

## Advanced Viewing: PHIGS

---



- Two coordinate systems
  - ┆ World reference coordinate system (WRC)
  
  - ┆ Viewing reference coordinate system (VRC)

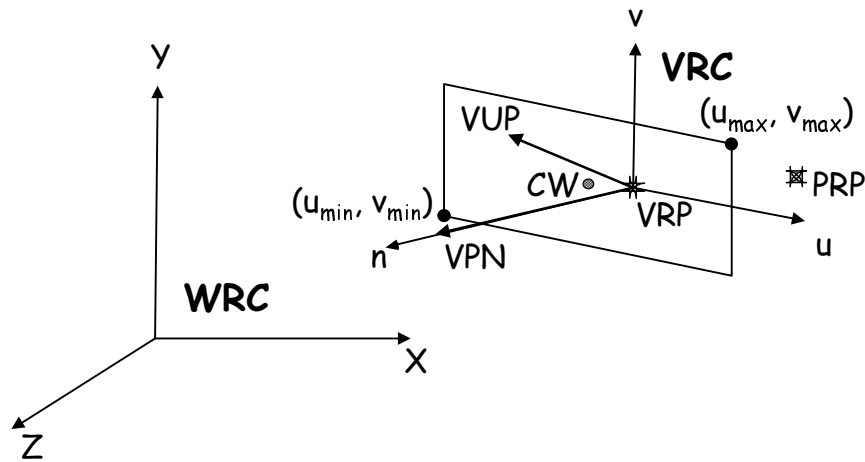
## Arbitrary view reference point

---



- Specify viewplane, view coords (WRC)
  - ┆ View Reference Point (VRP)
  - ┆ View Plane Normal (VPN)
  - ┆ View Up Vector (VUV)
- Specify window on the view plane (VRC)
  - ┆ Max and min  $u, v$  values (window center (CW))
  - ┆ Projection Reference Point (PRP)
    - ┆ Ignore VPD from book ...

## Specifying a view



## Normalizing Transformation for Perspective Views

1. Translate VRP to origin
2. Rotate the VRC system so that VPN become z-axis,  $u$  become x-axis and  $v$  become y-axis
3. Translate so that the CoP given by the PRP is at origin
4. Shear such that the center line of the view volume becomes the z-axis
5. Scale so that the view volume becomes the canonical view volume

## 1. Translate VRP to origin

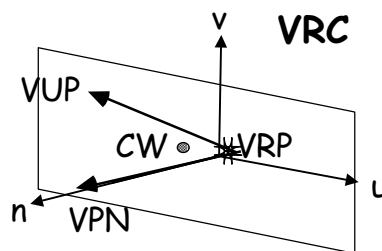
$$\begin{pmatrix} 1 & 0 & 0 & -VRP_x \\ 0 & 1 & 0 & -VRP_y \\ 0 & 0 & 1 & -VRP_z \\ 0 & 0 & 0 & 1 \end{pmatrix} = T(-VRP)$$

## 2. Rotate VRC

We want to take

- u into (1, 0, 0)
- v into (0, 1, 0)
- n into (0, 0, 1)

First derive n, u, and v from user input:



## 2. Rotate VRC (cont.)

---

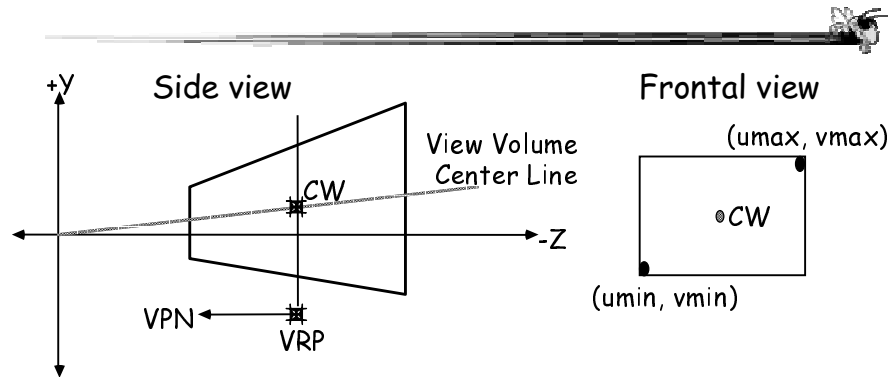
$$\begin{pmatrix} u_x & u_y & u_z & 0 \\ v_x & v_y & v_z & 0 \\ n_x & n_y & n_z & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix} = \mathbf{R}_{VRC}$$

## 3. Translate PRP to the origin

---

$$\begin{pmatrix} 1 & 0 & 0 & -PRP_u \\ 0 & 1 & 0 & -PRP_v \\ 0 & 0 & 1 & -PRP_n \\ 0 & 0 & 0 & 1 \end{pmatrix} = \mathbf{T}(-PRP)$$

#### 4. Shear such that the center line of the view volume becomes the z-axis



**Direction of projection (DoP) = CW - PRP**  
 The center line of the view volume is DoP

#### Shear (cont.)

Multiply DoP with a matrix to get  $(0,0,DoP_z)$

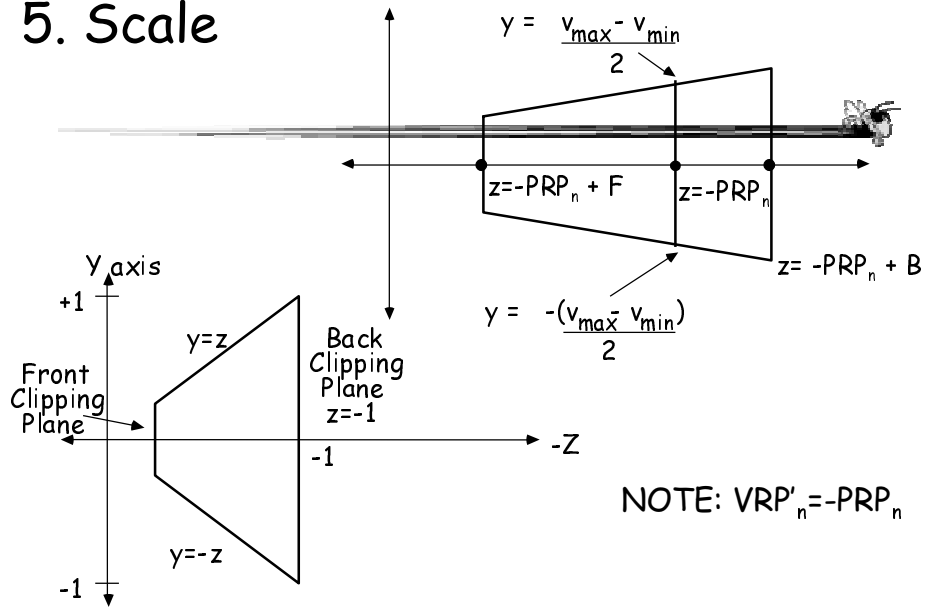
We want  $SH * DoP = (0,0,DoP_z)$

$$SH = \begin{pmatrix} 1 & 0 & SHx & 0 \\ 0 & 1 & SHy & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{pmatrix}$$

SHx =

SHy =

## 5. Scale



## 5. Scale (cont.)

Scale is done in two steps:

1. First scale in x and y

$$xscale = 2 PRP_n / (u_{\max} - u_{\min})$$

$$yscale = 2 PRP_n / (v_{\max} - v_{\min})$$

2. Scale everything uniformly such that the back clipping plane becomes  $z = -1$

$$xscale = 1 / (-PRP_n + B)$$

$$yscale = 1 / (-PRP_n + B)$$

$$zscale = 1 / (-PRP_n + B)$$

## Total Composite Transformation

$$N_{per} = S_{per} SH_{per} T(-PRP) R T(-VRP)$$

Use this to transform from the viewing to the world space, then project onto the viewplane.