# CS 4644-DL / 7643-A: LECTURE 16 DANFEI XU

Recurrent Neural Networks (RNN)

Long Short-Term Memory (LSTM)

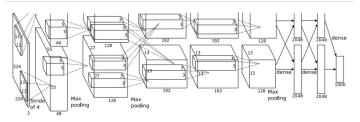
#### **Administrative:**

- Assignment 2 grace period ends today!
- Milestone guideline is out

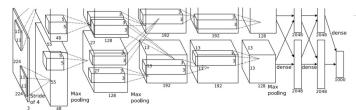
# Which pixels matter: Saliency via Occlusion

Mask part of the image before feeding to CNN, check how much predicted probabilities change

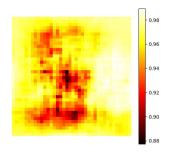






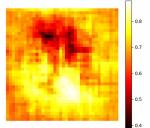




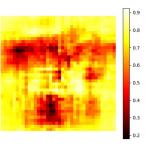


African elephant, Loxodonta africana





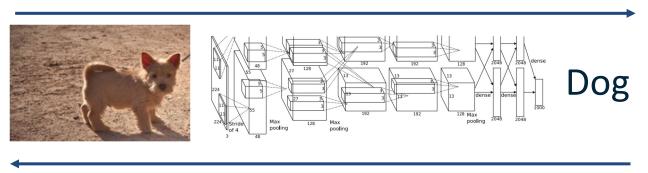




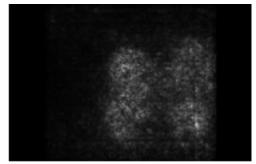
Boat image is CC0 public domain Elephant image is CC0 public domain Go-Karts image is CC0 public domain

# Which pixels matter: Saliency via Backprop

Forward pass: Compute probabilities

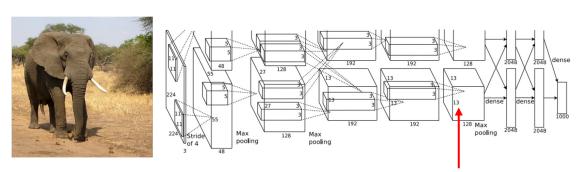


Compute gradient of (unnormalized) class score with respect to image pixels, take absolute value and max/sum over RGB channels



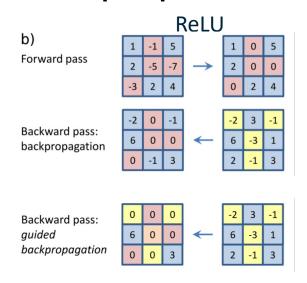
Simonyan, Vedaldi, and Zisserman, "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", ICLR Workshop 2014.

# Intermediate Features via (guided) backprop



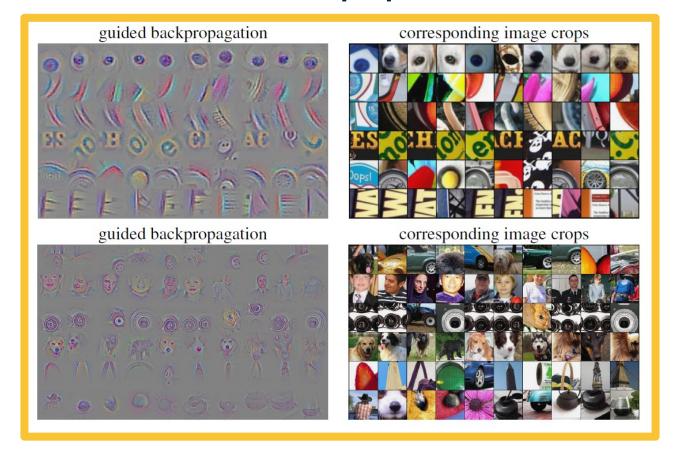
Pick a single intermediate neuron, e.g. one value in 128 x 13 x 13 conv5 feature map

Compute gradient of activation value with respect to image pixels



**Guided backprop**: suppress pathways that have negative gradients --- only backprop positive gradients through each ReLU

#### **Guided Backprop Results**



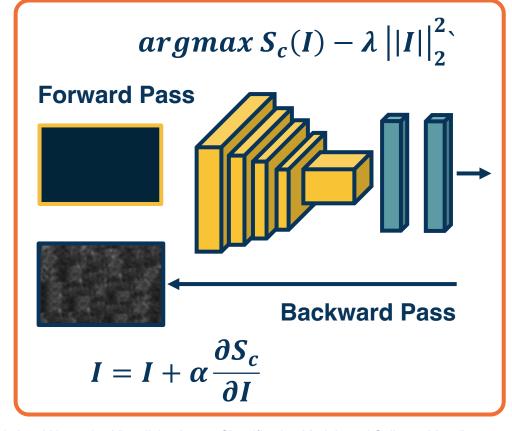
From: Springenberg et al., "Striving For Simplicity: The All Convolutional Net"

We can perform **gradient ascent** on image for image generation

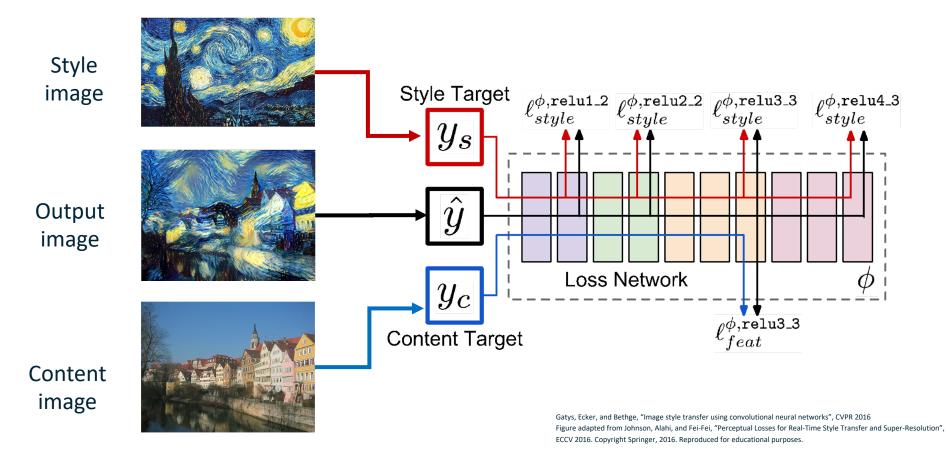
- Start from random/zero image
- Use scores to avoid minimizing other class scores instead

Often need **regularization term** to induce statistics of natural imagery

E.g. small pixel values, spatial smoothness



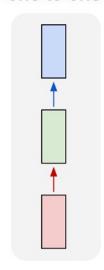
From: Simonyan et al., "Deep Inside Convolutional Networks: Visualising Image Classification Models and Saliency Maps", 2013



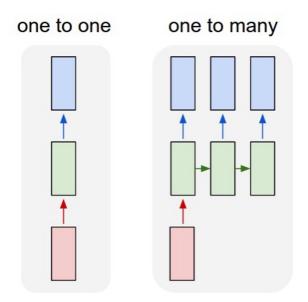
Today: Recurrent Neural Networks

#### "Vanilla" Neural Network

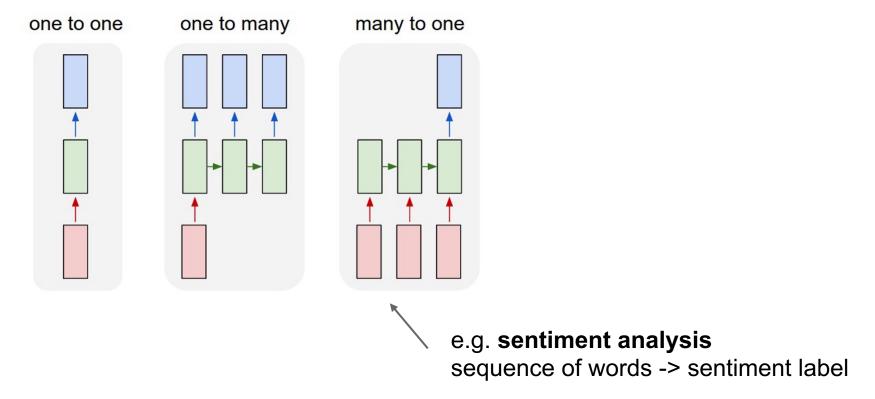
one to one

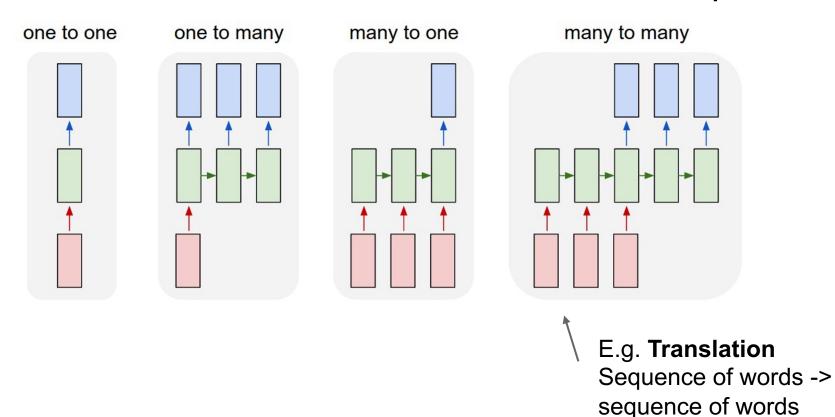


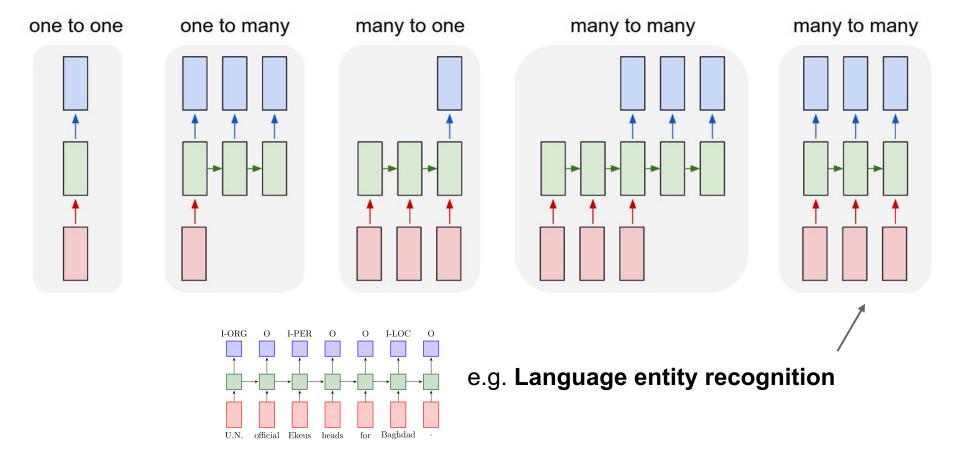
Vanilla Neural Networks



e.g. **Image Captioning** image -> sequence of words







# Why are existing convnets insufficient?

Variable sequence length inputs and outputs!

Example task: video captioning

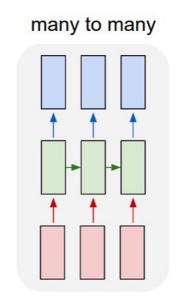
**Input** video can have variable number of frames

Output captions can be variable length.

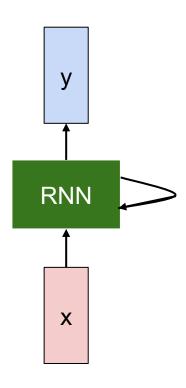


Output Captions
.....
A lady joins the man and sings along to the music.

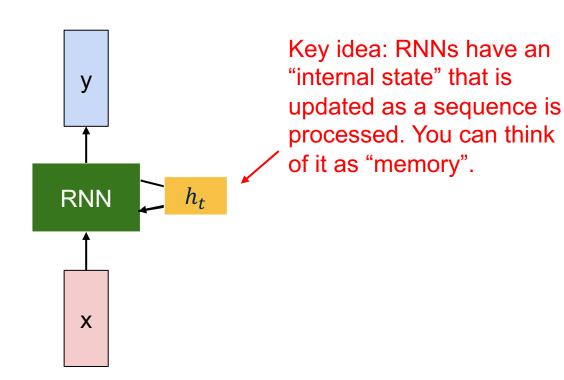
Let's start with a task that takes a variable input and produces an output at every step



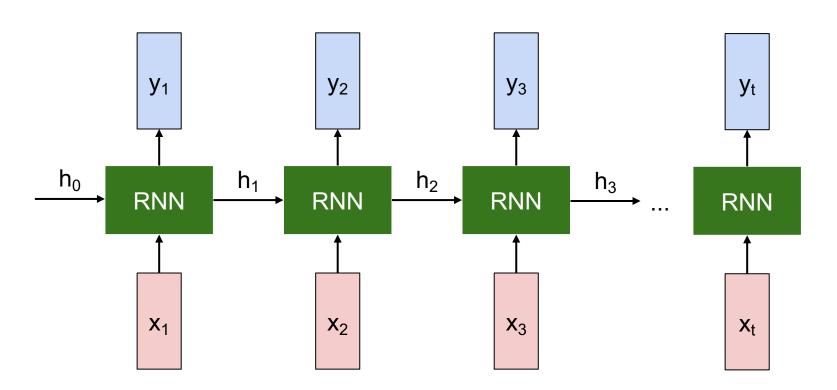
# Recurrent Neural Network



### Recurrent Neural Network



# **Unrolled RNN**

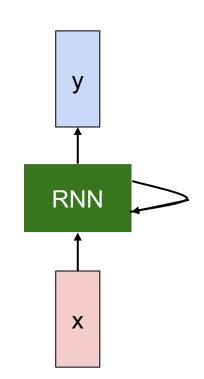


# RNN hidden state update

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$h_t = f_W(h_{t-1},x_t)$$
new state old state input vector at (vector) (vector) some time step some function with parameters W

Can set initial state  $h_0$  to all 0's



# RNN output generation

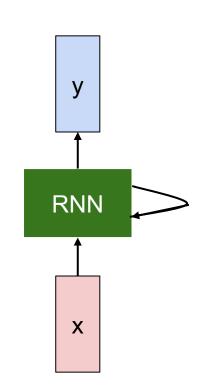
We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$y_{t} = f_{W_{hy}}(h_{t})$$
output

another function

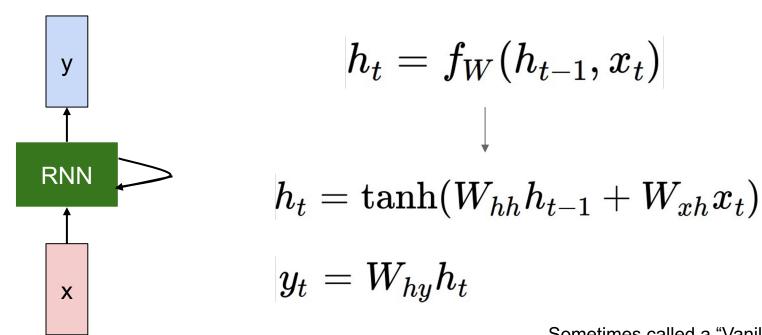
with parameters  $W_{0}$ 

Can set initial state  $h_0$  to all 0's

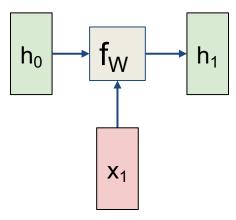


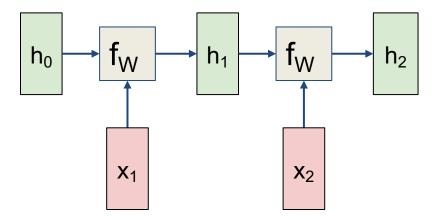
# (Simple) Recurrent Neural Network

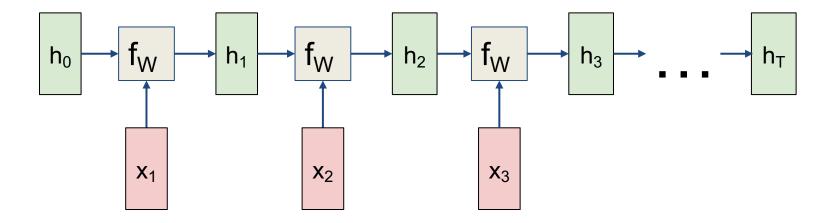
The state consists of a single "hidden" vector **h**:



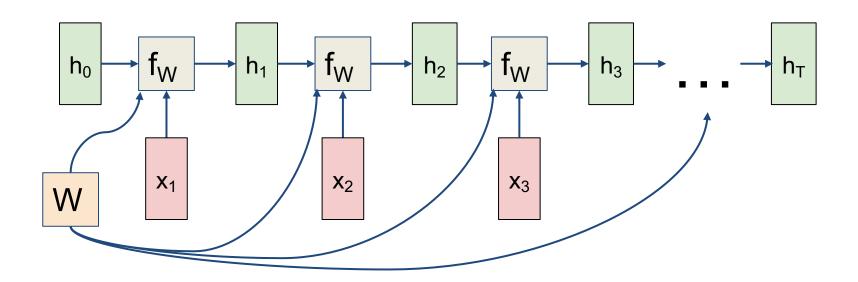
Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman



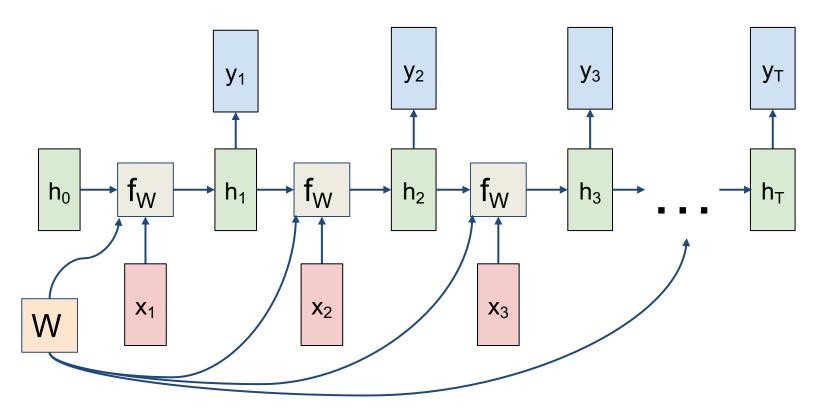




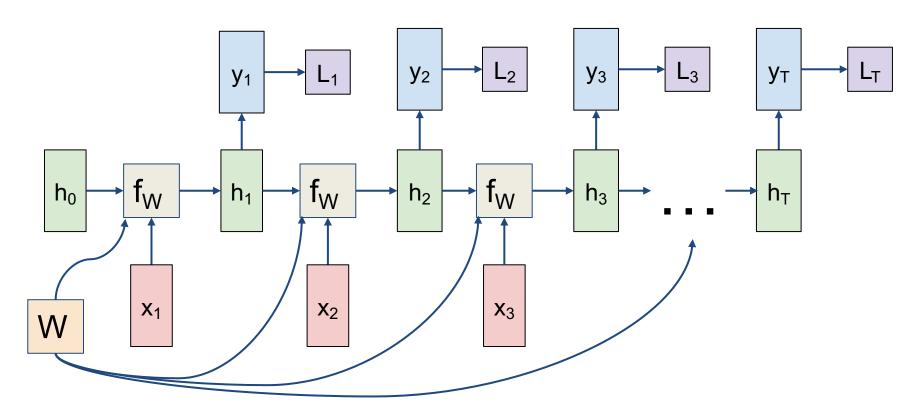
Re-use the same weight matrix at every time-step

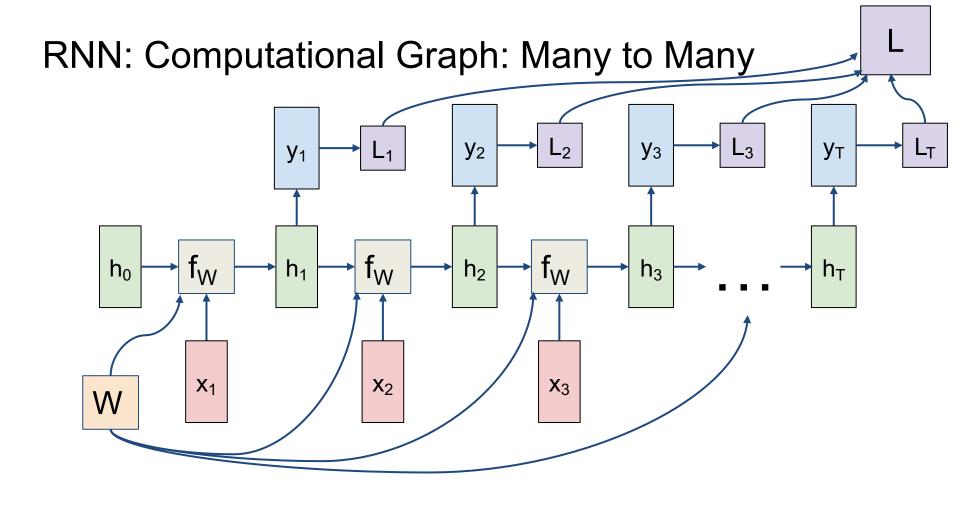


# RNN: Computational Graph: Many to Many

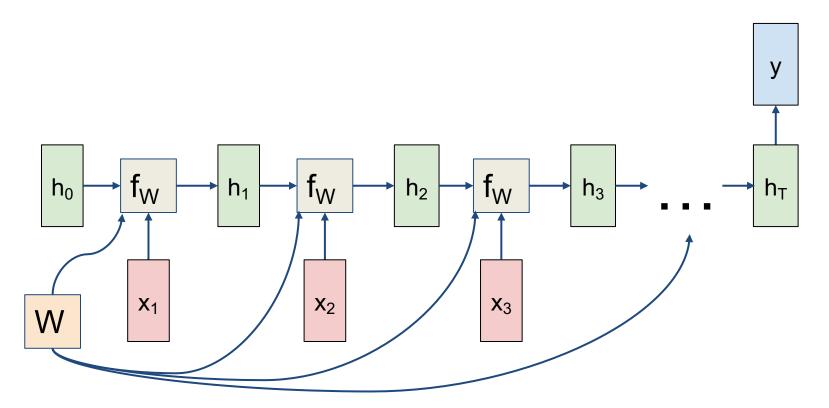


# RNN: Computational Graph: Many to Many

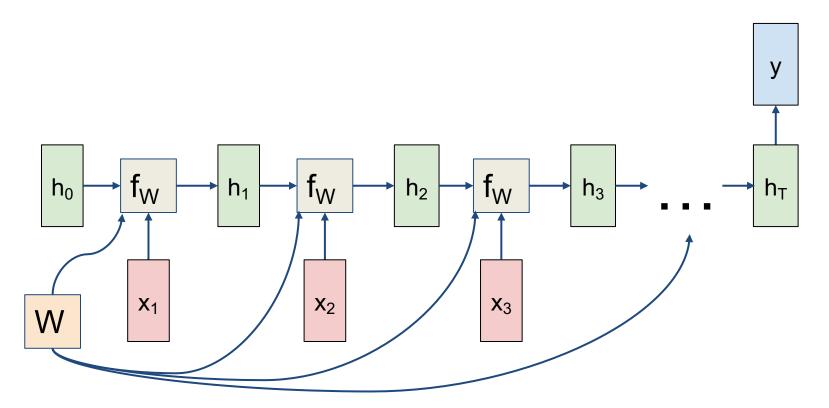




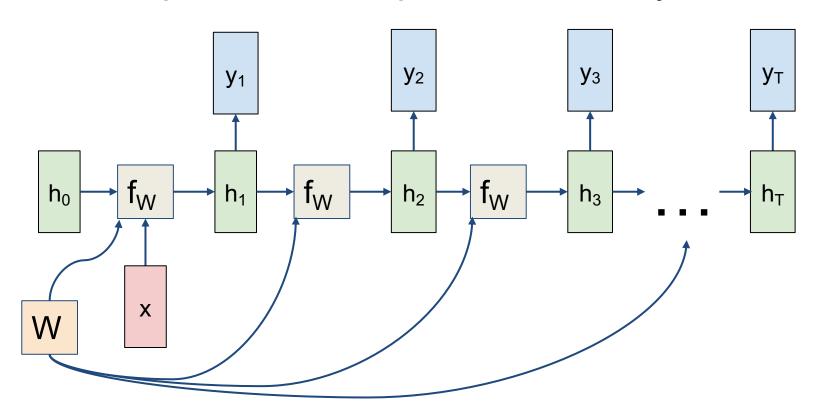
# RNN: Computational Graph: Many to One



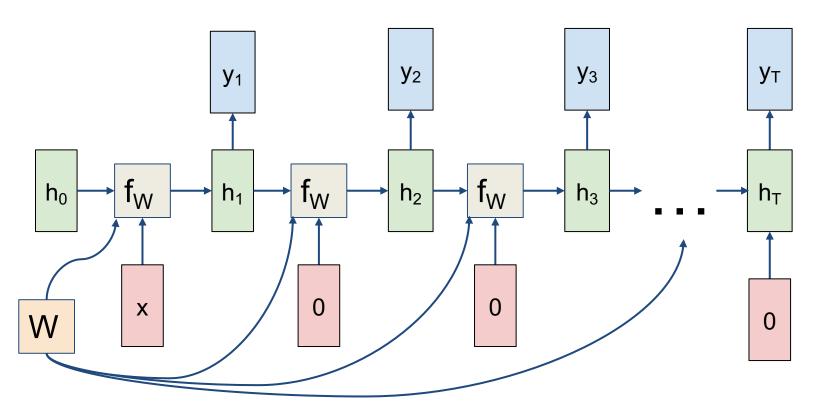
# RNN: Computational Graph: Many to One



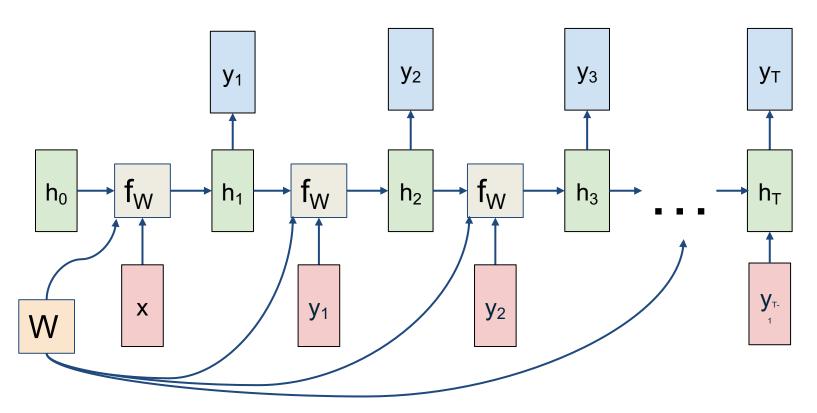
# RNN: Computational Graph: One to Many



# RNN: Computational Graph: One to Many

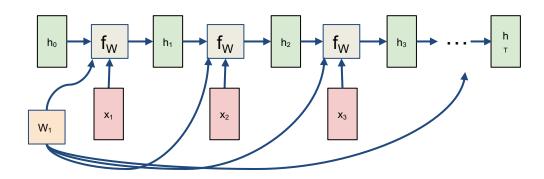


# RNN: Computational Graph: One to Many



# Sequence to Sequence: Many-to-one + one-tomany

Many to one: Encode input sequence in a single vector



# Sequence to Sequence: Many-to-one + one-tomany

sequence from single input vector Many to one: Encode input sequence in a single vector **y**<sub>1</sub> **y**<sub>2</sub>  $f_W$  $h_1$  $\mathbf{X}_2$  $W_2$ 

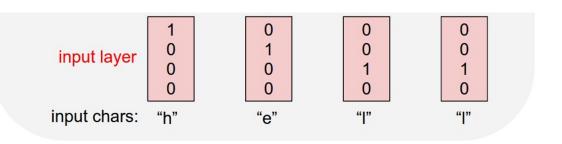
One to many: Produce output

## **Example: Character-level** Language Model

Vocabulary: [h,e,l,o]

Example training sequence:

"hello"

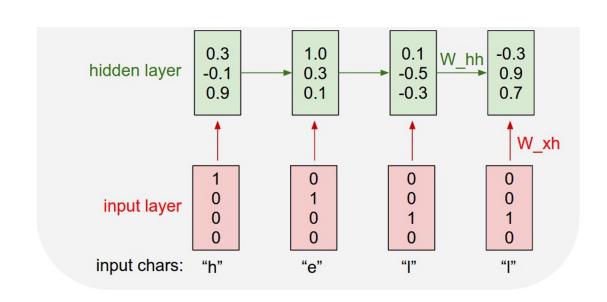


# Example: Character-level Language Model

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$

Vocabulary: [h,e,l,o]

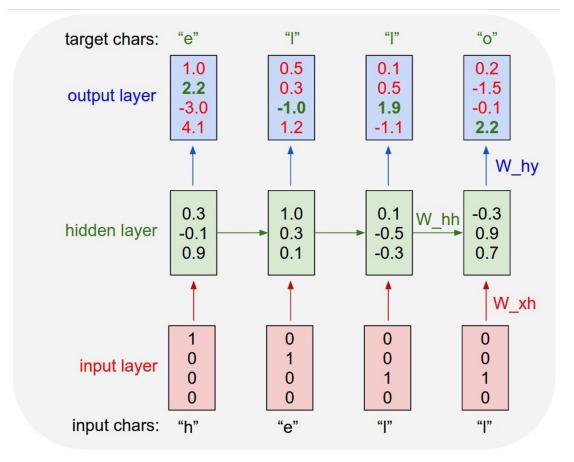
Example training sequence: "hello"



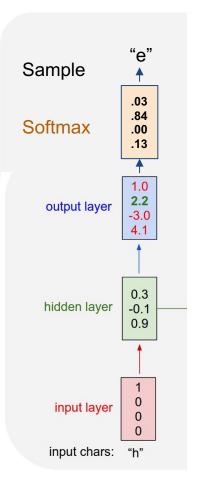
## Example: Character-level Language Model

Vocabulary: [h,e,l,o]

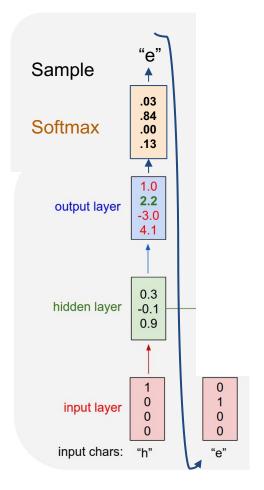
Example training sequence: "hello"



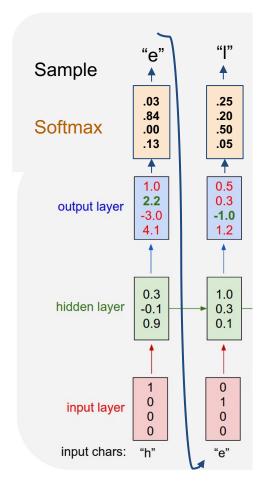
Vocabulary: [h,e,l,o]



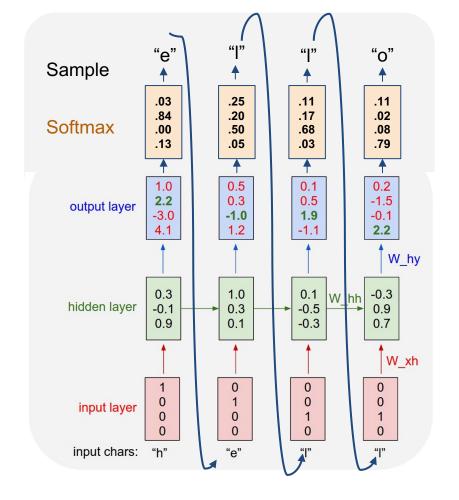
Vocabulary: [h,e,l,o]

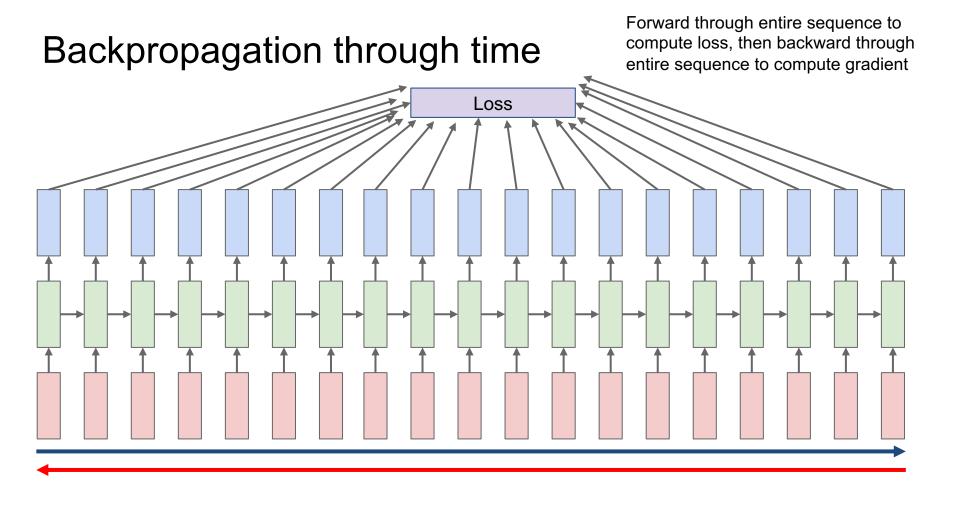


Vocabulary: [h,e,l,o]

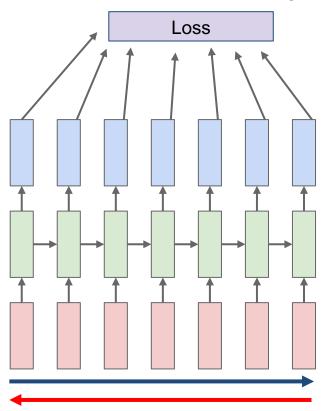


Vocabulary: [h,e,l,o]



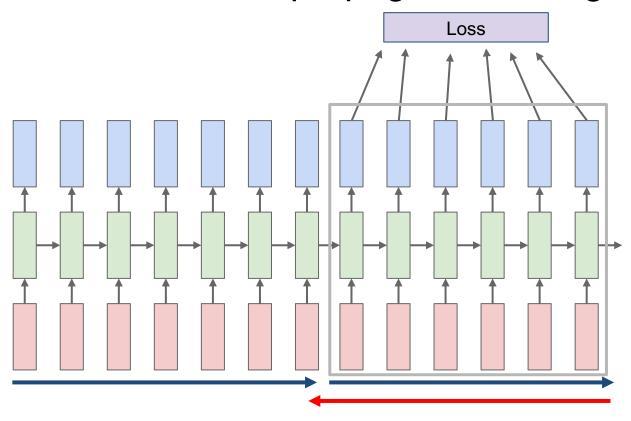


# Truncated Backpropagation through time



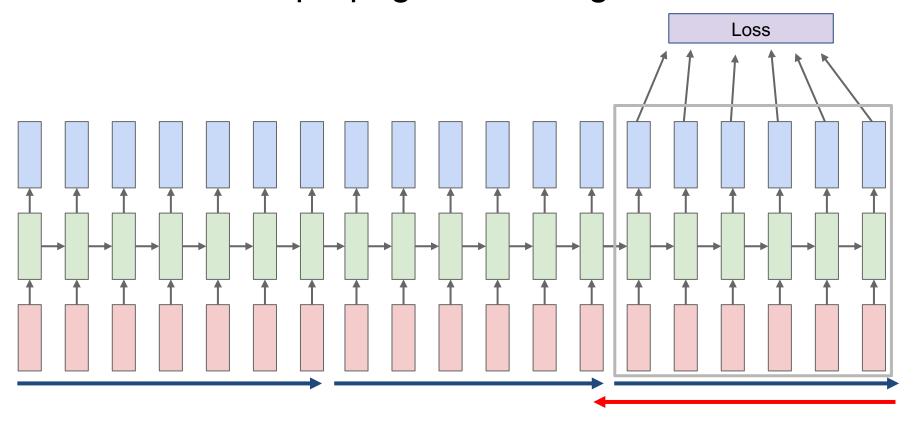
Run forward and backward through chunks (length k) of the sequence instead of whole sequence, do parameter update, clear gradient cache

## Truncated Backpropagation through time

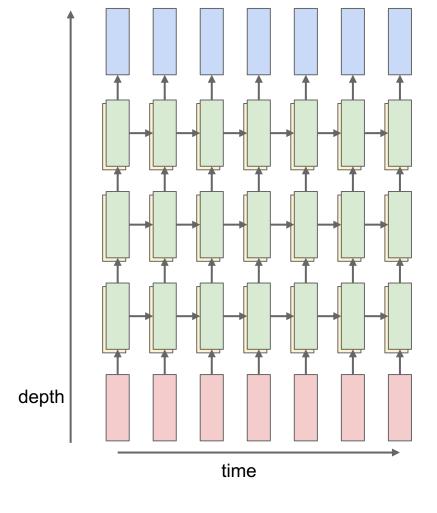


Carry hidden states forward in time for k steps, backprop, update parameter, clear gradient ...

# Truncated Backpropagation through time



# Multilayer RNNs



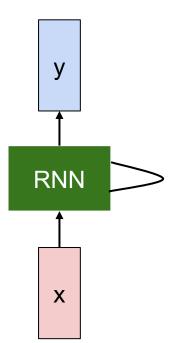
## THE SONNETS

## by William Shakespeare

From fairest creatures we desire increase,
That thereby beauty's rose might never die,
But as the riper should by time decease,
His tender heir might bear his memory:
But thou, contracted to thine own bright eyes,
Feed'st thy light's flame with self-substantial fuel,
Making a famine where abundance lies,
Thyself thy foe, to thy sweet self too cruel:
Thou that art now the world's fresh ornament,
And only herald to the gaudy spring,
Within thine own bud buriest thy content,
And tender churl mak'st waste in niggarding:
Pity the world, or else this glutton be,
To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies, Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer This fair child of mine Shall sum my count, and make my old excuse,' Proving his beauty by succession thine!

This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.



at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

### train more

"Tmont thithey" fomesscerliund
Keushey. Thom here
sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome
coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

## train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

## train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him.

Pierre aking his soul came to the packs and drove up his father-in-law women.

## PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death,

#### Second Senator:

I should not sleep.

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish

#### DUKE VINCENTIO:

Well, your wit is in the care of side and that.

The earth and thoughts of many states.

#### Second Lord:

They would be ruled after this chamber, and my fair nues begun out of the fact, to be conveyed, Whose noble souls I'll have the heart of the wars.

#### Clown:

Come, sir, I will make did behold your worship.

#### VIOLA:

I'll drink it.

VIOLA:

Why, Salisbury must find his flesh and thought
That which I am not aps, not a man and in fire,
To show the reining of the raven and the wars

We spare with hours, but cut thy council I am great,

To grace my hand reproach within, and not a fair are hand, That Caesar and my goodly father's world; When I was heaven of presence and our fleets,

Murdered and by thy master's ready there My power to give thee but so much as hell:

Some service in the noble bondman here,

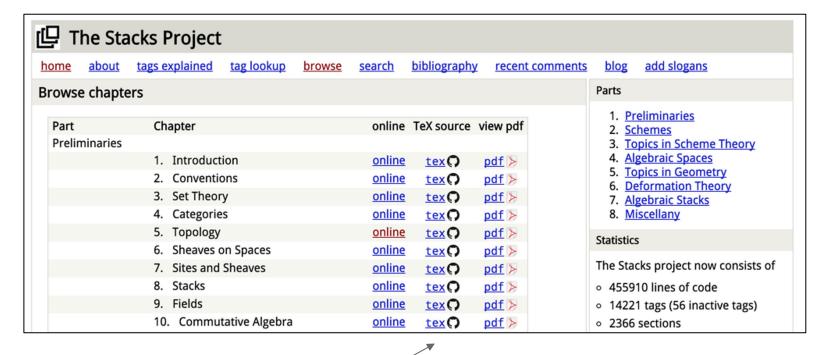
Would show him to her wine.

Shall be against your honour.

#### KING LEAR:

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds, So drop upon your lordship's head, and your opinion

## The Stacks Project: open source algebraic geometry textbook





http://stacks.math.columbia.edu/

The stacks project is licensed under the GNU Free Documentation License

For  $\bigoplus_{n=1,...,m}$  where  $\mathcal{L}_{m_{\bullet}} = 0$ , hence we can find a closed subset  $\mathcal{H}$  in  $\mathcal{H}$  and any sets  $\mathcal{F}$  on X, U is a closed immersion of S, then  $U \to T$  is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \operatorname{Spec}(R) = U \times_X U \times_X U$$

and the comparison in the fibre product covering we have to prove the lemma generated by  $\coprod Z \times_U U \to V$ . Consider the maps M along the set of points  $Sch_{fppf}$  and  $U \to U$  is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset  $W \subset U$  in Sh(G) such that  $Spec(R') \to S$  is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that  $f_i$  is of finite presentation over S. We claim that  $\mathcal{O}_{X,x}$  is a scheme where  $x,x',s''\in S'$  such that  $\mathcal{O}_{X,x'}\to \mathcal{O}'_{X',x'}$  is separated. By Algebra, Lemma ?? we can define a map of complexes  $\mathrm{GL}_{S'}(x'/S'')$ 

To prove study we see that  $\mathcal{F}|_U$  is a covering of  $\mathcal{X}'$ , and  $\mathcal{T}_i$  is an object of  $\mathcal{F}_{X/S}$  for i>0 and  $\mathcal{F}_p$  exists and let  $\mathcal{F}_i$  be a presheaf of  $\mathcal{O}_X$ -modules on  $\mathcal{C}$  as a  $\mathcal{F}$ -module. In particular  $\mathcal{F}=U/\mathcal{F}$  we have to show that

$$\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\operatorname{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$$

is a unique morphism of algebraic stacks. Note that

Arrows = 
$$(Sch/S)_{fppf}^{opp}$$
,  $(Sch/S)_{fppf}$ 

and

and we win.

$$V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by  $X_{spaces, \acute{e}tale}$  which gives an open subspace of X and T equal to  $S_{Zar}$ , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

**Lemma 0.1.** Assume (3) and (3) by the construction in the description.

Suppose  $X = \lim |X|$  (by the formal open covering X and a single map  $\underline{Proj}_X(A) = \operatorname{Spec}(B)$  over U compatible with the complex

$$Set(A) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$$

When in this case of to show that  $\mathcal{Q} \to \mathcal{C}_{Z/X}$  is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace  $Z \subset X$  of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1) 
$$f$$
 is locally of finite type. Since  $S = \operatorname{Spec}(R)$  and  $Y = \operatorname{Spec}(R)$ .

*Proof.* This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism  $U \to X$ . Let  $U \cap U = \coprod_{i=1,\dots,n} U_i$  be the scheme X over S at the schemes  $X_i \to X$  and  $U = \lim_i X_i$ .

The following lemma surjective restrocomposes of this implies that  $\mathcal{F}_{x_0}=\mathcal{F}_{x_0}=\mathcal{F}_{x,\dots,0}$ .

**Lemma 0.2.** Let X be a locally Noetherian scheme over S,  $E = \mathcal{F}_{X/S}$ . Set  $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$ . Since  $\mathcal{I}^n \subset \mathcal{I}^n$  are nonzero over  $i_0 \leq \mathfrak{p}$  is a subset of  $\mathcal{J}_{n,0} \circ \overline{A}_2$  works.

**Lemma 0.3.** In Situation ??. Hence we may assume q' = 0.

*Proof.* We will use the property we see that  $\mathfrak p$  is the mext functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where K is an F-algebra where  $\delta_{n+1}$  is a scheme over S.

Proof. Omitted.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

.

*Proof.* This is an algebraic space with the composition of sheaves  $\mathcal{F}$  on  $X_{\acute{e}tale}$  we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where G defines an isomorphism  $F \to F$  of O-modules.

Lemma 0.2. This is an integer Z is injective.

Proof. See Spaces, Lemma ??.

**Lemma 0.3.** Let S be a scheme. Let X be a scheme and X is an affine open covering. Let  $\mathcal{U} \subset \mathcal{X}$  be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

$$b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X.$$

be a morphism of algebraic spaces over S and Y.

*Proof.* Let X be a nonzero scheme of X. Let X be an algebraic space. Let  $\mathcal{F}$  be a quasi-coherent sheaf of  $\mathcal{O}_X$ -modules. The following are equivalent

- F is an algebraic space over S.
- (2) If X is an affine open covering.

Consider a common structure on X and X the functor  $\mathcal{O}_X(U)$  which is locally of finite type.

This since  $\mathcal{F} \in \mathcal{F}$  and  $x \in \mathcal{G}$  the diagram  $\begin{array}{c}
\mathcal{S} \\
\downarrow \\
\xi \\
\longrightarrow \mathcal{O}_{X'}
\end{array}$   $\begin{array}{c}
\alpha' \\
= \alpha' \\
\longrightarrow \alpha
\end{array}$   $\begin{array}{c}
X \\
\downarrow \\
\operatorname{Spec}(K_{\psi})
\end{array}$   $\begin{array}{c}
X \\
\downarrow \\
\operatorname{Mor}_{Sets}
\end{array}$   $\begin{array}{c}
\mathcal{A} \\
\downarrow \\
\operatorname{Mor}_{Sets}
\end{array}$ 

is a limit. Then  $\mathcal G$  is a finite type and assume S is a flat and  $\mathcal F$  and  $\mathcal G$  is a finite type  $f_*$ . This is of finite type diagrams, and

- the composition of G is a regular sequence,
- Ox' is a sheaf of rings.

*Proof.* We have see that  $X = \operatorname{Spec}(R)$  and  $\mathcal{F}$  is a finite type representable by algebraic space. The property  $\mathcal{F}$  is a finite morphism of algebraic stacks. Then the cohomology of X is an open neighbourhood of U.

*Proof.* This is clear that G is a finite presentation, see Lemmas ??.

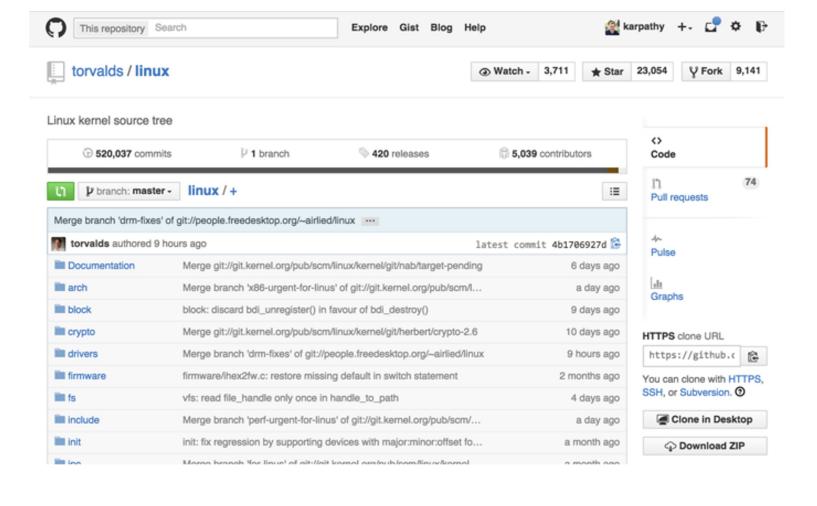
A reduced above we conclude that U is an open covering of  $\mathcal C.$  The functor  $\mathcal F$  is a "field

$$\mathcal{O}_{X,x} \longrightarrow \mathcal{F}_{\overline{x}} -1(\mathcal{O}_{X_{\delta tale}}) \longrightarrow \mathcal{O}_{X_s}^{-1}\mathcal{O}_{X_{\lambda}}(\mathcal{O}_{X_n}^{\overline{v}})$$

is an isomorphism of covering of  $\mathcal{O}_{X_i}$ . If  $\mathcal{F}$  is the unique element of  $\mathcal{F}$  such that X is an isomorphism.

is an isomorphism. The property  $\mathcal{F}$  is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme  $\mathcal{O}_X$ -algebra with  $\mathcal{F}$  are opens of finite type over S. If  $\mathcal{F}$  is a scheme theoretic image points.

If  $\mathcal{F}$  is a finite direct sum  $\mathcal{O}_{X_{\lambda}}$  is a closed immersion, see Lemma ??. This is a sequence of  $\mathcal{F}$  is a similar morphism.



```
static void do command(struct seg file *m, void *v)
 int column = 32 << (cmd[2] & 0x80);
 if (state)
    cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
 else
    seq = 1;
 for (i = 0; i < 16; i++) {
   if (k & (1 << 1))
      pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000fffffff8) & 0x000000f) << 8;
    if (count == 0)
      sub(pid, ppc_md.kexec_handle, 0x20000000);
    pipe set bytes(i, 0);
  /* Free our user pages pointer to place camera if all dash */
  subsystem info = &of changes[PAGE SIZE];
 rek controls(offset, idx, &soffset);
  /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
 for (i = 0; i < COUNTER; i++)
    seq puts(s, "policy ");
```

# Generated C code

```
Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
   This program is free software; you can redistribute it and/or modify it
* under the terms of the GNU General Public License version 2 as published by
* the Free Software Foundation.
         This program is distributed in the hope that it will be useful,
* but WITHOUT ANY WARRANTY; without even the implied warranty of
    MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the
   GNU General Public License for more details.
    You should have received a copy of the GNU General Public License
     along with this program; if not, write to the Free Software Foundation,
* Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
*/
#include ux/kexec.h>
#include ux/errno.h>
#include ux/io.h>
#include ux/platform device.h>
#include ux/multi.h>
#include ux/ckevent.h>
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
```

14

#include <asm/setew.h>
#include <asm/pgproto.h>

```
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG_PG vesa slot addr pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type) (func)
#define SWAP_ALLOCATE(nr)
                           (e)
#define emulate sigs() arch get unaligned child()
#define access rw(TST) asm volatile("movd %%esp, %0, %3" : : "r" (0)); \
 if ( type & DO READ)
static void stat PC SEC    read mostly offsetof(struct seq argsqueue, \
         pC>[1]);
static void
os prefix(unsigned long sys)
#ifdef CONFIG PREEMPT
 PUT_PARAM_RAID(2, sel) = get_state_state();
 set_pid_sum((unsigned long)state, current_state_str(),
          (unsigned long)-1->lr_full; low;
```

#include <asm/io.h>
#include <asm/prom.h>

# OpenAl GPT-2 generated text

**Input:** In a shocking finding, scientist discovered a herd of unicorns living in a remote, previously unexplored valley, in the Andes Mountains. Even more surprising to the researchers was the fact that the unicorns spoke perfect English.

**Output:** The scientist named the population, after their distinctive horn, Ovid's Unicorn. These four-horned, silver-white unicorns were previously unknown to science.

Now, after almost two centuries, the mystery of what sparked this odd phenomenon is finally solved.

Dr. Jorge Pérez, an evolutionary biologist from the University of La Paz, and several companions, were exploring the Andes Mountains when they found a small valley, with no other animals or humans. Pérez noticed that the valley had what appeared to be a natural fountain, surrounded by two peaks of rock and silver snow.

# Image Captioning

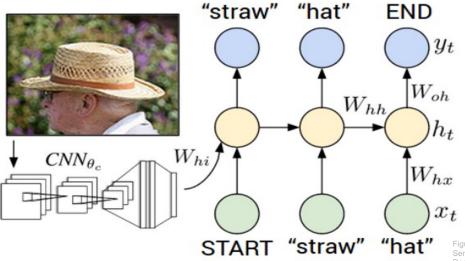


Figure from Karpathy et a, "Deep Visual-Semantic Alignments for Generating Image Descriptions", CVPR 2015; figure copyrigh IEEE, 2015.

Reproduced for educational purposes.

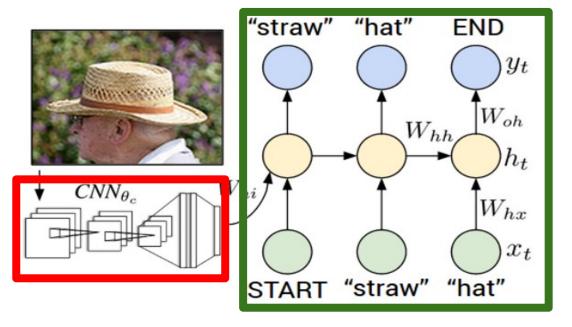
Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei
Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

## **Recurrent Neural Network**



**Convolutional Neural Network** 



test image

This image is CC0 public domain

image conv-64 conv-64 maxpool conv-128 conv-128 maxpool conv-256 conv-256 maxpool conv-512 conv-512 maxpool conv-512 conv-512 maxpool FC-4096 FC-4096 FC-1000

softmax



test image

image conv-64 conv-64 maxpool conv-128 conv-128 maxpool conv-256 conv-256 maxpool conv-512 conv-512 maxpool conv-512 conv-512 maxpool FC-4096 FC-4096 FC-1000 sof nax



test image

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool



test image

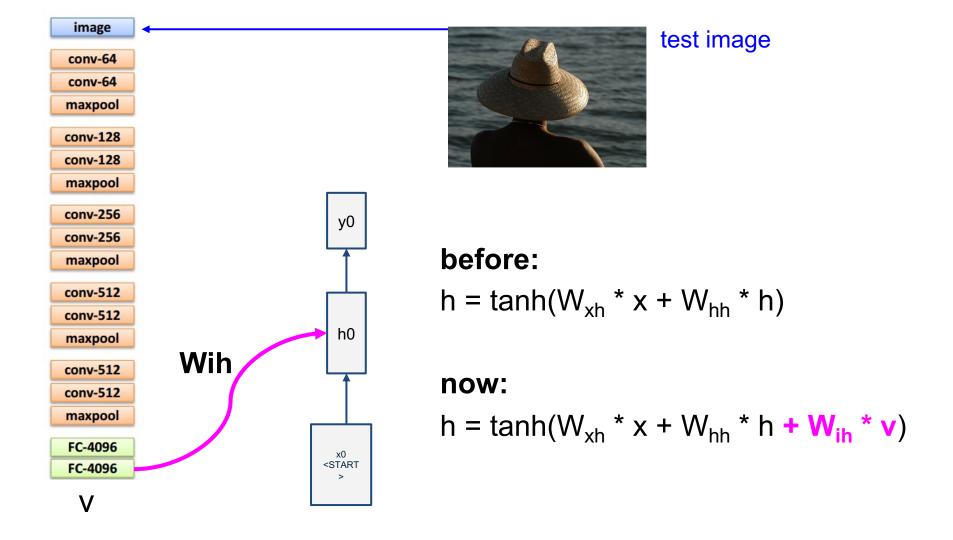
conv-256
conv-256
maxpool
conv-512
conv-512
maxpool

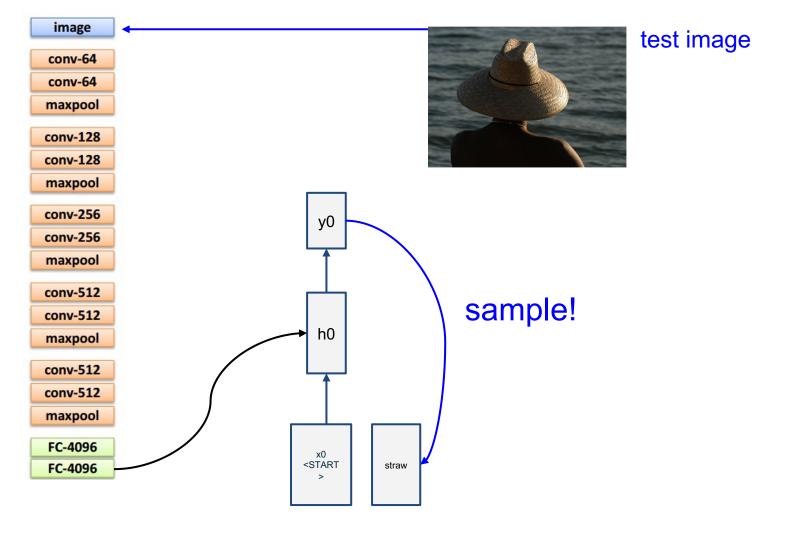
conv-512 conv-512 maxpool

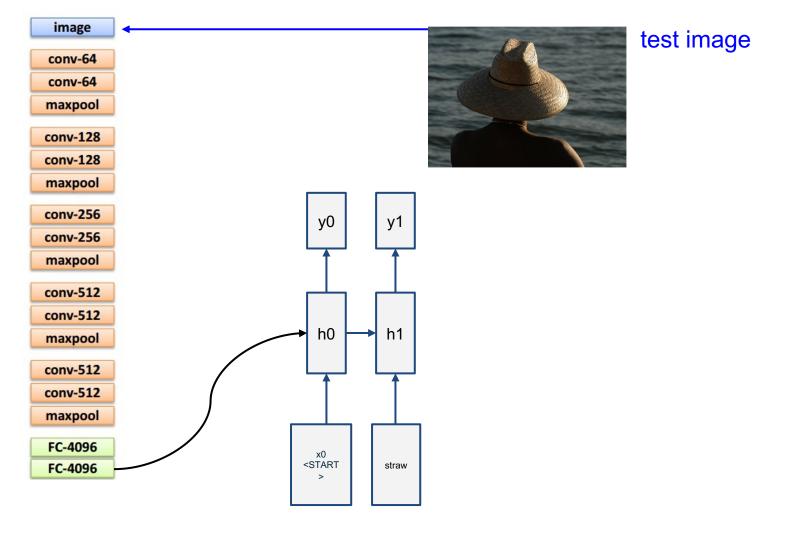
FC-4096

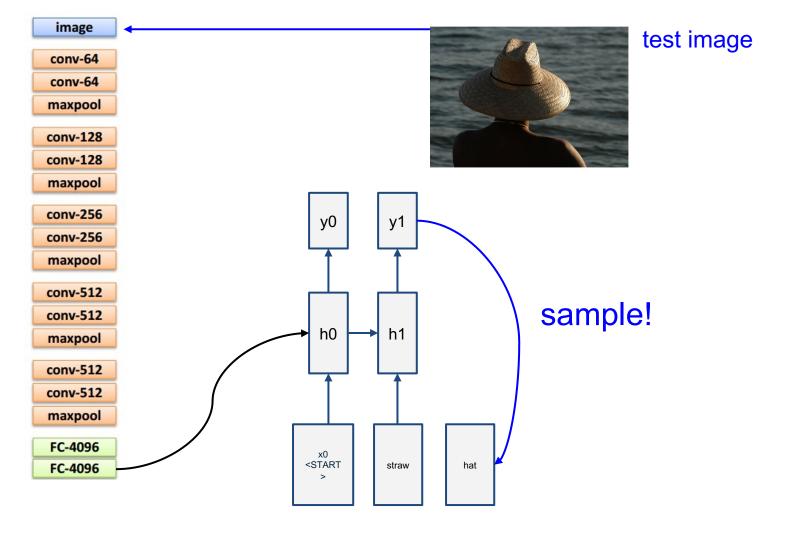
FC-4096

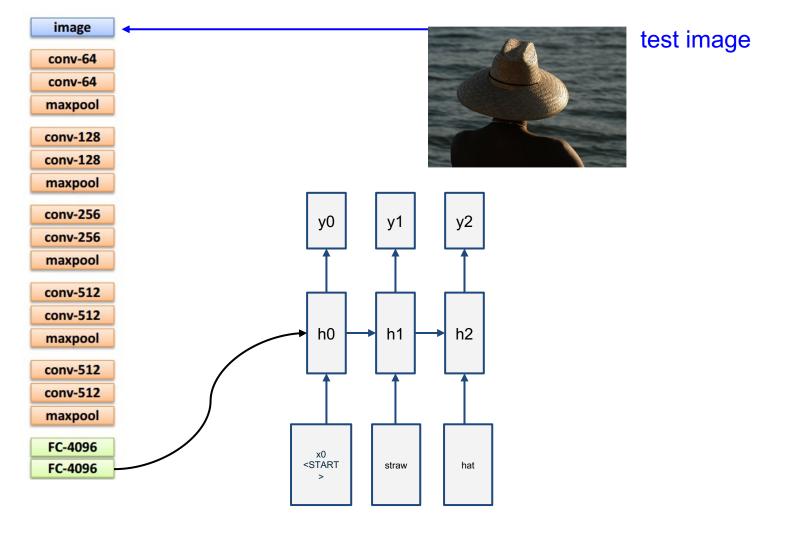
x0 <START >

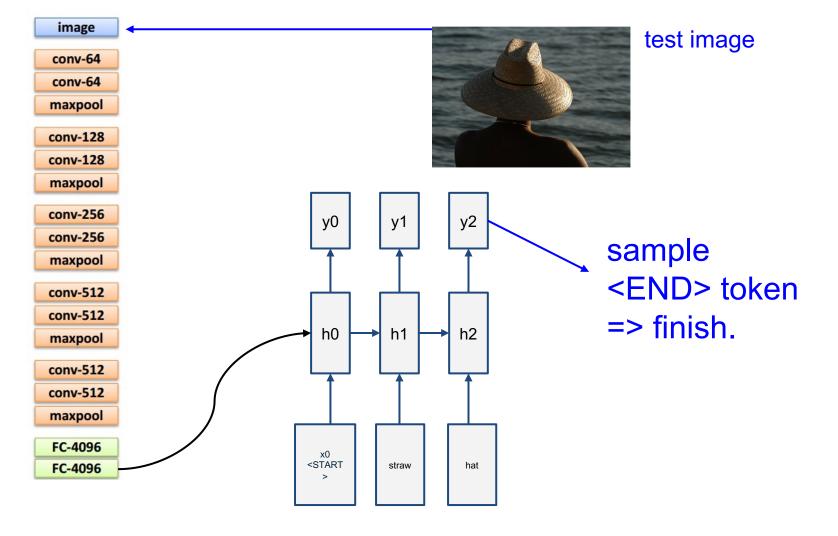












# Image Captioning: Example Results





A cat sitting on a suitcase on the floor



A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field



A man riding a dirt bike on a dirt track

# Image Captioning: Failure Cases



A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



A man in a baseball uniform throwing a ball

# Visual Question Answering (VQA)



Q: What endangered animal is featured on the truck?

A: A bald eagle.

A: A sparrow.

A: A humming bird.

A: A raven.



Q: Where will the driver go if turning right?

A: Onto 24 3/4 Rd.

A: Onto 25 3/4 Rd.

A: Onto 23 3/4 Rd.

A: Onto Main Street.



Q: When was the picture taken?

A: During a wedding.

A: During a bar mitzvah.

A: During a funeral.

A: During a Sunday church



Q: Who is under the umbrella?

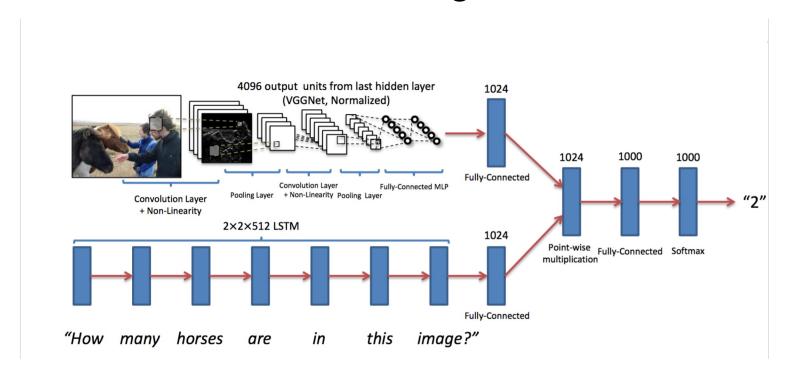
A: Two women.

A: A child.

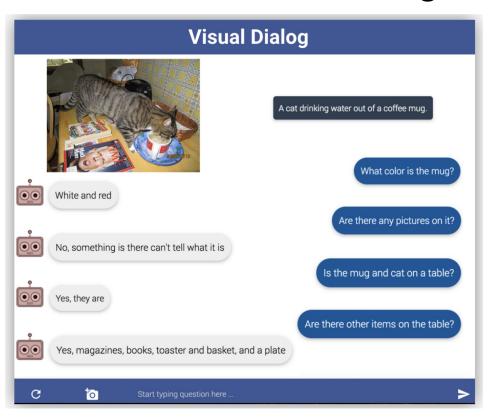
A: An old man.

A: A husband and a wife.

#### Visual Question Answering: RNNs with Attention



# Visual Dialog: Conversations about images



Das et al, "Visual Dialog", CVPR 2017 Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

### Visual Language Navigation: Go to the living room

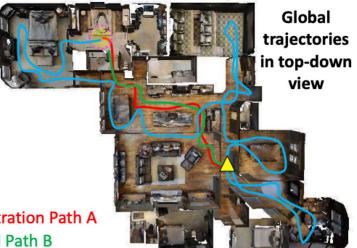
Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

#### Instruction

Turn right and head towards the kitchen. Then turn left, pass a table and enter the hallway. Walk down the hallway and turn into the *entry* way to your right without doors. Stop in front of the *toilet*.

Local visual scene





**Initial Position** 



**Target Position** 

Demonstration Path A



Executed Path C

Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018 Figures from Wang et al. copyright IEEE 2017. Reproduced with permission.

#### RNN tradeoffs

#### RNN Advantages:

- Can process any length input
- Computation for step t can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

#### RNN Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back
- Vanishing gradient / gradient explosion

#### Vanilla RNN

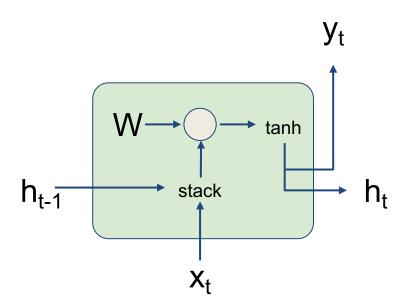
$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

#### **LSTM**

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

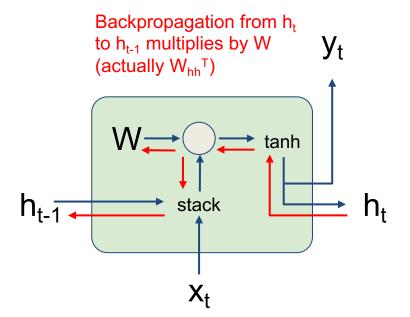
$$h_t = o \odot \tanh(c_t)$$



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

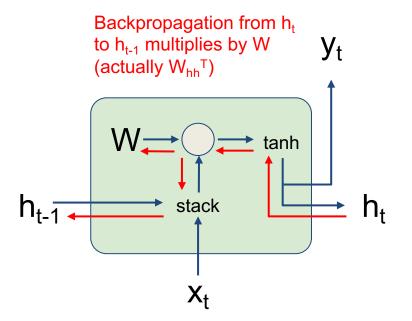
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

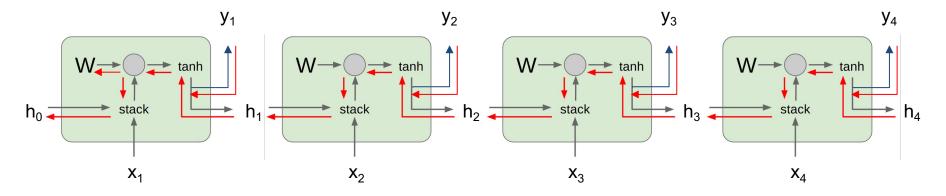


$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$

$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

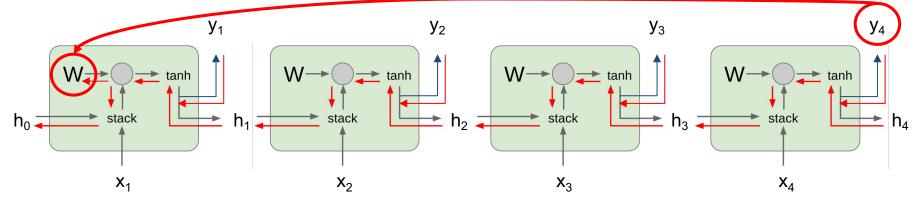
$$= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_{t} \end{pmatrix}\right)$$

$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1} + W_{xh}x_t)W_{hh}$$



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

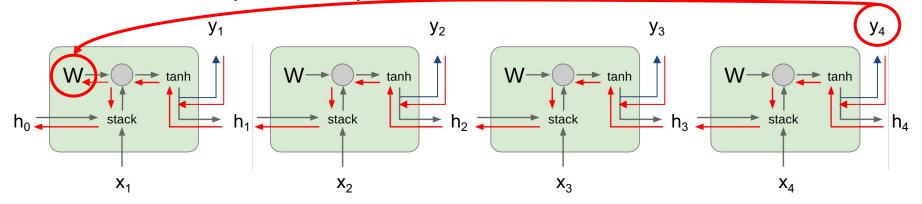
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W}$$

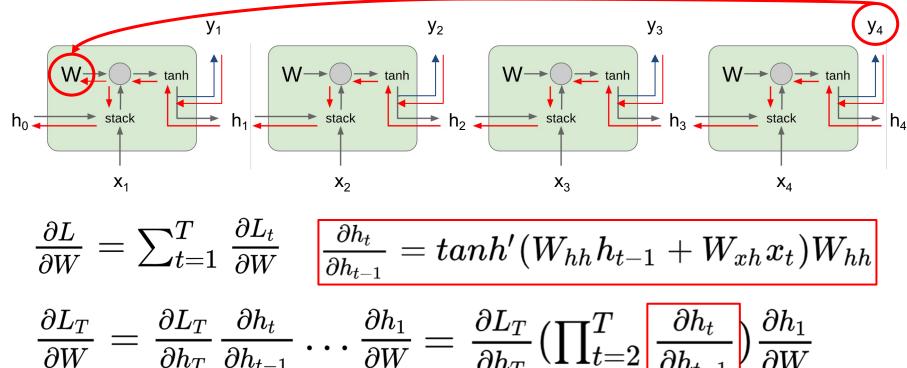
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



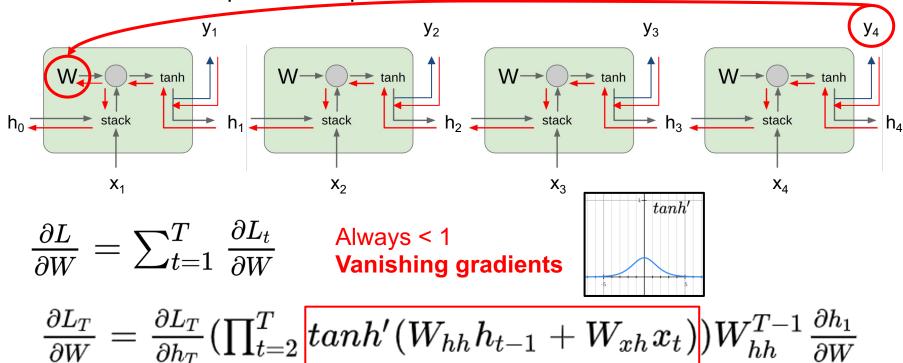
$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T rac{\partial h_t}{\partial h_{t-1}}) rac{\partial h_1}{\partial W}$$

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

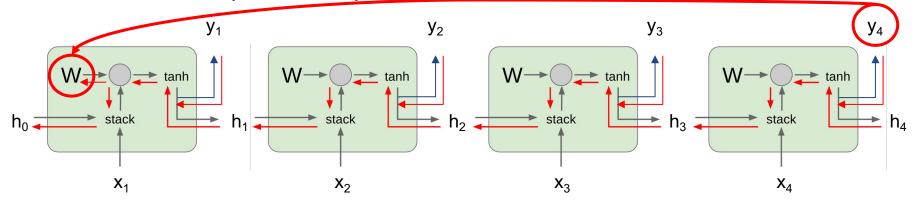


Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:

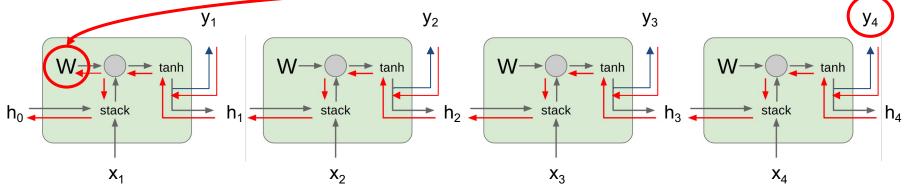


$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

What if we assumed no non-linearity?

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



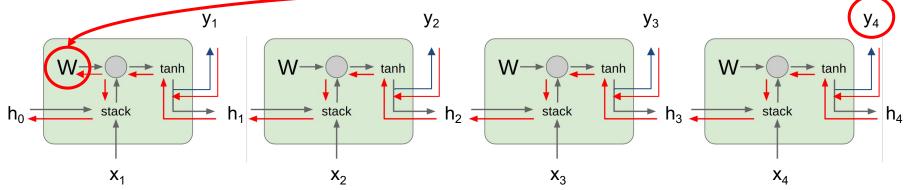
$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest eigen value < 1: **Vanishing gradients** 

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



$$\frac{\partial L}{\partial W} = \sum_{t=1}^{T} \frac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest eigen value > 1: **Exploding gradients** 

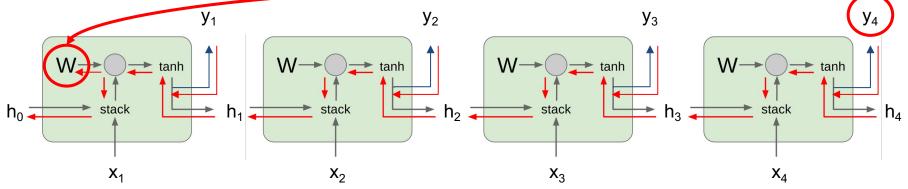
Largest eigen value < 1: Vanishing gradients

→ Gradient clipping: Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
   grad *= (threshold / grad_norm)
```

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



$$rac{\partial L}{\partial W} = \sum_{t=1}^{T} rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} W_{hh}^{T-1} rac{\partial h_1}{\partial W}$$

Largest eigen value > 1: **Exploding gradients** 

→ We need a new RNN architecture!

#### Vanilla RNN

$$h_t = \tanh\left(W\begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)$$

#### **LSTM**

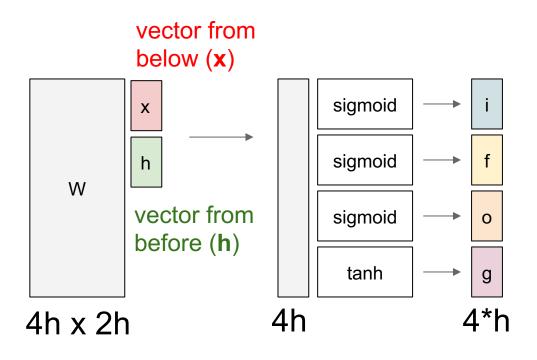
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

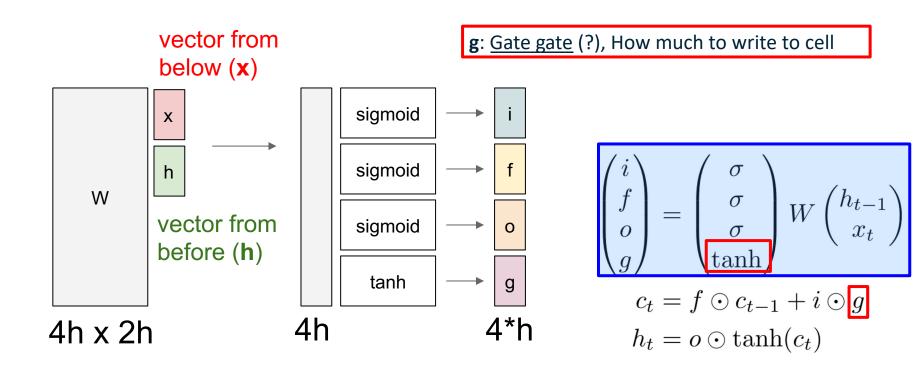
$$h_t = o \odot \tanh(c_t)$$

Learn to control information flow from previous state to the next state

[Hochreiter et al., 1997]

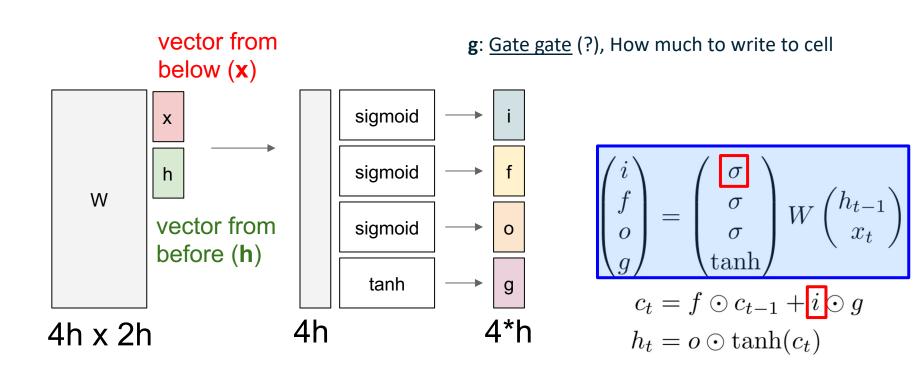


[Hochreiter et al., 1997]



[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

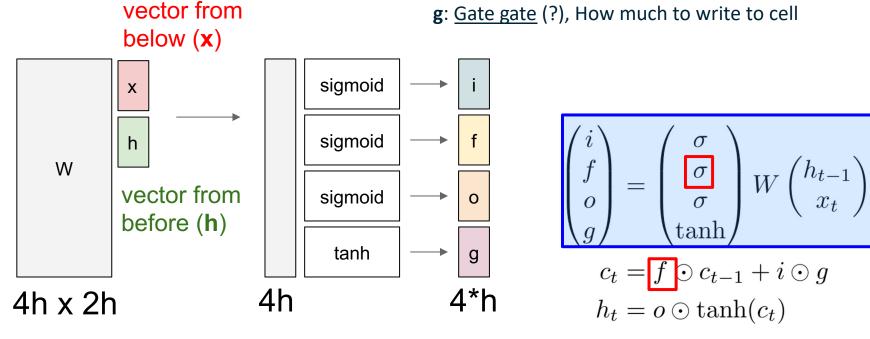


[Hochreiter et al., 1997]

i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

g: Gate gate (?), How much to write to cell



[Hochreiter et al., 1997]

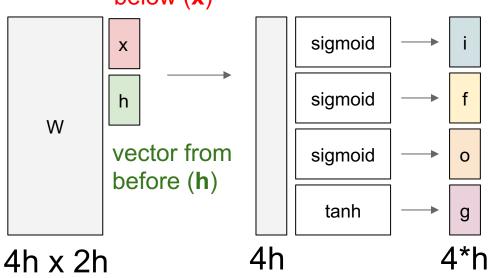
i: Input gate, whether to write to cell

f: Forget gate. Whether to erase cell

o: Output gate, How much to reveal cell

g: Gate gate (?), How much to write to cell



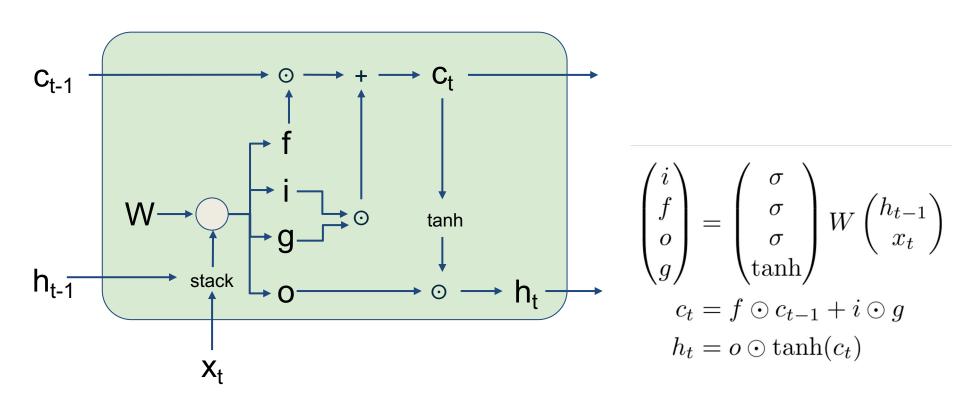


$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \cot \phi \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

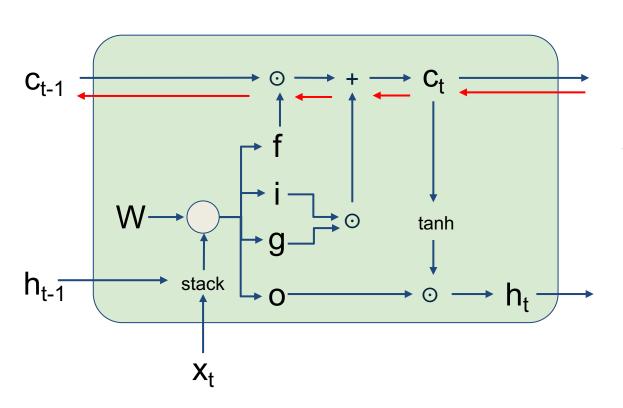
$$h_t = \boxed{o} \odot \tanh(c_t)$$

[Hochreiter et al., 1997]



#### Long Short Term Memory (LSTM): Gradient Flow

[Hochreiter et al., 1997]



Backpropagation from c<sub>t</sub> to c<sub>t-1</sub> only elementwise multiplication by f, no matrix multiply by W

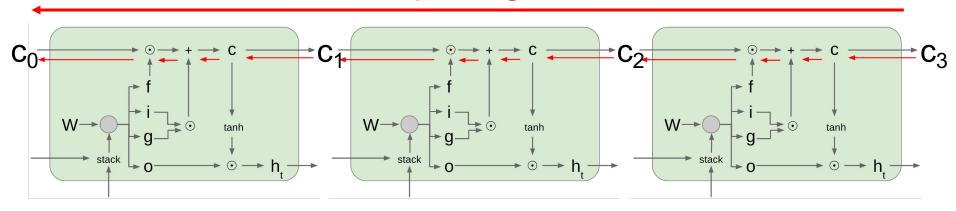
$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

# Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

### Uninterrupted gradient flow!



Notice that the gradient contains the **f** gate's vector of activations

 allows better control of gradients values, using suitable parameter updates of the forget gate.

Also notice that are added through the **f**, **i**, **g**, and **o** gates

- better balancing of gradient values

# Do LSTMs solve the vanishing gradient problem?

The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

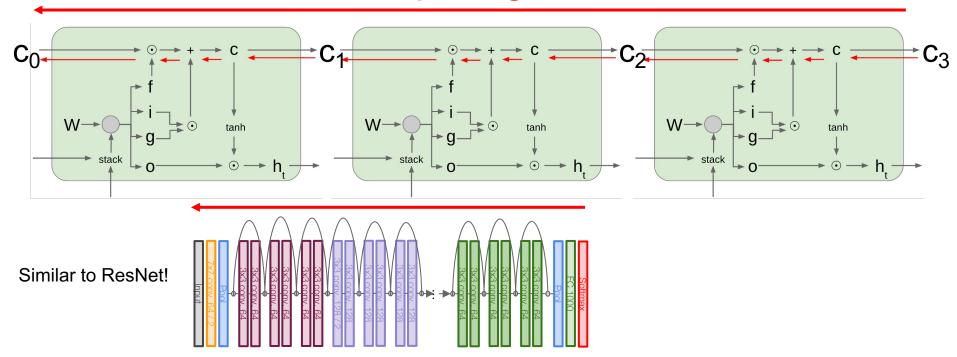
- e.g. **if the f = 1 and the i = 0**, then the information of that cell is preserved indefinitely.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix
   Wh that preserves info in hidden state

LSTM doesn't guarantee that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies.

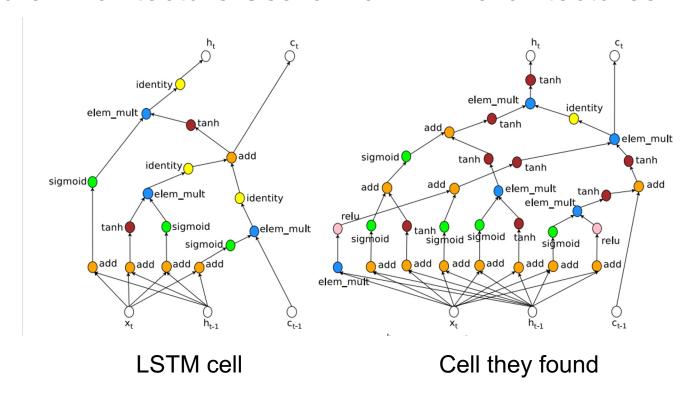
It is possible to mitigate vanishing / exploding gradient by learning the correct i and f.

# Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

# Uninterrupted gradient flow!



#### Neural Architecture Search for RNN architectures



Zoph et Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Figures copyright Zoph et al, 2017. Reproduced with permission.

#### Other RNN Variants

**GRU** [Learning phrase representations using rnn encoder-decoder for statistical machine translation, Cho et al. 2014]

$$r_{t} = \sigma(W_{xr}x_{t} + W_{hr}h_{t-1} + b_{r})$$

$$z_{t} = \sigma(W_{xz}x_{t} + W_{hz}h_{t-1} + b_{z})$$

$$\tilde{h}_{t} = \tanh(W_{xh}x_{t} + W_{hh}(r_{t} \odot h_{t-1}) + b_{h})$$

$$h_{t} = z_{t} \odot h_{t-1} + (1 - z_{t}) \odot \tilde{h}_{t}$$

Simpler than LSTM, control information flow without cell state.

[An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

```
MUT1:
       z = \operatorname{sigm}(W_{xz}x_t + b_z)
       r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)
  h_{t+1} = \tanh(W_{hh}(r \odot h_t) + \tanh(x_t) + b_h) \odot z
            + h<sub>t</sub> ⊙ (1 − z)
MUT2:
        z = \operatorname{sigm}(W_{rr}x_t + W_{hr}h_t + b_r)
        r = \operatorname{sigm}(x_t + W_{hr}h_t + b_r)
   h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z
             + h_t \odot (1-z)
MUT3:
         z = \operatorname{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z)
        r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)
   h_{t+1} = \tanh(W_{hh}(r \odot h_t) + W_{\tau h}x_t + b_h) \odot z
             + h_t \odot (1-z)
```

[LSTM: A Search Space Odyssey, Greff et al., 2015]

#### Recurrence for Vision

- LSTM wer a good default choice until this year
- Use variants like GRU if you want faster compute and less parameters
- Use transformers (next lecture) as they are dominating NLP models
  - almost everyday there is a new vision transformer model

Su et al. "VI-bert: Pre-training of generic visual-linguistic representations." ICLR 2020 Lu et al. "Vilbert: Pretraining task-agnostic visiolinguistic representations for vision-and-language tasks." NeurIPS 2019 Li et al. "Visualbert: A simple and performant baseline for vision and language." *arXiv* 2019

# Summary

- RNNs allow a lot of flexibility in architecture design
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish. Exploding is controlled with gradient clipping. Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.