (Shape: $N_Q \times N_X$) $E_{i,j} = Q_i \cdot K_j$ / $sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_i A_{i,j} V_j$

Changes:

- Use dot product for similarity
- Multiple query vectors
- Separate key and value

Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$)

Computation:

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_Q \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$

Attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

 X_1

 X_2

 X_3

Q 1 Q

Q

4

Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$)

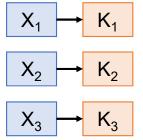
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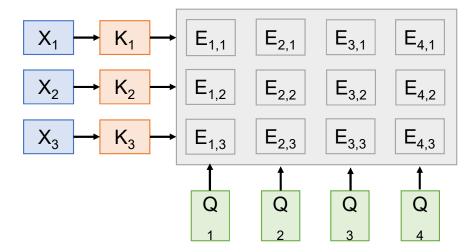
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Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Query vectors: Q (Shape: $N_Q \times D_Q$) Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$)

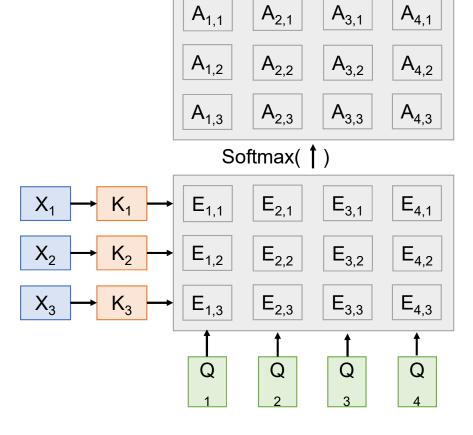
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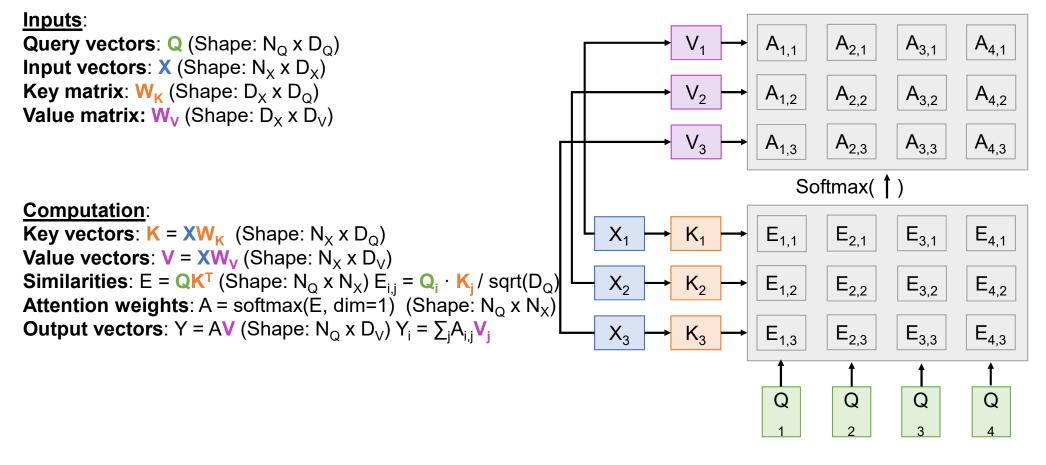
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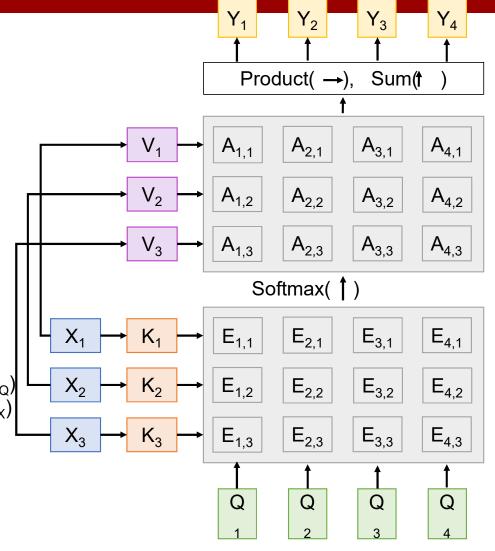
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Attention weights: A = softmax(E, dim=1) (Shape: $N_Q \times N_X$)

Output vectors: Y = AV (Shape: $N_Q \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



One query per input vector

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$)

Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$







One query per input vector

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Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$)

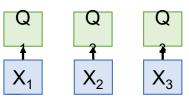
Computation:

Query vectors: Q = XW_Q

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

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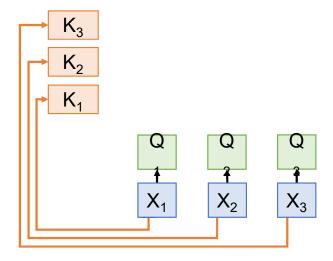
Computation:

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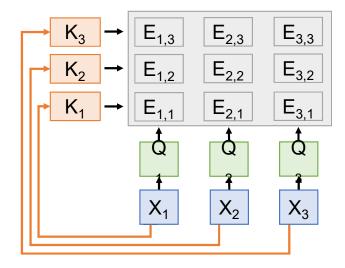
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Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



One query per input vector

Inputs:

Input vectors: \mathbf{X} (Shape: $N_X \times D_X$) Key matrix: \mathbf{W}_K (Shape: $D_X \times D_Q$) Value matrix: \mathbf{W}_V (Shape: $D_X \times D_V$) Query matrix: \mathbf{W}_Q (Shape: $D_X \times D_Q$)

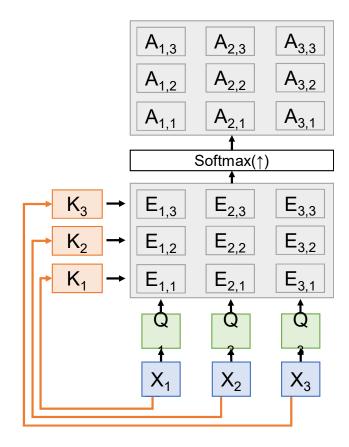
Computation:

Query vectors: Q = XW_o

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



One query per input vector

Inputs:

Input vectors: \mathbf{X} (Shape: $N_X \times D_X$) Key matrix: \mathbf{W}_K (Shape: $D_X \times D_Q$) Value matrix: \mathbf{W}_V (Shape: $D_X \times D_V$) Query matrix: \mathbf{W}_Q (Shape: $D_X \times D_Q$)

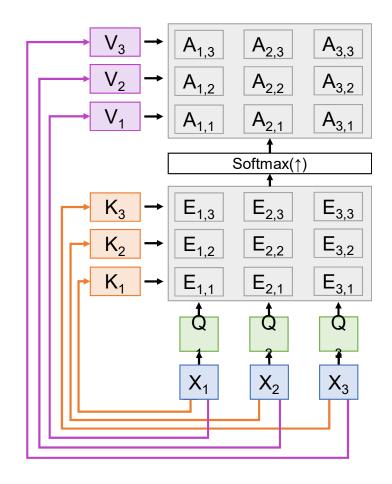
Computation:

Query vectors: Q = XW_o

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



One query per input vector

Inputs:

Input vectors: \mathbf{X} (Shape: $N_X \times D_X$) Key matrix: \mathbf{W}_K (Shape: $D_X \times D_Q$) Value matrix: \mathbf{W}_V (Shape: $D_X \times D_V$) Query matrix: \mathbf{W}_Q (Shape: $D_X \times D_Q$)

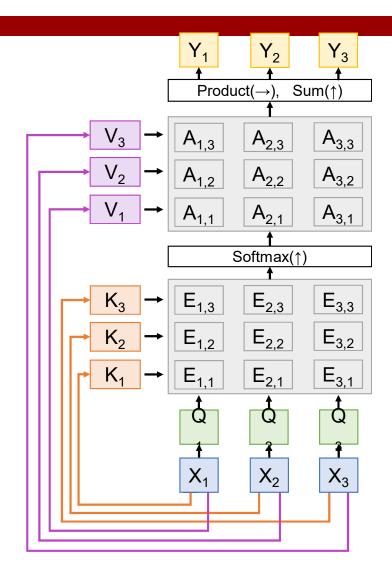
Computation:

Query vectors: Q = XW_o

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$) Consider **permuting** the input vectors:

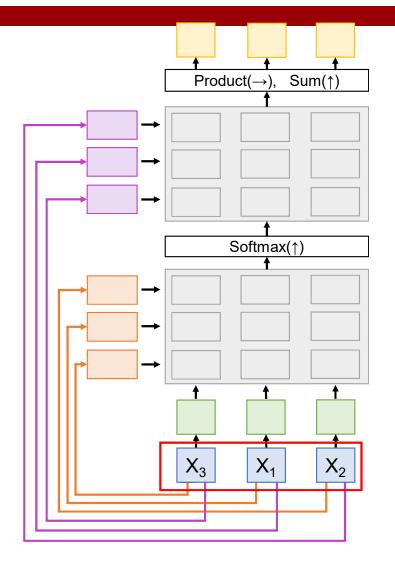
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$)

Consider **permuting** the input vectors:

Queries and Keys will be the same, but permuted

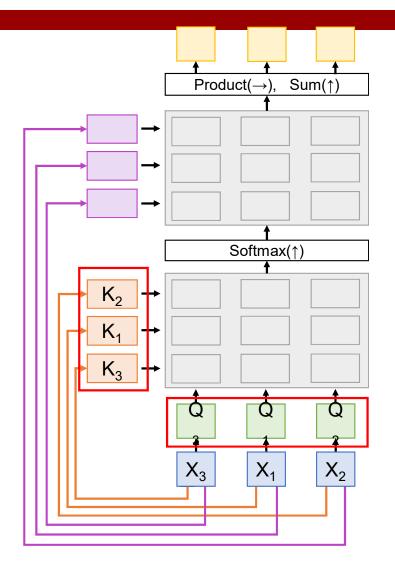
Computation:

Query vectors: Q = XW_o

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value Vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$) Consider **permuting** the input vectors:

Similarities will be the same, but permuted

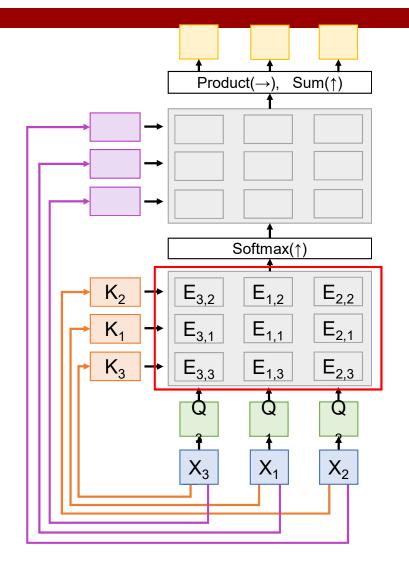
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ **Attention weights**: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$)

Consider **permuting** the input vectors:

Attention weights will be the same, but permuted

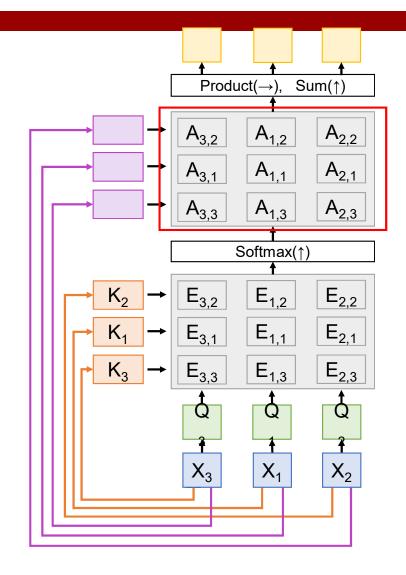
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ **Attention weights**: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$) Consider **permuting** the input vectors:

Values will be the same, but permuted

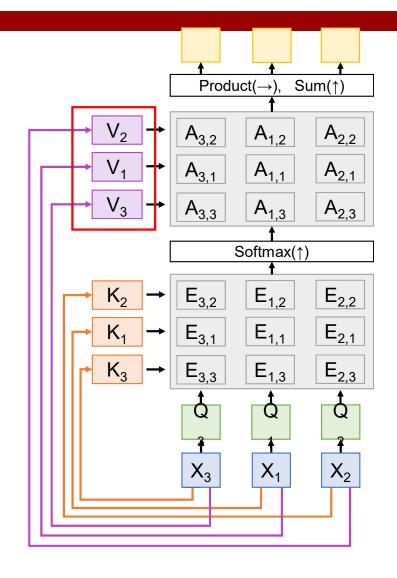
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ **Attention weights**: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$) Consider **permuting** the input vectors:

Outputs will be the same, but permuted

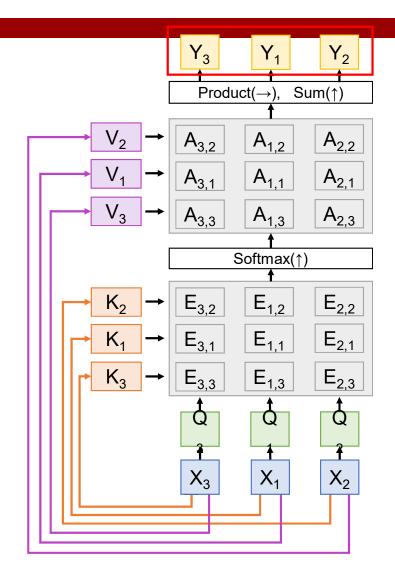
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_Q$)

Computation:

Query vectors: Q = XW_o

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$)

Value vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

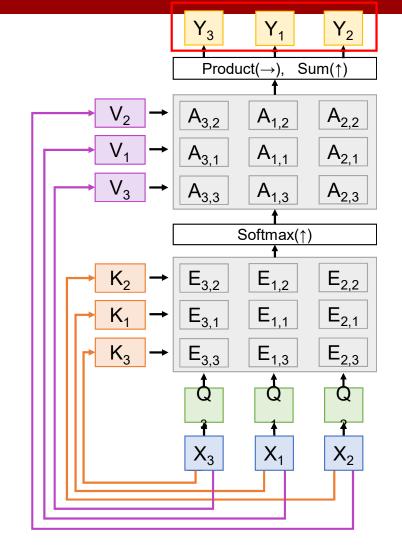
Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$

Consider **permuting** the input vectors:

Outputs will be the same, but permuted

Self-attention layer is **Permutation Equivariant** $f(x(x)) = e^{f(x)}$

f(s(x)) = s(f(x))



Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_Q (Shape: $D_X \times D_Q$) Self attention doesn't "know" the order of the vectors it is processing!

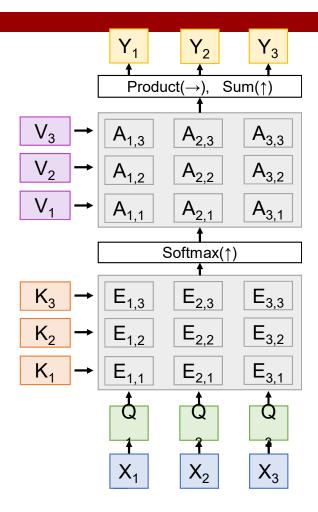
Computation:

Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Inputs:

Input vectors: X (Shape: $N_x \times D_x$) **Key matrix**: W_{κ} (Shape: $D_{\chi} \times D_{\Omega}$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: Wo (Shape: Dx x Do) Self attention doesn't "know" the order of the vectors it is processing!

In order to make processing position-aware, concatenate input with positional encoding

Computation:

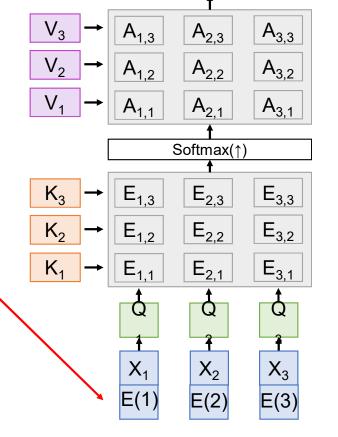
Query vectors: $Q = XW_0$

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) or fixed function

Similarities: $\overline{D}_X = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{QK^T}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j / \operatorname{sqrt}(D_Q)$ **Attention weights**: A = softmax(E, dim=1) (Shape: $N_x \times N_x$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_i A_{i,j} V_i$



 Y_3

Sum(↑)

 Y_2

 $Product(\rightarrow)$,

Masked Self-Attention Layer

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_Q$)

Don't let vectors "look ahead" in the sequence

Used for language modeling (predict next word)

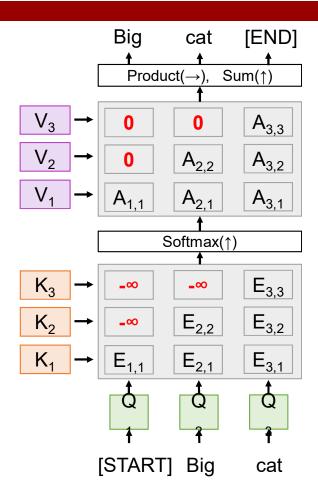
Computation:

Query vectors: Q = XW_Q

Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) **Value vectors**: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = \mathbf{QK^T}$ (Shape: $N_X \times N_X$) $E_{i,j} = \mathbf{Q}_i \cdot \mathbf{K}_j$ / $sqrt(D_Q)$ Attention weights: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$



Multihead Self-Attention Layer

Inputs:

Input vectors: X (Shape: $N_X \times D_X$) Key matrix: W_K (Shape: $D_X \times D_Q$) Value matrix: W_V (Shape: $D_X \times D_V$) Query matrix: W_O (Shape: $D_X \times D_Q$)

Use H independent "Attention Heads" in

parallel

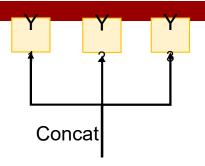
Computation:

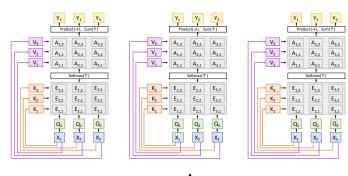
Query vectors: Q = XW_Q

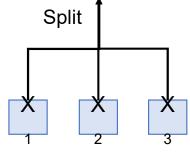
Key vectors: $K = XW_K$ (Shape: $N_X \times D_Q$) Value vectors: $V = XW_V$ (Shape: $N_X \times D_V$)

Similarities: $E = QK^T$ (Shape: $N_X \times N_X$) $E_{i,j} = Q_i \cdot K_j / sqrt(D_Q)$ **Attention weights**: A = softmax(E, dim=1) (Shape: $N_X \times N_X$)

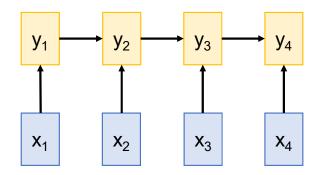
Output vectors: Y = AV (Shape: $N_X \times D_V$) $Y_i = \sum_j A_{i,j} V_j$







Recurrent Neural Network



Works on **Ordered Sequences**

(+) Good at long sequences: After one RNN layer, h_T "sees" the whole sequence

(-) Not parallelizable: need to compute hidden states sequentially

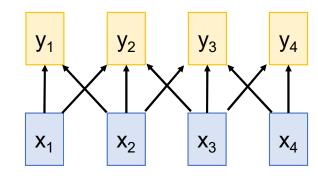
Recurrent Neural Network

 $\begin{array}{c|c} y_1 & \longrightarrow & y_2 & \longrightarrow & y_3 & \longrightarrow & y_4 \\ \uparrow & & \uparrow & & \uparrow & & \uparrow \end{array}$

 X_3

 X_4

1D Convolution



Works on **Ordered Sequences**

 X_2

 X_1

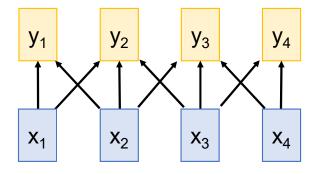
- (+) Good at long sequences: After one RNN layer, h_T "sees" the whole sequence
- (-) Not parallelizable: need to compute hidden states sequentially

Works on **Multidimensional Grids**

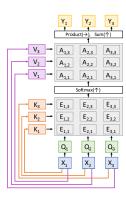
- (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
- (+) Highly parallel: Each output can be computed in parallel

Recurrent Neural Network

1D Convolution



Self-Attention



Works on **Ordered Sequences**

(+) Good at long sequences: After one RNN layer, h_T "sees" the whole sequence

(-) Not parallelizable: need to compute hidden states sequentially

Works on **Multidimensional Grids**

(-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence

(+) Highly parallel: Each output can be computed in parallel

Works on **Sets of Vectors**

(+) Good at long sequences: after one self-attention layer, each output "sees" all inputs!

(+) Highly parallel: Each output can be computed in parallel

(-) Very memory intensive

Recurrent Neural Network

1D Convolution

Self-Attention

Attention is all you need

Vaswani et al, NeurIPS 2017

Works on **Ordered Sequences**

- (+) Good at long sequences: After one RNN layer, h_T "sees" the whole sequence
- (-) Not parallelizable: need to compute hidden states sequentially

Works on **Multidimensional Grids**

- (-) Bad at long sequences: Need to stack many conv layers for outputs to "see" the whole sequence
- (+) Highly parallel: Each output can be computed in parallel

Works on **Sets of Vectors**

- (+) Good at long sequences: after one self-attention layer, each output "sees" all inputs!
- (+) Highly parallel: Each output can be computed in parallel
- (-) Very memory intensive

X₁

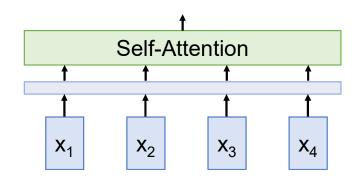
X₂

X₃

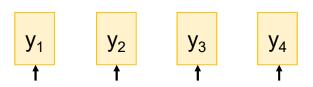
X₄

Vaswani et al, "Attention is all you need", NeurIPS 2017

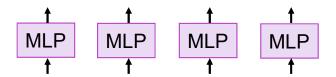
All vectors interact with each other



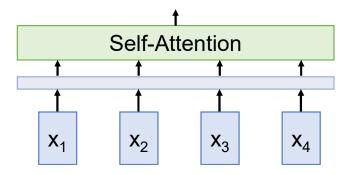
Vaswani et al, "Attention is all you need", NeurIPS 2017



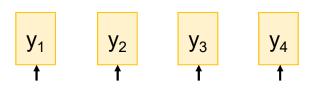
MLP independently on each vector



All vectors interact with each other



Vaswani et al, "Attention is all you need", NeurlPS 2017

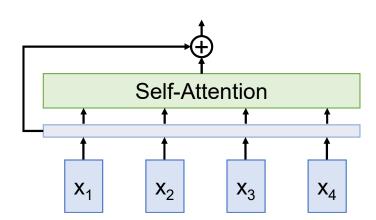


MLP independently on each vector

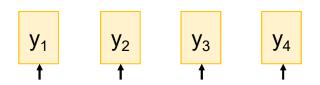


Residual connection

All vectors interact with each other



Vaswani et al, "Attention is all you need", NeurlPS 2017



Recall Layer Normalization:

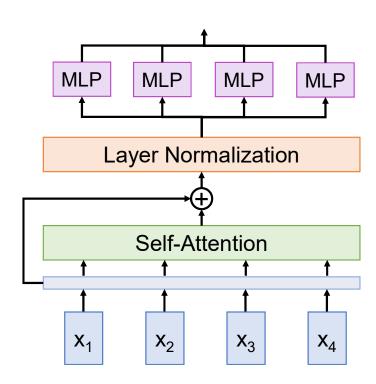
Given
$$h_1, ..., h_N$$
 (Shape: D)
scale: γ (Shape: D)
shift: β (Shape: D)
 $\mu_i = (1/D)\sum_j h_{i,j}$ (scalar)
 $\sigma_i = (\sum_j (h_{i,j} - \mu_i)^2)^{1/2}$ (scalar)
 $z_i = (h_i - \mu_i) / \sigma_i$
 $y_i = \gamma * z_i + \beta$

Ba et al, 2016

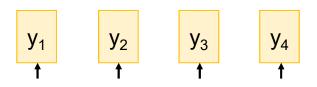
MLP independently on each vector

Residual connection

All vectors interact with each other



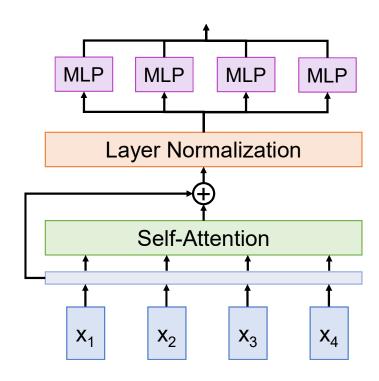
Vaswani et al, "Attention is all you need", NeurIPS 2017



MLP independently on each vector

Residual connection

All vectors interact with each other



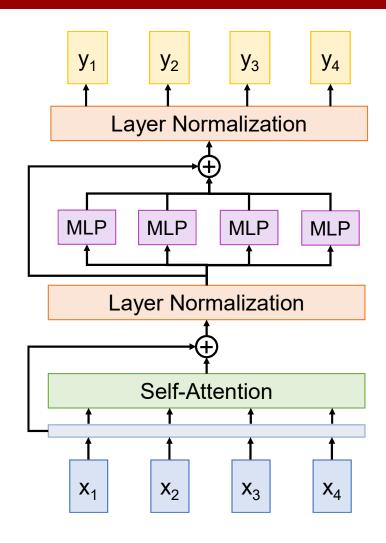
Vaswani et al, "Attention is all you need", NeurlPS 2017

Residual connection

MLP independently on each vector

Residual connection

All vectors interact with each other



Vaswani et al, "Attention is all you need", NeurIPS 2017

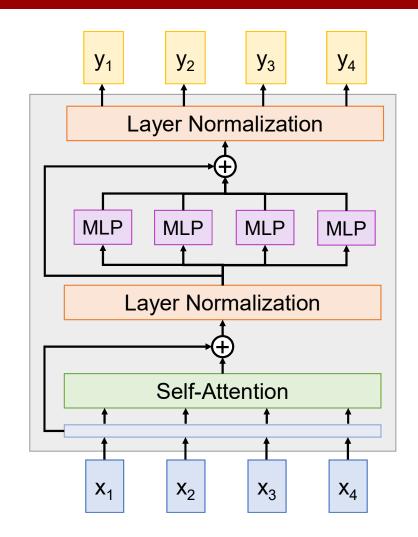
Transformer Block:

Input: Set of vectors x
Output: Set of vectors y

Self-attention is the only interaction between vectors!

Layer norm and MLP work independently per vector

Highly scalable, highly parallelizable



Vaswani et al, "Attention is all you need", NeurIPS 2017

Transformer Block:

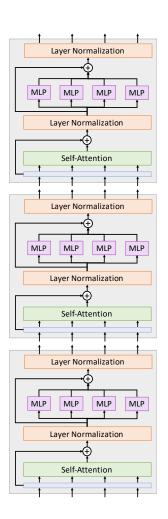
Input: Set of vectors x
Output: Set of vectors y

Self-attention is the only interaction between vectors!

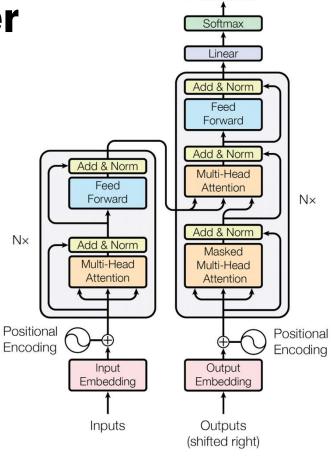
Layer norm and MLP work independently per vector

Highly scalable, highly parallelizable

A **Transformer** is a sequence of transformer blocks



Vaswani et al, "Attention is all you need", NeurIPS 2017



Output Probabilities

Encoder-Decoder

GLUE Benchmark

1	Rank	Name	Model	URL	Score	CoLA	SST-2	MRPC	STS-B	QQP	MNLI-m	MNLI-mm	QNLI	RTE	WNLI	AX
	1	HFL IFLYTEK	MacALBERT + DKM		90.7	74.8	97.0	94.5/92.6	92.8/92.6	74.7/90.6	91.3	91.1	97.8	92.0	94.5	52.6
+	2	Alibaba DAMO NLP	StructBERT + TAPT		90.6	75.3	97.3	93.9/91.9	93.2/92.7	74.8/91.0	90.9	90.7	97.4	91.2	94.5	49.1
+	3 PIN 4 ERI 5 T5	PING-AN Omni-Sinitic	ALBERT + DAAF + NAS		90.6	73.5	97.2	94.0/92.0	93.0/92.4	76.1/91.0	91.6	91.3	97.5	91.7	94.5	51.2
	4	ERNIE Team - Baidu	ERNIE	Z	90.4	74.4	97.5	93.5/91.4	93.0/92.6	75.2/90.9	91.4	91.0	96.6	90.9	94.5	51.7
	5	T5 Team - Google	Т5	♂	90.3	71.6	97.5	92.8/90.4	93.1/92.8	75.1/90.6	92.2	91.9	96.9	92.8	94.5	53.1
	6	Microsoft D365 AI & MSR AI & GATECH	MT-DNN-SMART	♂	89.9	69.5	97.5	93.7/91.6	92.9/92.5	73.9/90.2	91.0	90.8	99.2	89.7	94.5	50.2
+	7	Zihang Dai	Funnel-Transformer (Ensemble B10-10-10H1024)		89.7	70.5	97.5	93.4/91.2	92.6/92.3	75.4/90.7	91.4	91.1	95.8	90.0	94.5	51.6
+	8	ELECTRA Team	ELECTRA-Large + Standard Tricks	♂	89.4	71.7	97.1	93.1/90.7	92.9/92.5	75.6/90.8	91.3	90.8	95.8	89.8	91.8	50.7
+	9	Huawei Noah's Ark Lab	NEZHA-Large		89.1	69.9	97.3	93.3/91.0	92.4/91.9	74.2/90.6	91.0	90.7	95.7	88.7	93.2	47.9
+	10	Microsoft D365 AI & UMD	FreeLB-RoBERTa (ensemble)	♂	88.4	68.0	96.8	93.1/90.8	92.3/92.1	74.8/90.3	91.1	90.7	95.6	88.7	89.0	50.1
	11	Junjie Yang	HIRE-RoBERTa	Z	88.3	68.6	97.1	93.0/90.7	92.4/92.0	74.3/90.2	90.7	90.4	95.5	87.9	89.0	49.3
	12	Facebook Al	RoBERTa	♂	88.1	67.8	96.7	92.3/89.8	92.2/91.9	74.3/90.2	90.8	90.2	95.4	88.2	89.0	48.7
+	13	Microsoft D365 AI & MSR AI	MT-DNN-ensemble	♂	87.6	68.4	96.5	92.7/90.3	91.1/90.7	73.7/89.9	87.9	87.4	96.0	86.3	89.0	42.8
	14	GLUE Human Baselines	GLUE Human Baselines	♂	87.1	66.4	97.8	86.3/80.8	92.7/92.6	59.5/80.4	92.0	92.8	91.2	93.6	95.9	-
	15	Stanford Hazy Research	Snorkel MeTaL	Z	83.2	63.8	96.2	91.5/88.5	90.1/89.7	73.1/89.9	87.6	87.2	93.9	80.9	65.1	39.9

source: https://gluebenchmark.com/leaderboard

GLUE Benchmark

li	Rank	Name	Model	URL	Score	CoLA	SST-2	MRPC	STS-B	QQP	MNLI-m MN	ILI-mm	QNLI	RTE	WNLI	AX
	1	HFL IFLYTEK	MacALBERT + DKM		90.7	74.8	97.0	94.5/92.6	92.8/92.6	74.7/90.6	91.3	91.1	97.8	92.0	94.5	52.6
+	2	Alibaba DAMO NLP	StructBERT + TAPT		90.6	75.3	97.3	93.9/91.9	93.2/92.7	74.8/91.0	90.9	90.7	97.4	91.2	94.5	49.1
+	3	PING-AN Omni-Sinitic	ALBERT + DAAF + NAS		90.6	73.5	97.2	94.0/92.0	93.0/92.4	76.1/91.0	91.6	91.3	97.5	91.7	94.5	51.2
	4	ERNIE Team - Baidu	ERNIE	♂	90.4	74.4	97.5	93.5/91.4	93.0/92.6	75.2/90.9	91.4	91.0	96.6	90.9	94.5	51.7
	5	T5 Team - Google	Т5	♂	90.3	71.6	97.5	92.8/90.4	93.1/92.8	75.1/90.6	92.2	91.9	96.9	92.8	94.5	53.1
	6	Microsoft D365 AI & MSR AI & GATECH	MT-DNN-SMART	♂	89.9	69.5	97.5	93.7/91.6	92.9/92.5	73.9/90.2	91.0	90.8	99.2	89.7	94.5	50.2
+	7	Zihang Dai	Funnel-Transformer (Ensemble B10-10-10H1024)	♂	89.7	70.5	97.5	93.4/91.2	92.6/92.3	75.4/90.7	91.4	91.1	95.8	90.0	94.5	51.6
+	8	ELECTRA Team	ELECTRA-Large + Standard Tricks	♂	89.4	71.7	97.1	93.1/90.7	92.9/92.5	75.6/90.8	91.3	90.8	95.8	89.8	91.8	50.7
+	9	Huawei Noah's Ark Lab	NEZHA-Large		89.1	69.9	97.3	93.3/91.0	92.4/91.9	74.2/90.6	91.0	90.7	95.7	88.7	93.2	47.9
+	10	Microsoft D365 AI & UMD	FreeLB-RoBERTa (ensemble)	♂	88.4	68.0	96.8	93.1/90.8	92.3/92.1	74.8/90.3	91.1	90.7	95.6	88.7	89.0	50.1
	11	Junjie Yang	HIRE-RoBERTa	Z	88.3	68.6	97.1	93.0/90.7	92.4/92.0	74.3/90.2	90.7	90.4	95.5	87.9	89.0	49.3
	12	Facebook Al	RoBERTa	Z	88.1	67.8	96.7	92.3/89.8	92.2/91.9	74.3/90.2	90.8	90.2	95.4	88.2	89.0	48.7
+	13	Microsoft D365 AI & MSR AI	MT-DNN-ensemble	♂	87.6	68.4	96.5	92.7/90.3	91.1/90.7	73.7/89.9	87.9	87.4	96.0	86.3	89.0	42.8
	14	GLUE Human Baselines	GLUE Human Baselines	♂	87.1	66.4	97.8	86.3/80.8	92.7/92.6	59.5/80.4	92.0	92.8	91.2	93.6	95.9	-
	15	Stanford Hazy Research	Snorkel MeTaL	<u>C</u>	83.2	63.8	96.2	91.5/88.5	90.1/89.7	73.1/89.9	87.6	87.2	93.9	80.9	65.1	39.9

source: https://gluebenchmark.com/leaderboard

SYSTEM PROMPT (HUMAN-WRITTEN)

In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

MODEL COMPLETION (MACHINE-WRITTEN, 10 TRIES)

The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.

Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow.

Pérez and the others then ventured further into the valley. "By the time we reached the top of one peak, the water looked blue, with some crystals on top," said Pérez.

Source: OpenAI, "Better Language Models and Their Implications" https://openai.com/blog/better-language-models/

Can Attention/Transformers be used from more than text processing?

ViLBERT: A Visolinguistic Transformer







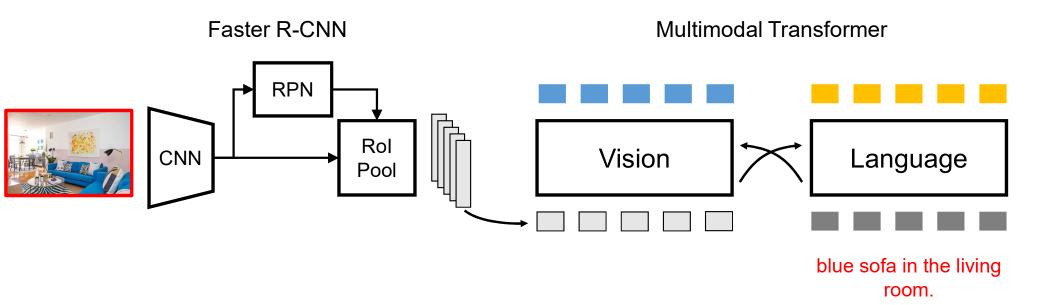
pop artist performs at the festival in a city.

a worker helps to clear the debris.

blue sofa in the living room.

Image and captions from: Sharma, Piyush, et al. "Conceptual captions: A cleaned, hypernymed, image alt-text dataset for automatic image captioning." ACL. 2018.

ViLBERT: A Visolinguistic Transformer



Lu et al "Vilbert: Pretraining task-agnostic visiolinguistic representations for vision-and-language tasks." *NeurIPS*. 2019. Ren et al. "Faster r-cnn: Towards real-time object detection with region proposal networks." *NeurIPS*. 2015.

ViLBERT Demo:

https://demo.allennlp.org/visual-question-answering

Summary

Self-Attention

Transformer Model

VILBERT

