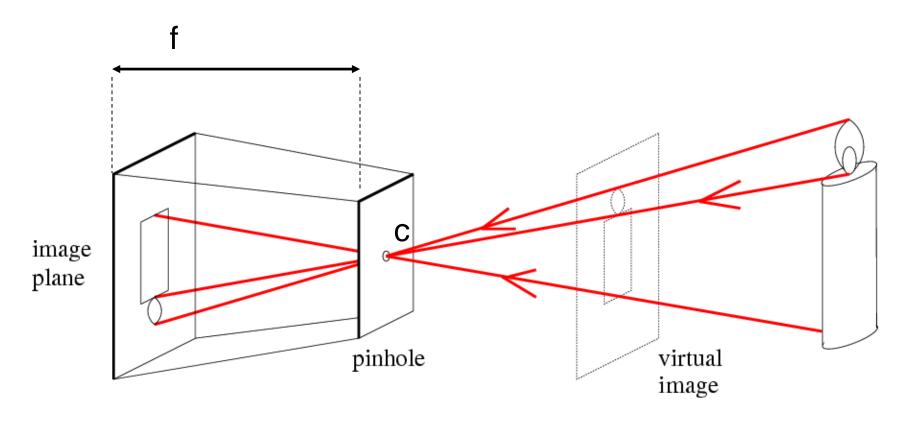




Computer Vision
James Hays

Recap: Light and Sensors

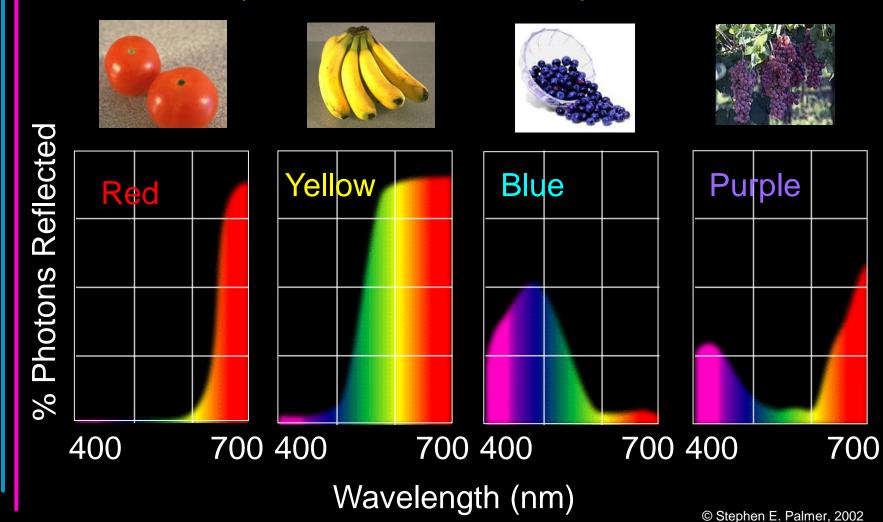
Pinhole camera



f = focal length
c = center of the camera

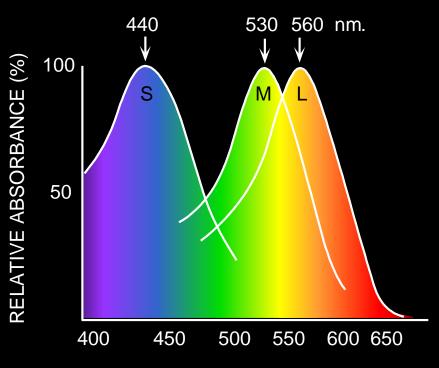
The Physics of Light

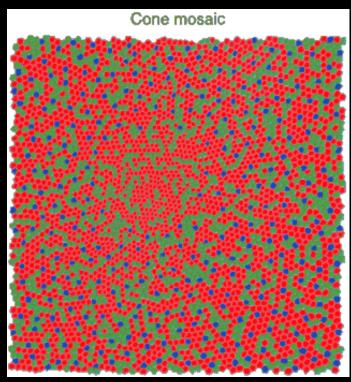
Some examples of the <u>reflectance</u> spectra of <u>surfaces</u>



Physiology of Color Vision

Three kinds of cones:

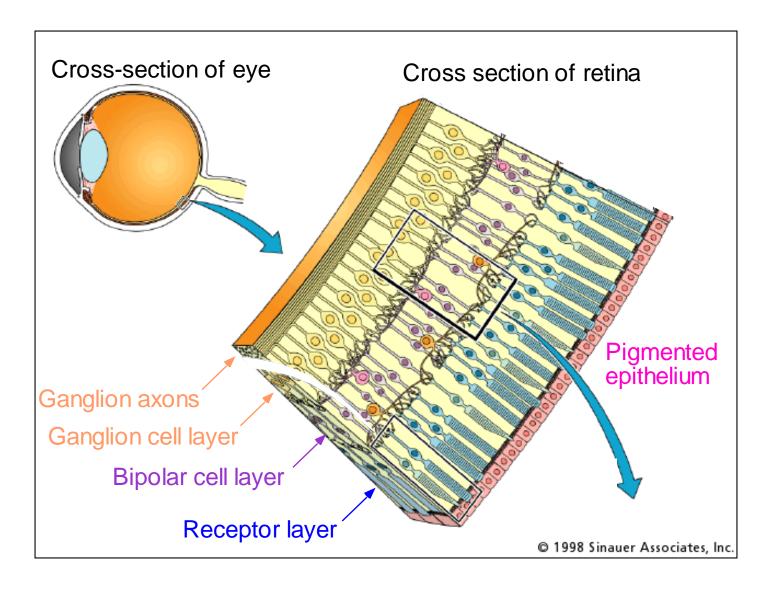




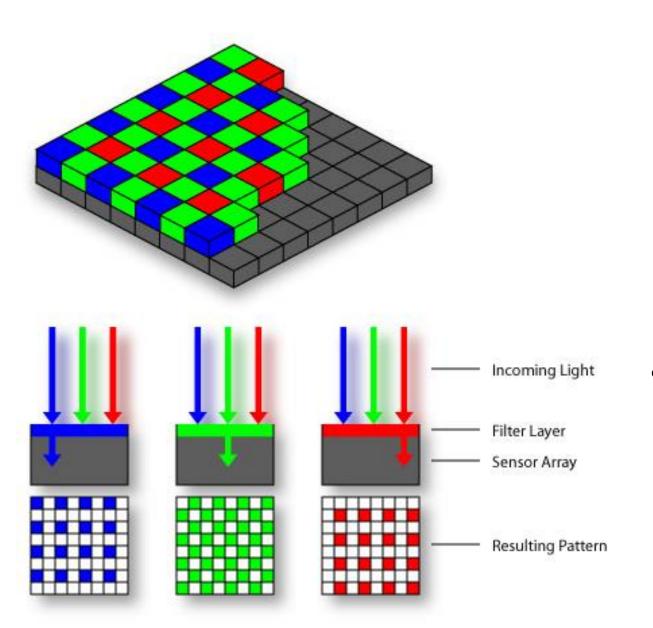
WAVELENGTH (nm.)

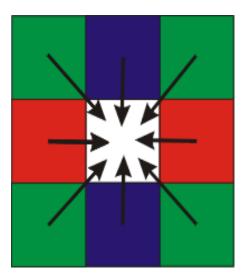
- Why are M and L cones so close?
- Why are there 3?

The Retina



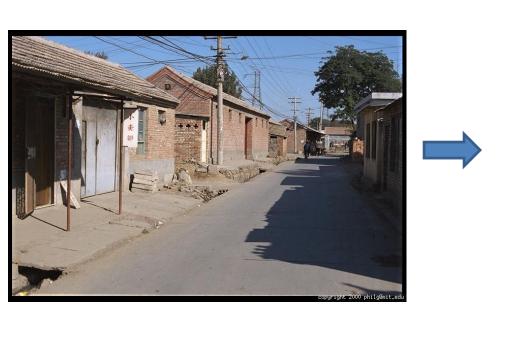
Practical Color Sensing: Bayer Grid





Estimate RGB
 at 'G' cells from
 neighboring
 values

Color Image



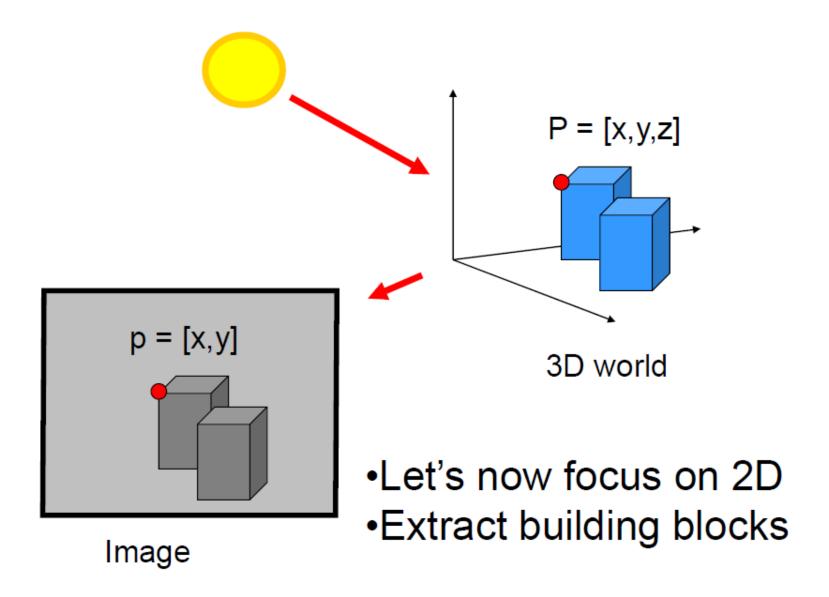


Images in Matlab

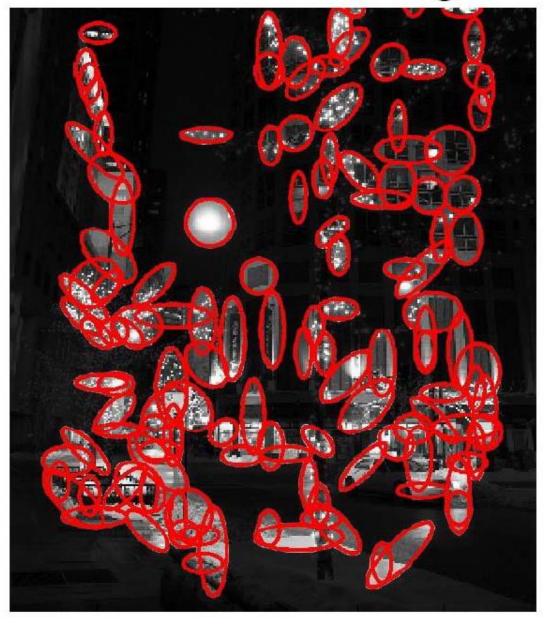
- Images represented as a matrix
- Suppose we have a NxM RGB image called "im"
 - im(1,1,1) = top-left pixel value in R-channel
 - im(y, x, b) = y pixels down, x pixels to right in the bth channel
 - im(N, M, 3) = bottom-right pixel in B-channel
- imread(filename) returns a uint8 image (values 0 to 255)
 - Convert to double format (values 0 to 1) with im2double

	col	um	n -									\Rightarrow				
row	0.92	0.93	0.94	0.97	0.62	0.37	0.85	0.97	0.93	0.92	0.99	R				
	0.95	0.89	0.82	0.89	0.56	0.31	0.75	0.92	0.81	0.95	0.91					
	0.89	0.72	0.51	0.55	0.51	0.42	0.57	0.41	0.49	0.91	0.92	0.92	0.99	ı G		
	0.96	0.95	0.88	0.94	0.56	0.46	0.91	0.87	0.90	0.97	0.95	0.95	0.91			_
	0.71	0.81	0.81	0.87	0.57	0.37	0.80	0.88	0.89	0.79	0.85	0.91	0.92			В
	0.49	0.62	0.60	0.58	0.50	0.60	0.58	0.50	0.61	0.45	0.33	0.97	0.95	0.92	0.99	
	0.86	0.84	0.74	0.58	0.51	0.39	0.73	0.92	0.91	0.49	0.74	0.79	0.85	0.95	0.91	
	0.96	0.67	0.54	0.85	0.48	0.37	0.88	0.90	0.94	0.82	0.93	0.45	0.33	0.91	0.92	
	0.69	0.49	0.56	0.66	0.43	0.42	0.77	0.73	0.71	0.90	0.99	0.49	0.74	0.97	0.95	
	0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	0.43	0.93	0.79	0.85	
V	0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	0.90	0.99	0.45	0.33	
			0.79	0.73	0.90	0.67	0.33	0.42	0.69	0.79	0.73	0.93	0.97	0.49	0.74	
			0.79	0.73	0.89	0.67	0.33	0.01	0.03	0.73	0.73	0.93	0.97	0.82	0.93	
			0.91	0.94	0.05	0.49	0.41	0.78	0.78	0.77	0.77	0.75	0.93	0.90	0.99	
					0.79	0.73	0.90	0.67	0.33	0.61	0.69	0.79	0.73	0.93	0.97	
					0.91	0.94	0.89	0.49	0.41	0.78	0.78	0.77	0.89	0.99	0.93	

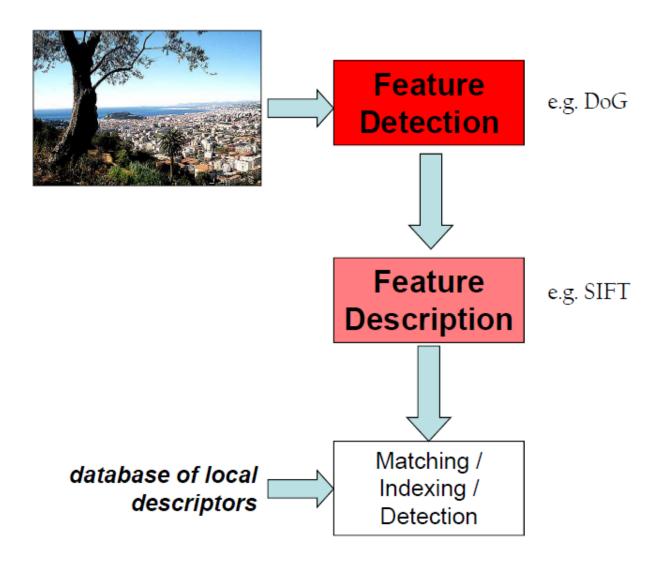
From the 3D to 2D



Extract useful building blocks



The big picture...





Computer Vision
James Hays

Upcoming classes: three views of filtering

- Image filters in spatial domain
 - Filter is a mathematical operation of a grid of numbers
 - Smoothing, sharpening, measuring texture
- Image filters in the frequency domain
 - Filtering is a way to modify the frequencies of images
 - Denoising, sampling, image compression
- Templates and Image Pyramids
 - Filtering is a way to match a template to the image
 - Detection, coarse-to-fine registration

 Image filtering: compute function of local neighborhood at each position

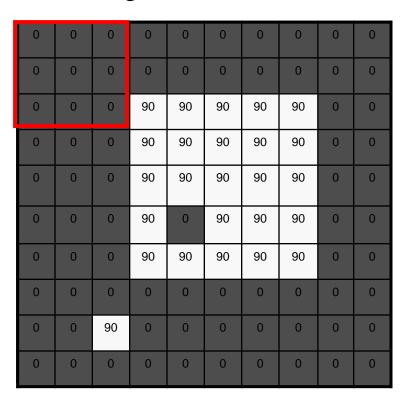
- Really important!
 - Enhance images
 - Denoise, resize, increase contrast, etc.
 - Extract information from images
 - Texture, edges, distinctive points, etc.
 - Detect patterns
 - Template matching
 - Deep Convolutional Networks

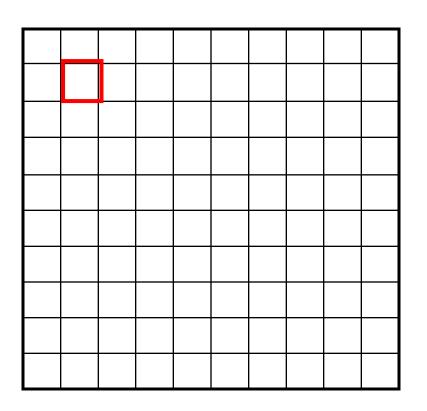
Example: box filter

$$g[\cdot,\cdot]$$

$$\frac{1}{9}\begin{bmatrix} 1 & 1 & 1 \\ 1 & 1 & 1 \\ 1 & 1 & 1 \end{bmatrix}$$

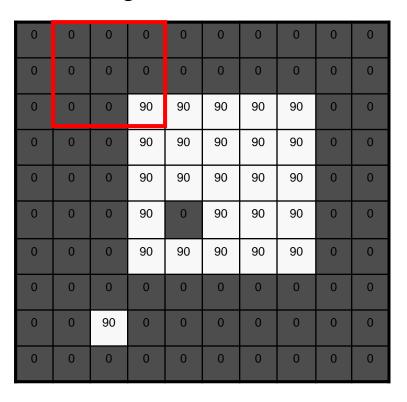
$$g[\cdot,\cdot]^{\frac{1}{9}}$$

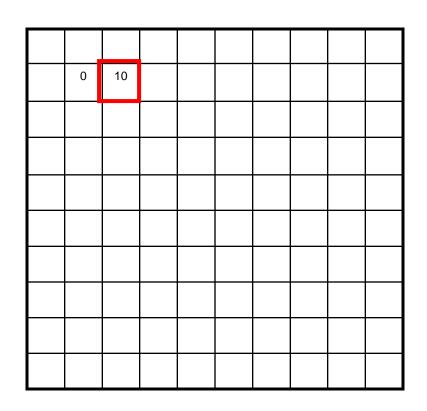




$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

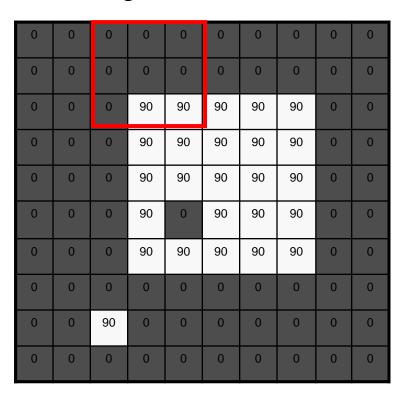
$$g[\cdot,\cdot]^{\frac{1}{9}}$$

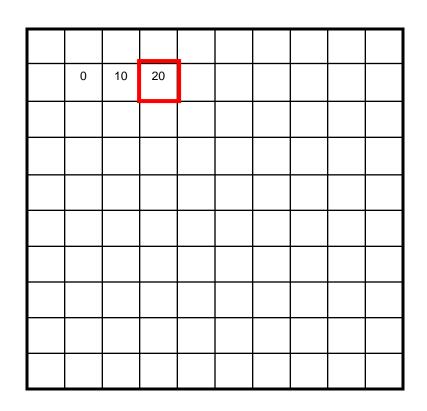




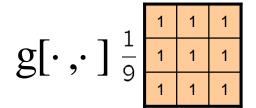
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

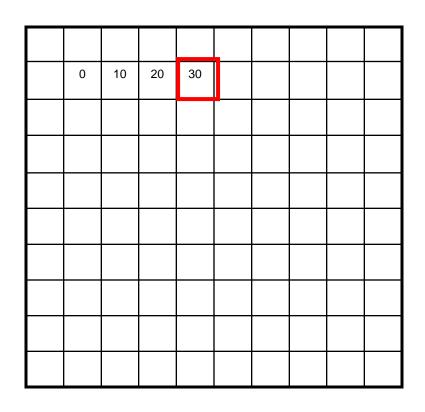




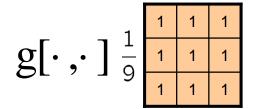
$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

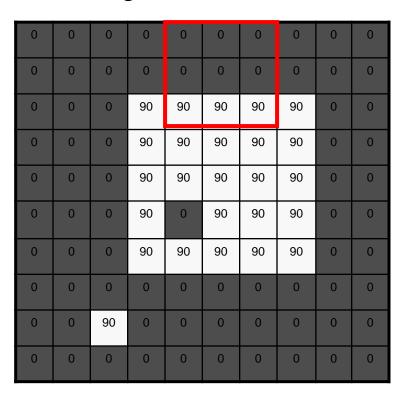


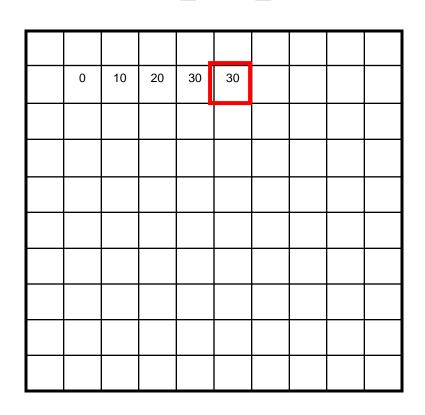
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$



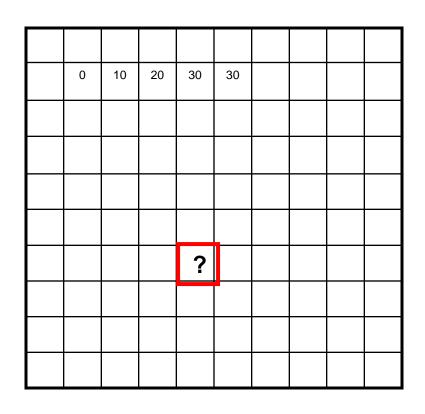




$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

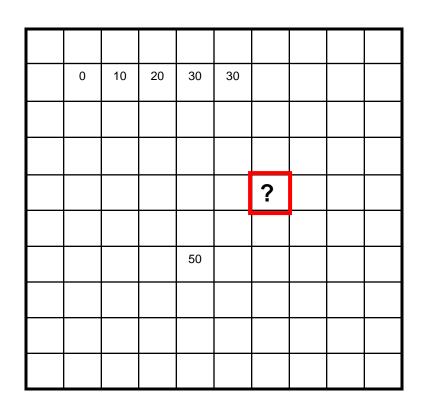
0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]^{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0



$$h[m,n] = \sum_{k,l} g[k,l] f[m+k,n+l]$$

$$g[\cdot,\cdot]_{\frac{1}{9}}$$

0	0	0	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	90	0	90	90	90	0	0
0	0	0	90	90	90	90	90	0	0
0	0	0	0	0	0	0	0	0	0
0	0	90	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0	0	0

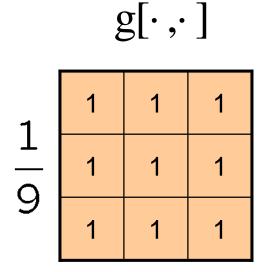
0	10	20	30	30	30	20	10	
0	20	40	60	60	60	40	20	
0	30	60	90	90	90	60	30	
0	30	50	80	80	90	60	30	
0	30	50	80	80	90	60	30	
0	20	30	50	50	60	40	20	
10	20	30	30	30	30	20	10	
10	10	10	0	0	0	0	0	

$$h[m,n] = \sum_{l=1}^{n} g[k,l] f[m+k,n+l]$$

Box Filter

What does it do?

- Replaces each pixel with an average of its neighborhood
- Achieve smoothing effect (remove sharp features)



Smoothing with box filter





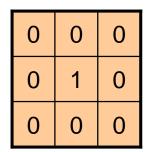
\sim	•	•	1
()1	r19	211	ıal
	7	7	

0	0	0
0	1	0
0	0	0





Original





Filtered (no change)



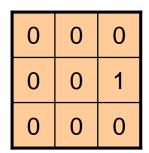
\sim	•	•	1
O_1	r19	711	าลไ
<u> </u>	٦- ٦	>**	101

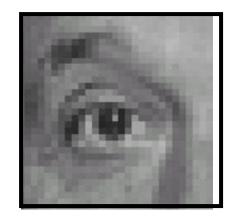
0	0	0
0	0	1
0	0	0





Original





Shifted left By 1 pixel



Original

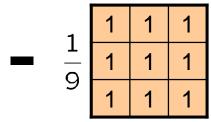
0	0	0	1	1	1	1
0	2	0	<u> </u>	1	1	1
0	0	0	9	1	1	1

(Note that filter sums to 1)

Source: D. Lowe



0	0	0
0	2	0
0	0	0



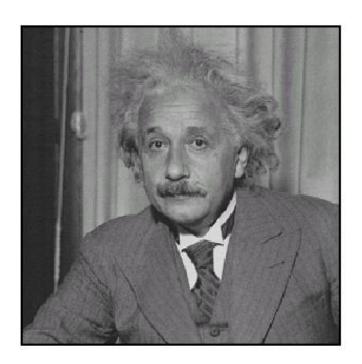


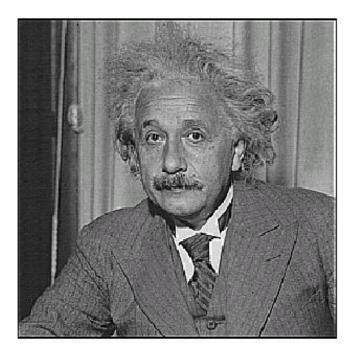
Original

Sharpening filter

- Accentuates differences with local average

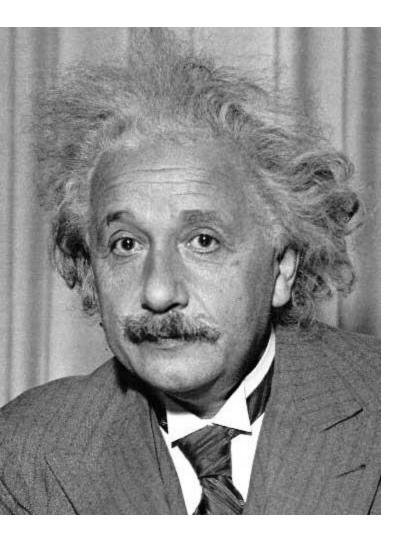
Sharpening





before after

Other filters



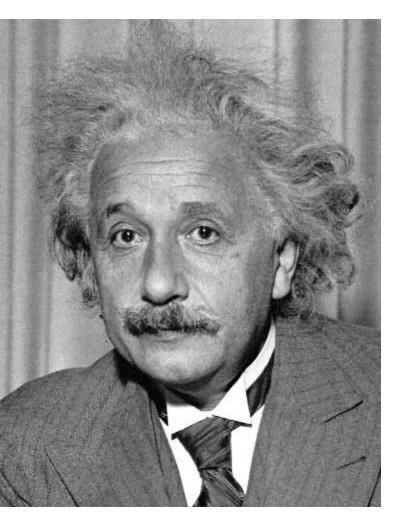
1	0	-1
2	0	-2
1	0	-1

Sobel



Vertical Edge (absolute value)

Other filters



1	2	1
0	0	0
-1	- 2	-1

Sobel



Horizontal Edge (absolute value)

Filtering vs. Convolution

• 2d filtering f=filter I=image -h=filter2(f,I); or h=imfilter(I,f); $h[m,n] = \sum_{k,l} f[k,l] I[m+k,n+l]$

2d convolution

-h=conv2(f, I);
$$h[m,n] = \sum_{k,l} f[k,l] I[m-k,n-l]$$

Key properties of linear filters

Linearity:

```
imfilter(I, f_1 + f_2) =
imfilter(I, f_1) + imfilter(I, f_2)
```

Shift invariance: same behavior regardless of pixel location

```
imfilter(I, shift(f)) = shift(imfilter(I, f))
```

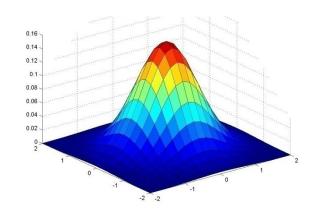
Any linear, shift-invariant operator can be represented as a convolution

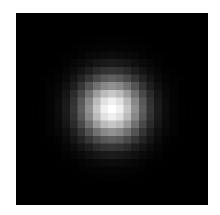
More properties

- Commutative: *a* * *b* = *b* * *a*
 - Conceptually no difference between filter and signal
 - But particular filtering implementations might break this equality
- Associative: a * (b * c) = (a * b) * c
 - Often apply several filters one after another: $(((a * b_1) * b_2) * b_3)$
 - This is equivalent to applying one filter: a * $(b_1 * b_2 * b_3)$
- Distributes over addition: a * (b + c) = (a * b) + (a * c)
- Scalars factor out: ka * b = a * kb = k (a * b)
- Identity: unit impulse e = [0, 0, 1, 0, 0],
 a * e = a

Important filter: Gaussian

Weight contributions of neighboring pixels by nearness





0.003	0.013	0.022	0.013	0.003
0.013	0.059	0.097	0.059	0.013
0.022	0.097	0.159	0.097	0.022
0.013	0.059	0.097	0.059	0.013
0.003	0.013	0.022	0.013	0.003

$$5 \times 5$$
, $\sigma = 1$

$$G_{\sigma} = \frac{1}{2\pi\sigma^2} e^{-\frac{(x^2+y^2)}{2\sigma^2}}$$

Smoothing with Gaussian filter



Smoothing with box filter



Gaussian filters

- Remove "high-frequency" components from the image (low-pass filter)
 - Images become more smooth
- Convolution with self is another Gaussian
 - So can smooth with small-width kernel, repeat, and get same result as larger-width kernel would have
 - Convolving two times with Gaussian kernel of width σ is same as convolving once with kernel of width σ V2
- Separable kernel
 - Factors into product of two 1D Gaussians

Separability of the Gaussian filter

$$G_{\sigma}(x,y) = \frac{1}{2\pi\sigma^2} \exp^{-\frac{x^2 + y^2}{2\sigma^2}}$$

$$= \left(\frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{x^2}{2\sigma^2}}\right) \left(\frac{1}{\sqrt{2\pi}\sigma} \exp^{-\frac{y^2}{2\sigma^2}}\right)$$

The 2D Gaussian can be expressed as the product of two functions, one a function of x and the other a function of y

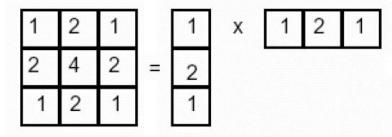
In this case, the two functions are the (identical) 1D Gaussian

Separability example

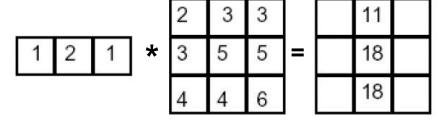
2D convolution (center location only)

1	2	1		2	3	3
2	4	2	*	3	5	5
1	2	1		4	4	6

The filter factors into a product of 1D filters:



Perform convolution along rows:



Followed by convolution along the remaining column:

Separability

Why is separability useful in practice?

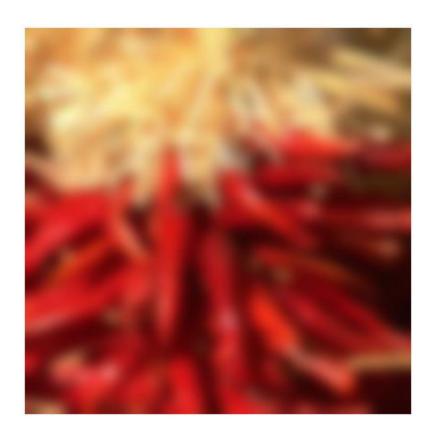
Some practical matters

Practical matters How big should the filter be?

- Values at edges should be near zero
- Rule of thumb for Gaussian: set filter half-width to about 3 σ

Practical matters

- What about near the edge?
 - the filter window falls off the edge of the image
 - need to extrapolate
 - methods:
 - clip filter (black)
 - wrap around
 - copy edge
 - reflect across edge



To be continued...

Next class: Thinking in Frequency

