

## Advanced Viewing: PHIGS

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- Two coordinate systems
  - | World reference coordinate system (WRC)
  - | Viewing reference coordinate system (VRC)

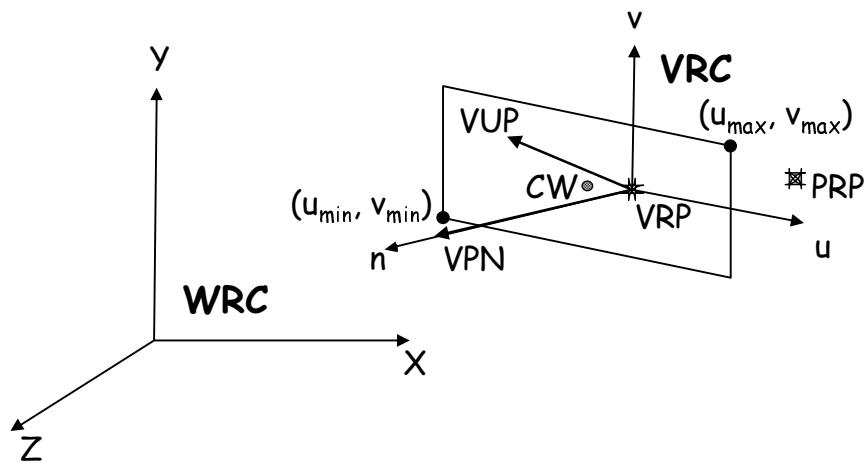
## Arbitrary view reference point

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- Specify viewplane, view coords (WRC)
  - | View Reference Point (VRP)
  - | View Plane Normal (VPN)
  - | View Up Vector (VUV)
- Specify window on the view plane (VRC)
  - | Max and min u,v values (window center (CW))
  - | Projection Reference Point (PRP)
    - | Ignore VPD from book ...

## Specifying a view



## Normalizing Transformation for Perspective Views

1. Translate VRP to origin
2. Rotate the VRC system so that VPN become z-axis, u become x-axis and v become y-axis
3. Translate so that the CoP given by the PRP is at origin
4. Shear such that the center line of the view volume becomes the z-axis
5. Scale so that the view volume becomes the canonical view volume

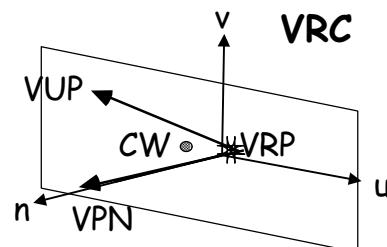
## 1. Translate VRP to origin

$$\begin{pmatrix} 1 & 0 & 0 & -\text{VRP}_x \\ 0 & 1 & 0 & -\text{VRP}_y \\ 0 & 0 & 1 & -\text{VRP}_z \\ 0 & 0 & 0 & 1 \end{pmatrix} = T(-\text{VRP})$$

## 2. Rotate VRC

We want to take  $u$  into  $(1, 0, 0)$   
 $v$  into  $(0, 1, 0)$   
 $n$  into  $(0, 0, 1)$

First derive  $n$ ,  $u$ , and  $v$  from user input:



## 2. Rotate VRC (cont.)

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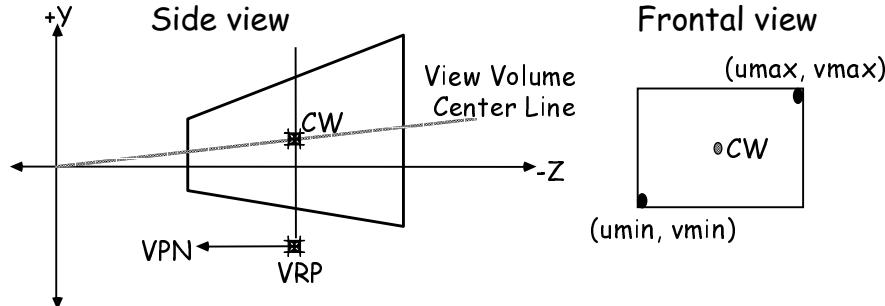
$$\begin{pmatrix} u_x & u_y & u_z & 0 \\ v_x & v_y & v_z & 0 \\ n_x & n_y & n_z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} = R_{VRC}$$

## 3. Translate PRP to the origin

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$$\begin{pmatrix} 1 & 0 & 0 & -PRP_u \\ 0 & 1 & 0 & -PRP_v \\ 0 & 0 & 1 & -PRP_n \\ 0 & 0 & 0 & 1 \end{pmatrix} = T(-PRP)$$

#### 4. Shear such that the center line of the view volume becomes the z-axis



**Direction of projection (DoP) = CW - PRP**

The center line of the view volume is DoP

#### Shear (cont.)

Multiply DoP with a matrix to get  $(0,0,\text{DoP}_z)$

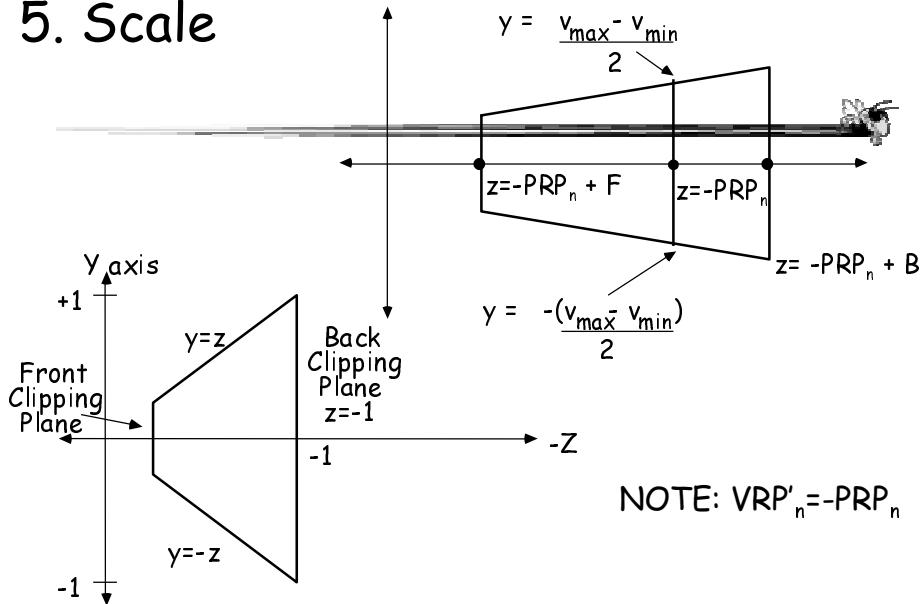
We want  $\text{SH} * \text{DoP} = (0,0,\text{DoP}_z)$

$$\text{SH} = \begin{pmatrix} 1 & 0 & \text{SHx} & 0 \\ 0 & 1 & \text{SHy} & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

$$\text{SHx} =$$

$$\text{SHy} =$$

## 5. Scale



## 5. Scale (cont.)

Scale is done in two steps:

1. First scale in x and y

$$xscale = 2 PRP_n / (u_{\max} - u_{\min})$$

$$yscale = 2 PRP_n / (v_{\max} - v_{\min})$$

2. Scale everything uniformly such that the back clipping plane becomes  $z = -1$

$$xscale = 1 / (-PRP_n + B)$$

$$yscale = 1 / (-PRP_n + B)$$

$$zscale = 1 / (-PRP_n + B)$$

## Total Composite Transformation

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$$N_{per} = S_{per} \cdot SH_{per} \cdot T(-PRP) \cdot R \cdot T(-VRP)$$

Use this to transform from the viewing to the world space, then project onto the viewplane.